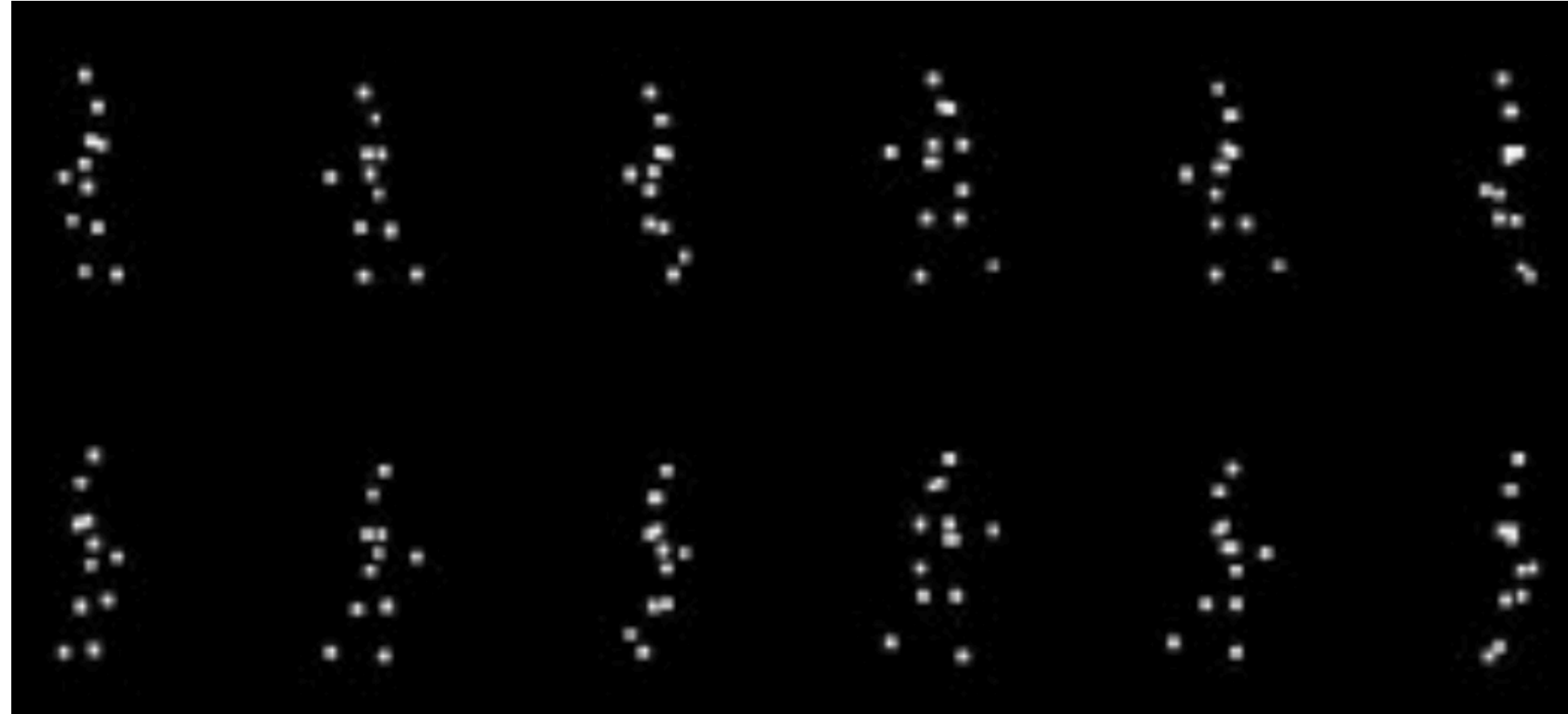


Graph dictionary learning for the study of human motion

Marion Chauveau, Antoine Mazarguil and Laurent Oudre

Université Paris-Saclay, Université Paris Cité, ENS Paris Saclay, CNRS, SSA,
INSERM, Centre Borelli, F-91190, Gif-sur-Yvette, France

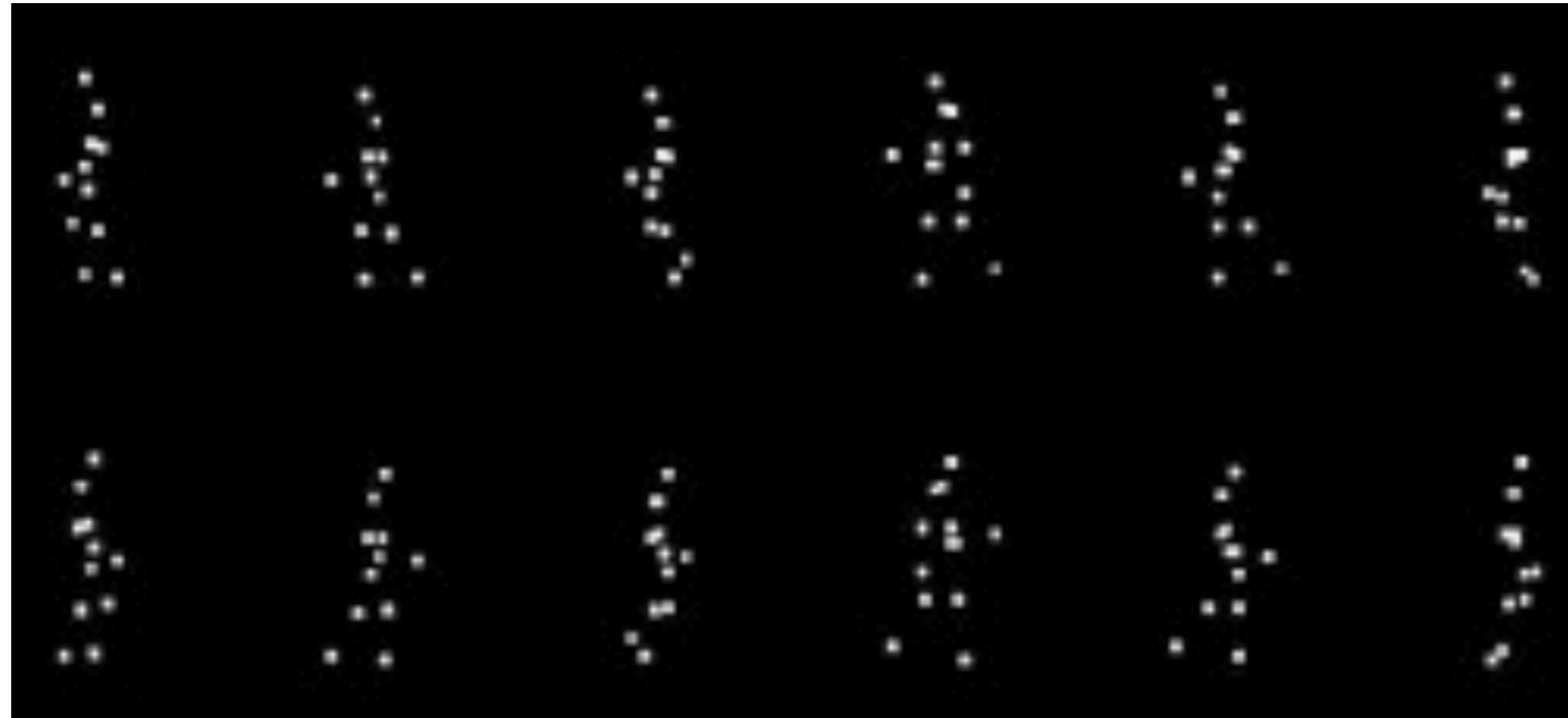
Skeleton-based motion data



Film that illustrates the work of Gunnar Johansson on Motion perception, 1971, James Maas, Cornell University.

- L. Feng et al, A comparative review of graph convolutional networks for human skeleton-based action recognition, 2022
- Q. Wang et al, Visual analysis of human motion: A survey on recent advances and applications, 2018
- Z. Kertesz et al, 3d motion capture methods for pathological and non-pathological human motion analysis, 2006
- S. Tanaka et al, Determination of human motion for rehabilitation based on time-scale transformation, 2007
- G. Johansson, Visual perception of biological motion and a model for its analysis, 1973

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Film that illustrates the work of Gunnar Johansson on Motion perception, 1971, James Maas, Cornell University.

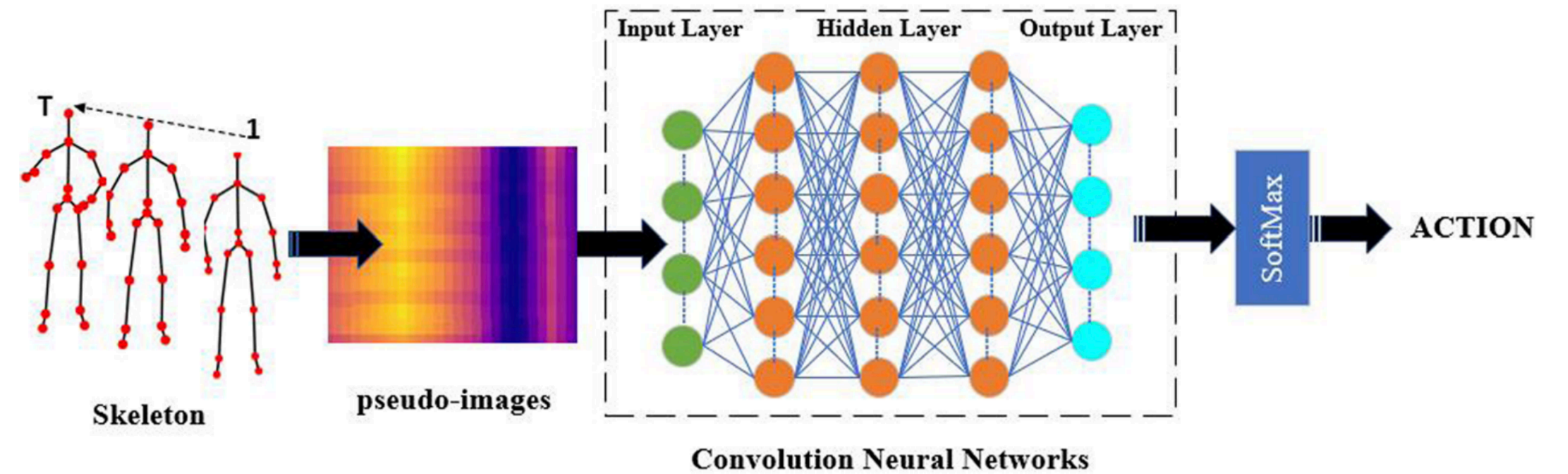


Illustration of a CNN-based human action recognition, L. Feng et al, 2022

L. Feng et al, A comparative review of graph convolutional networks for human skeleton-based action recognition, 2022

Q. Wang et al, Visual analysis of human motion: A survey on recent advances and applications, 2018

Z. Kertesz et al, 3d motion capture methods for pathological and non-pathological human motion analysis, 2006

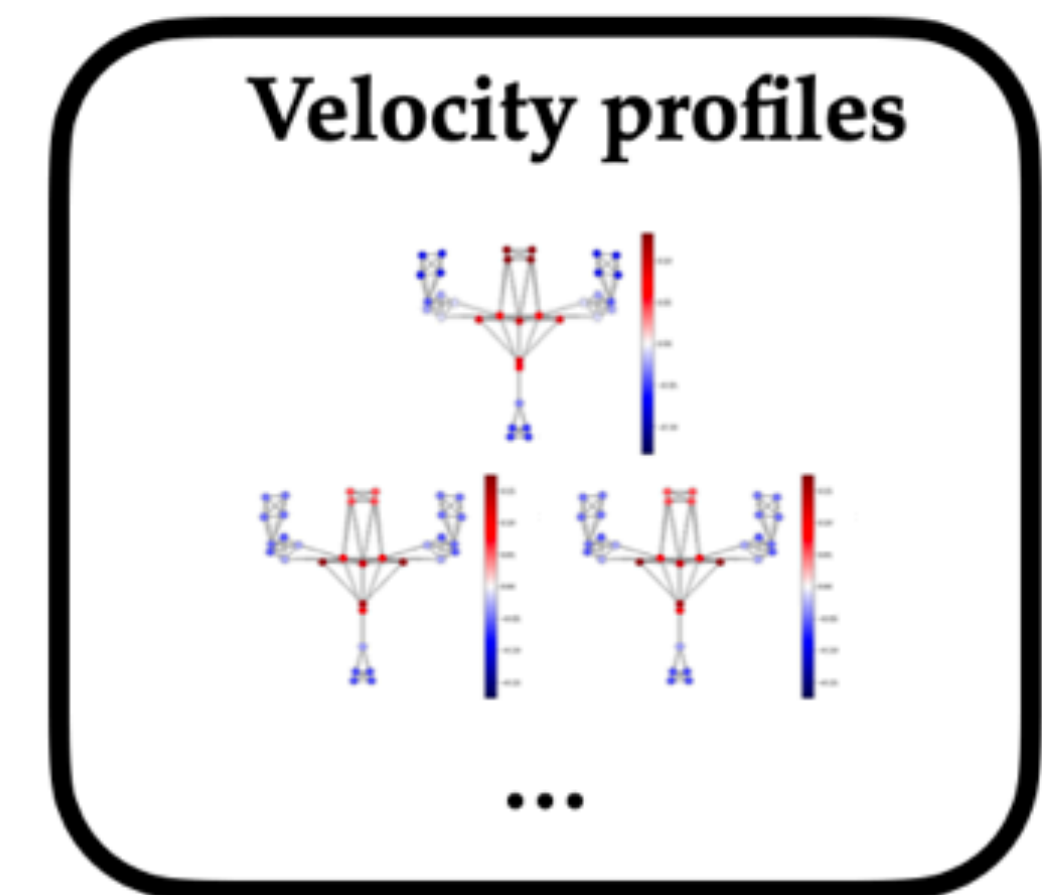
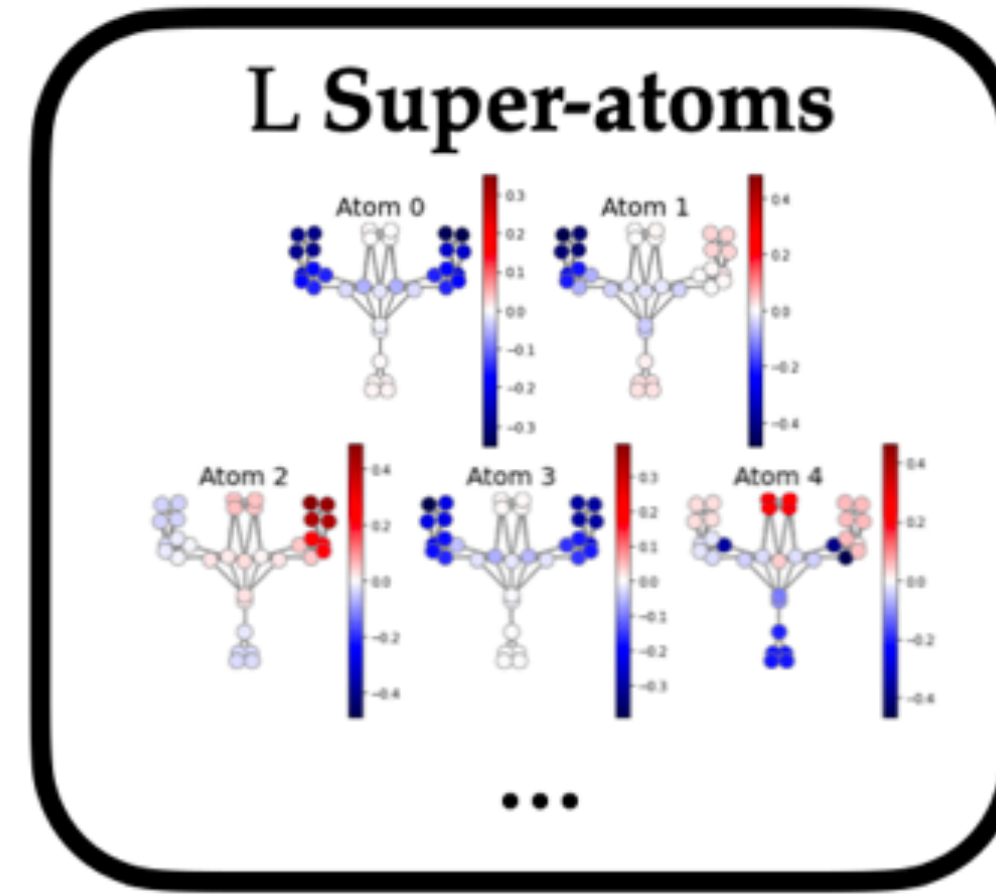
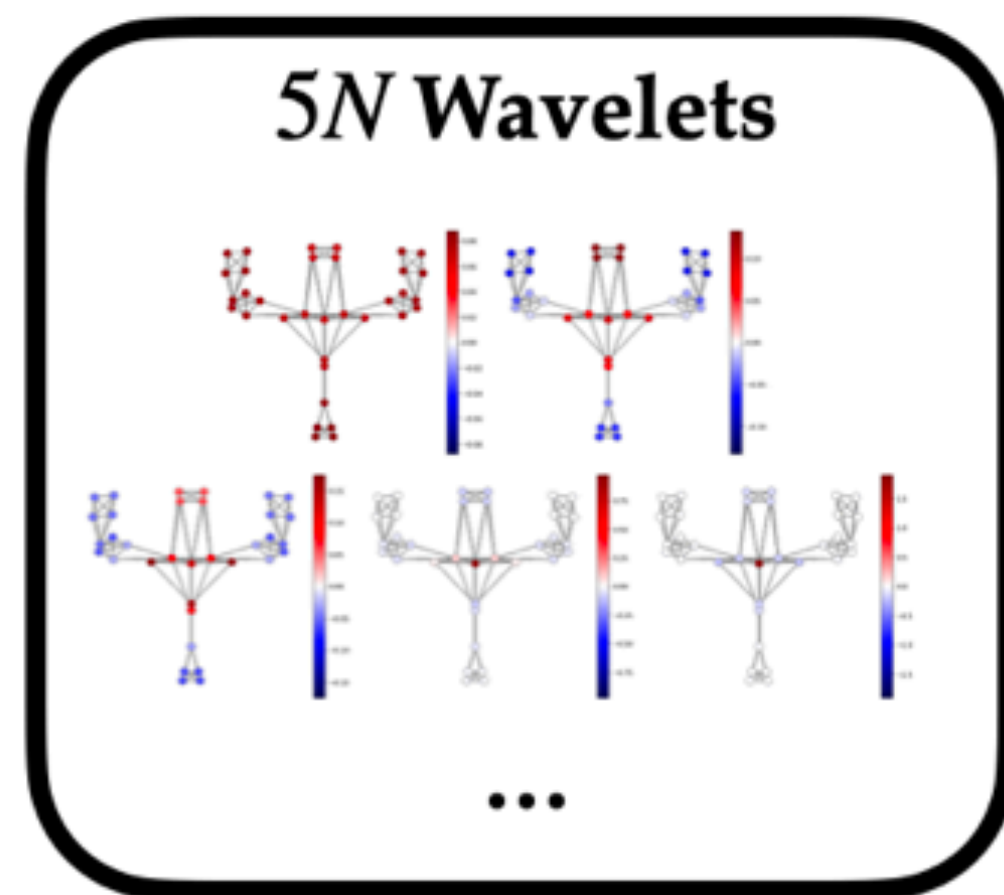
S. Tanaka et al, Determination of human motion for rehabilitation based on time-scale transformation, 2007

G. Johansson, Visual perception of biological motion and a model for its analysis, 1973

Graph dictionary learning approach

Construction of $L = 10$
super-atoms by combining
at most $P = 5$ wavelets

Use of at most $T = 3$ super-atoms
to approximate each graph signal

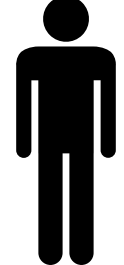


Upper limbs movements: Arm-CODA

Subjects :  × 16

 Healthy subjects

Upper limbs movements: Arm-CODA

Subjects :  $\times 16$

 Healthy subjects

Sensors :  $\times 34$

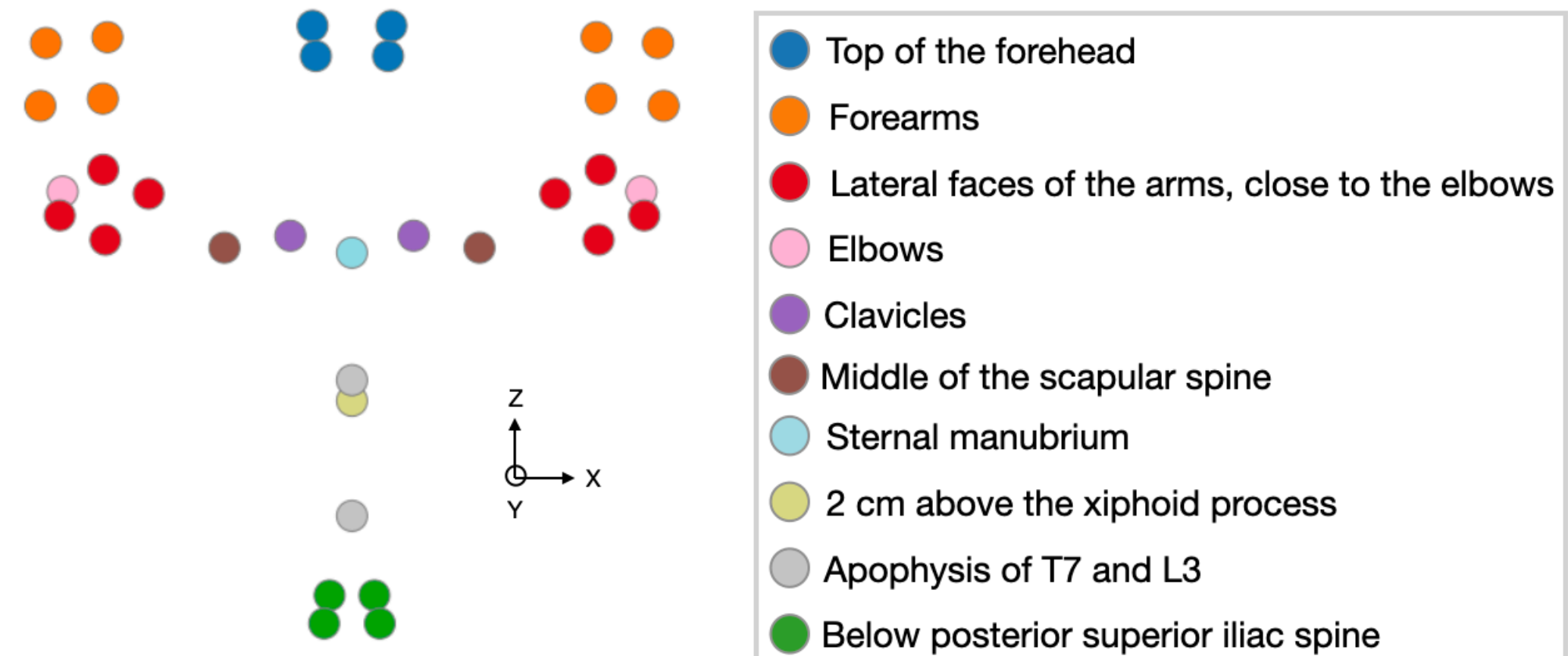
 Cartesian Optoelectronic Dynamic Anthropometer (CODA)

 3D positions data in millimeters at 100 Hz

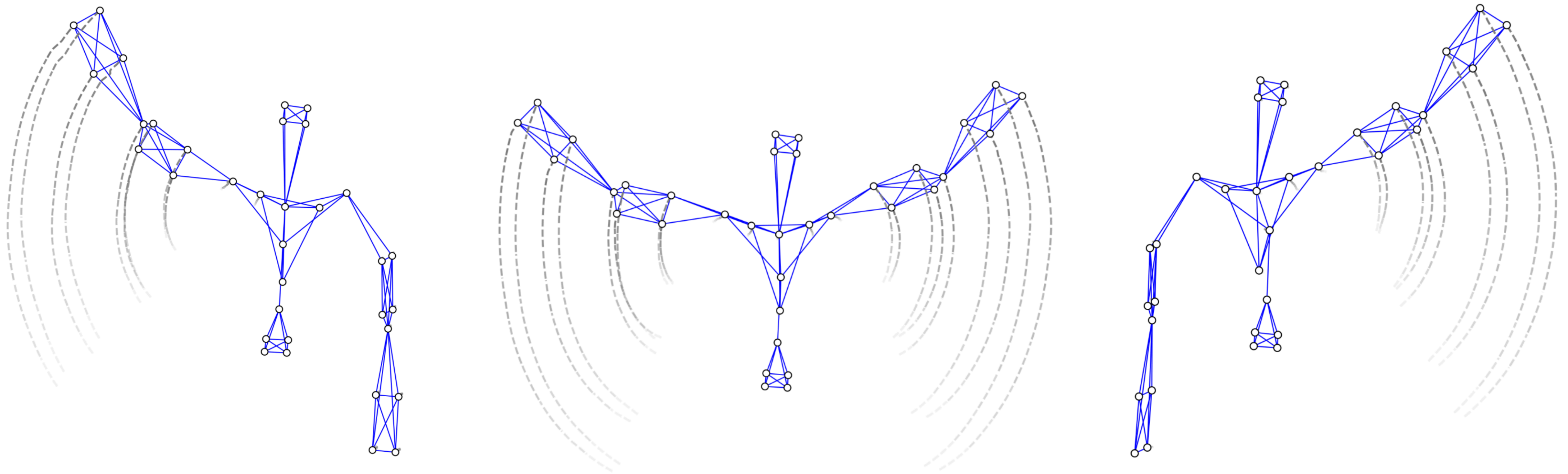
 System of 6 depth Cameras



View in the Sagittal plane



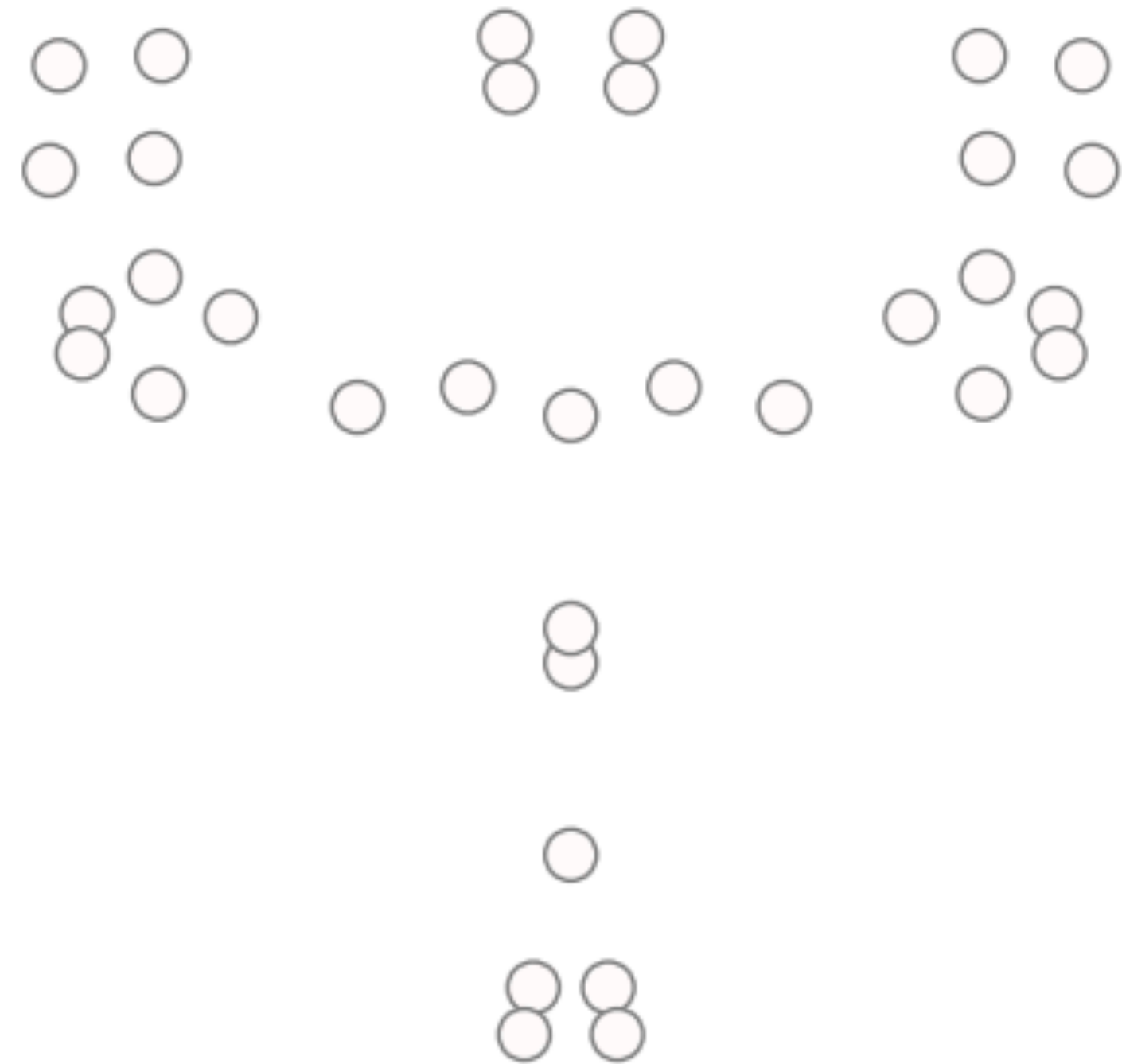
Elevation movements in the scapular plane: right arm, left arm and bilateral elevation



Graph

Graph signal

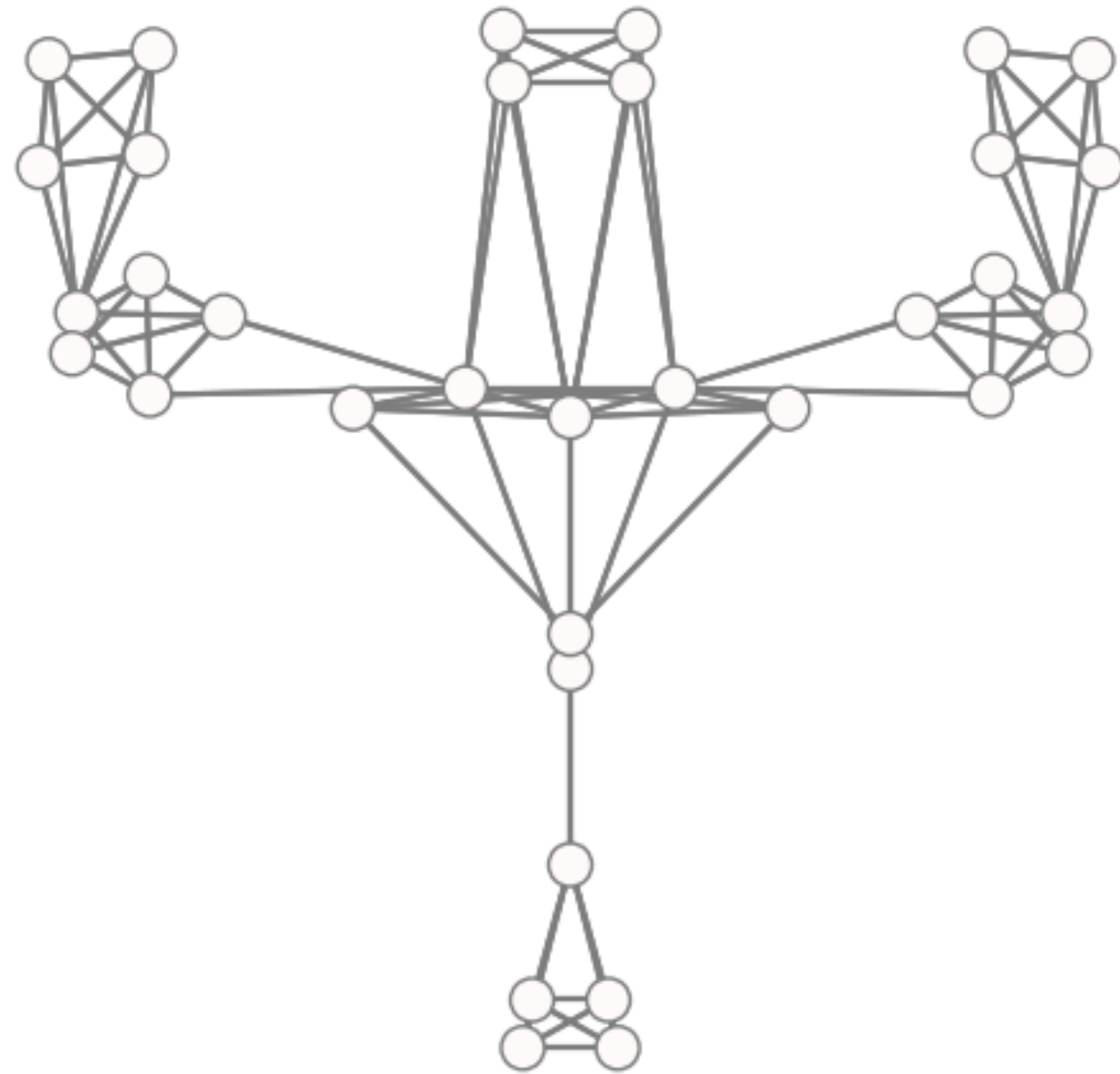
Nodes



Graph

Graph signal

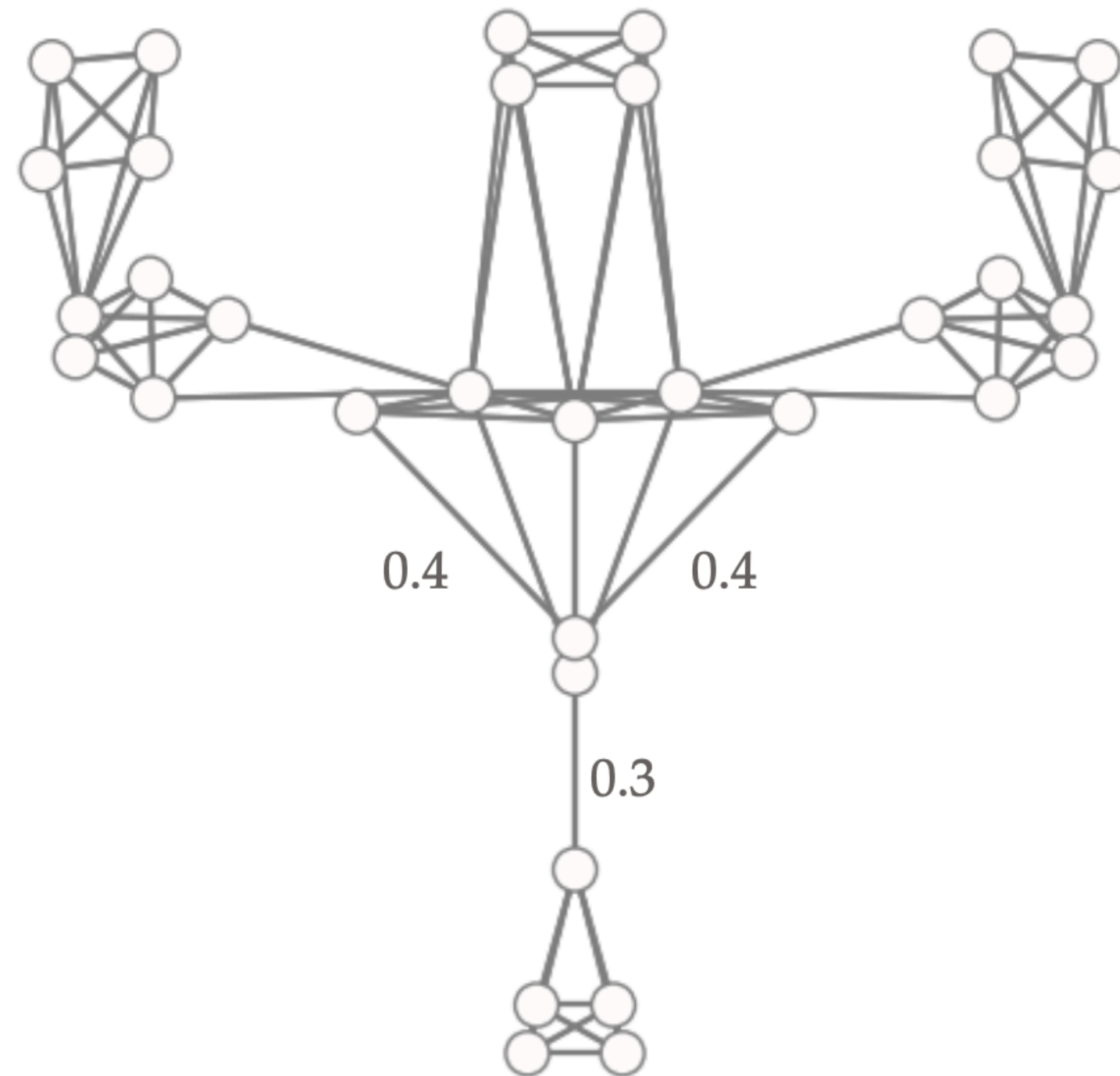
Nodes
+
Edges



Graph

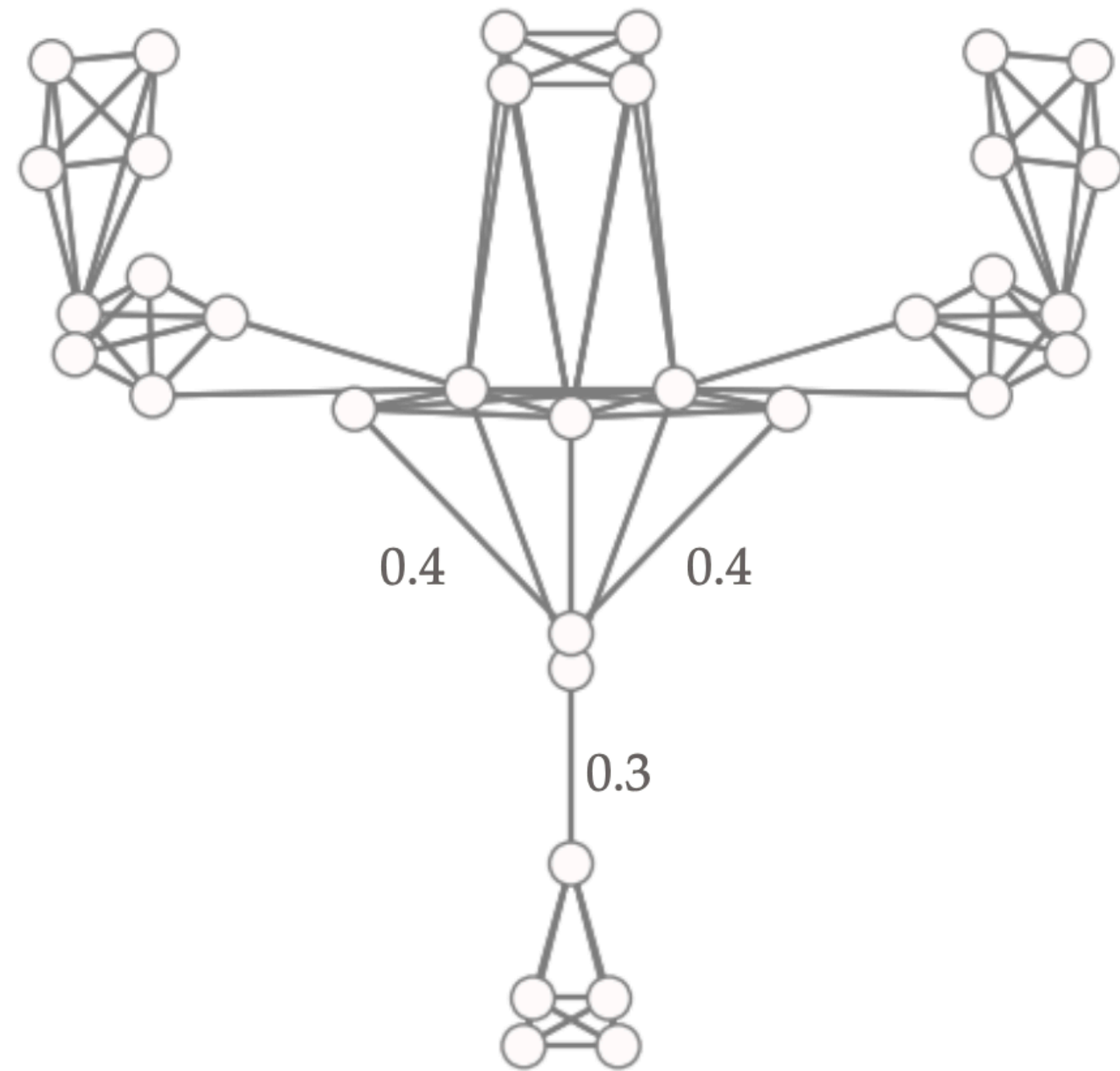
Graph signal

Nodes
+
Edges
+
Weights



Graph

Nodes
+
Edges
+
Weights

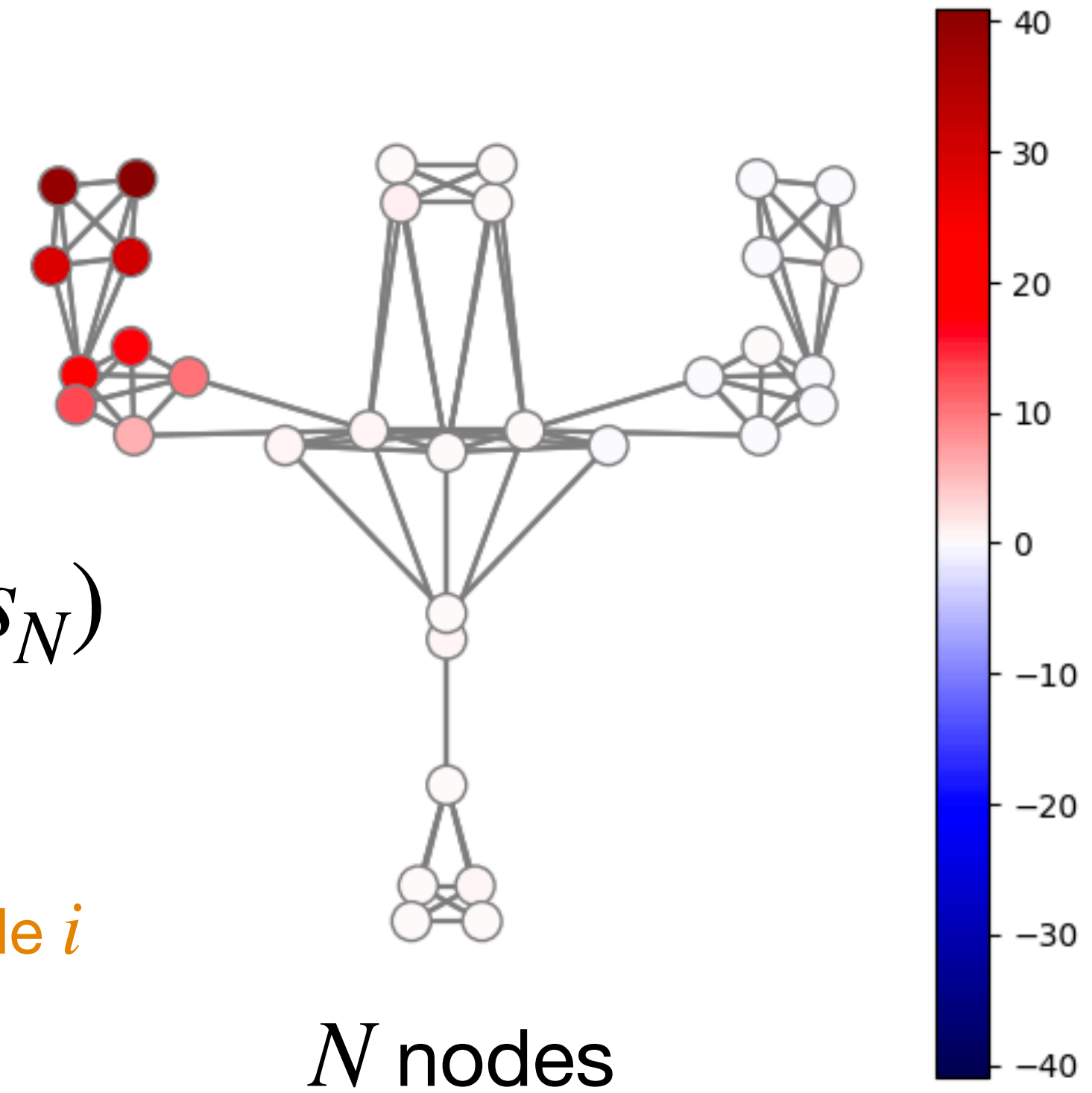


Graph signal

A value is associated to each node

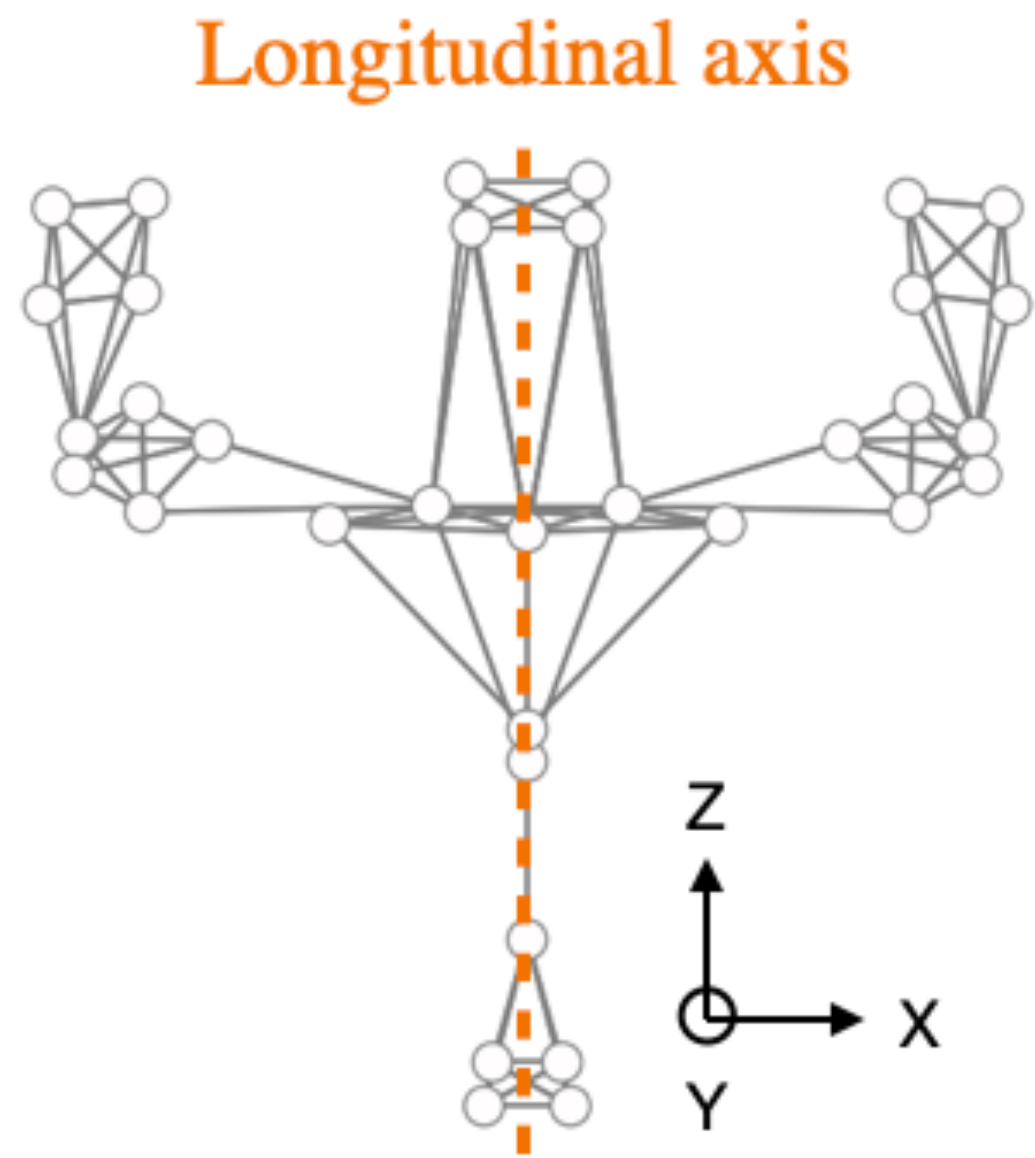
$$\mathbf{s} = (s_1, \dots, s_i, \dots, s_N)$$

Value associated to node i



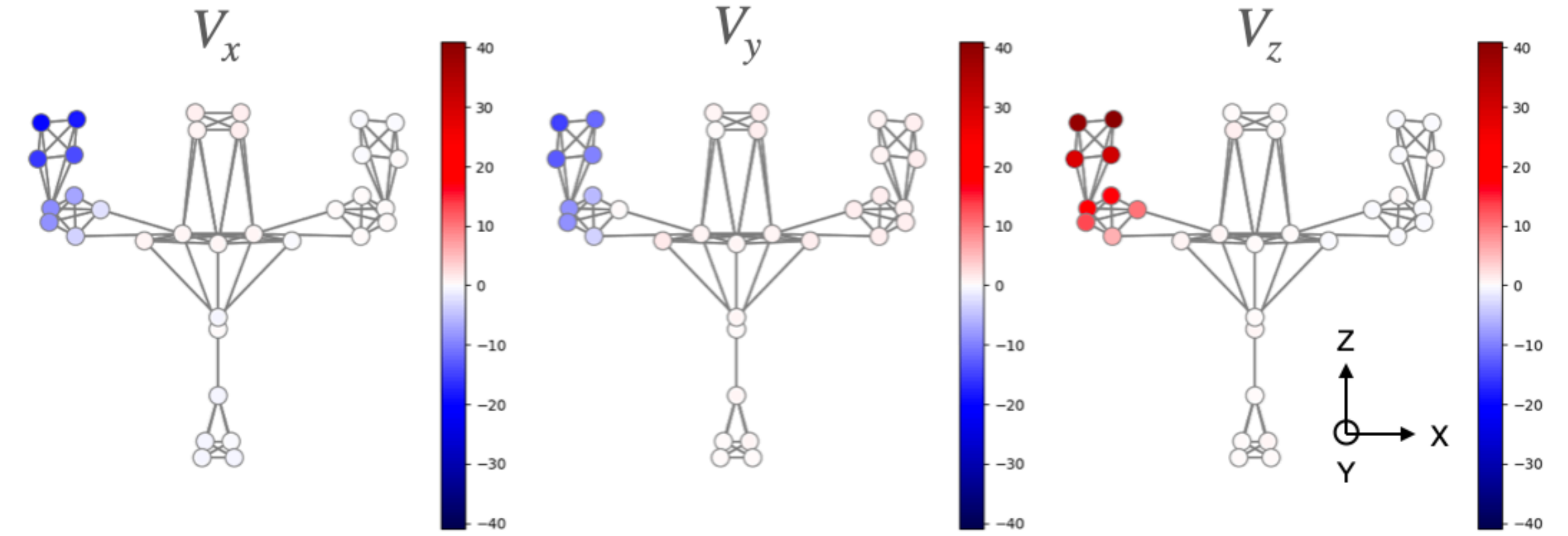
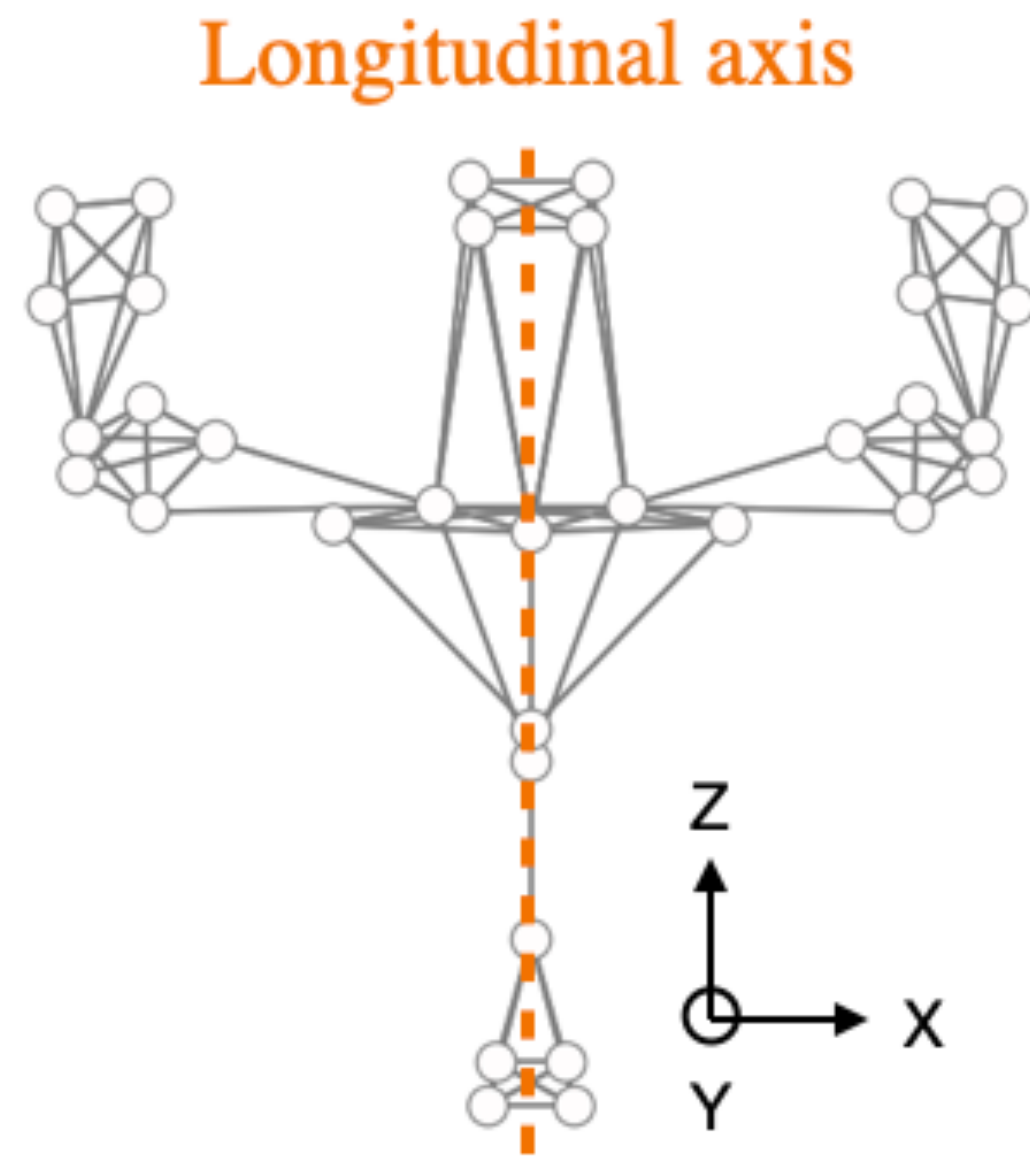
Graph construction

Close nodes
↓
Close sensors
along the body

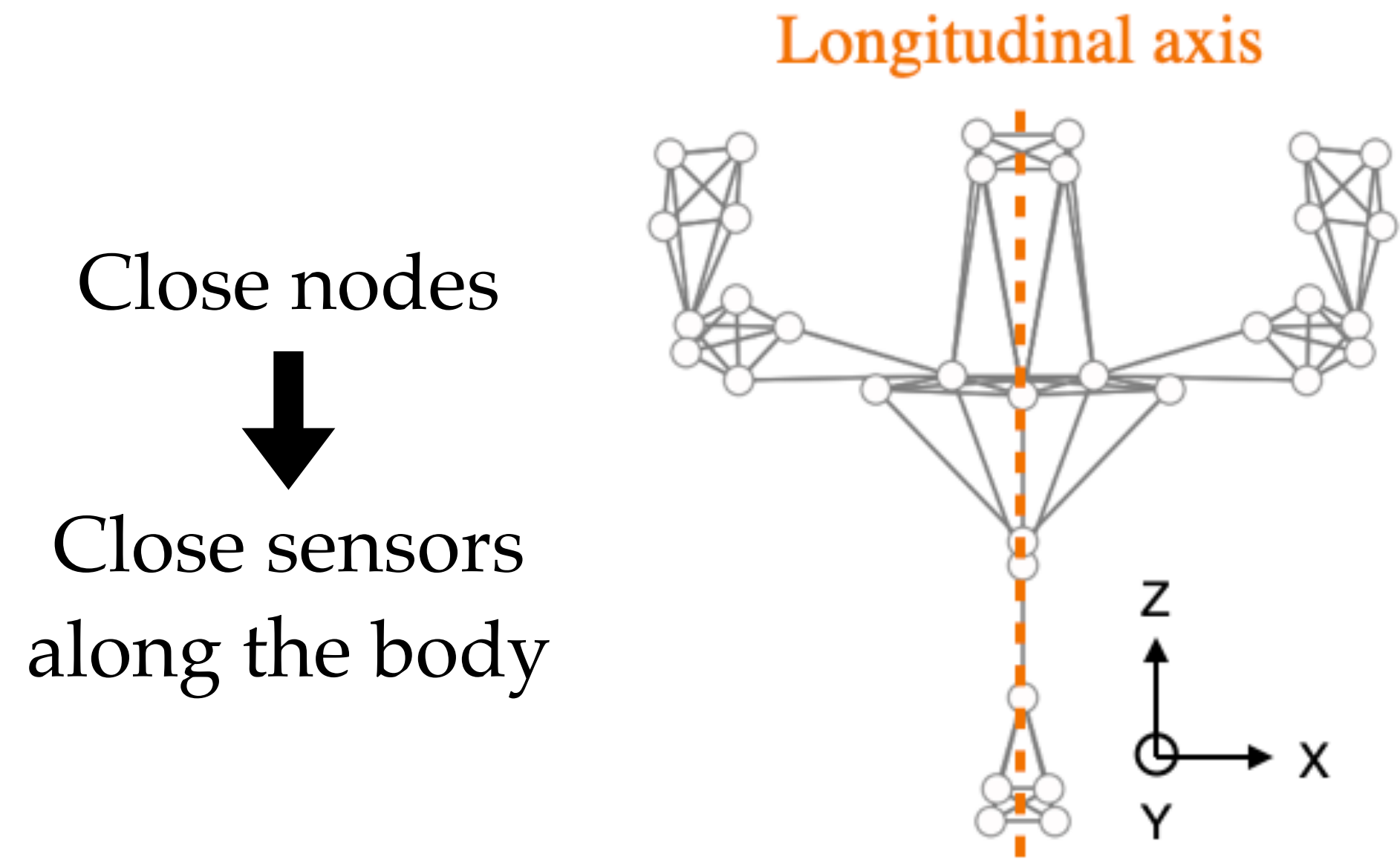


Graph construction

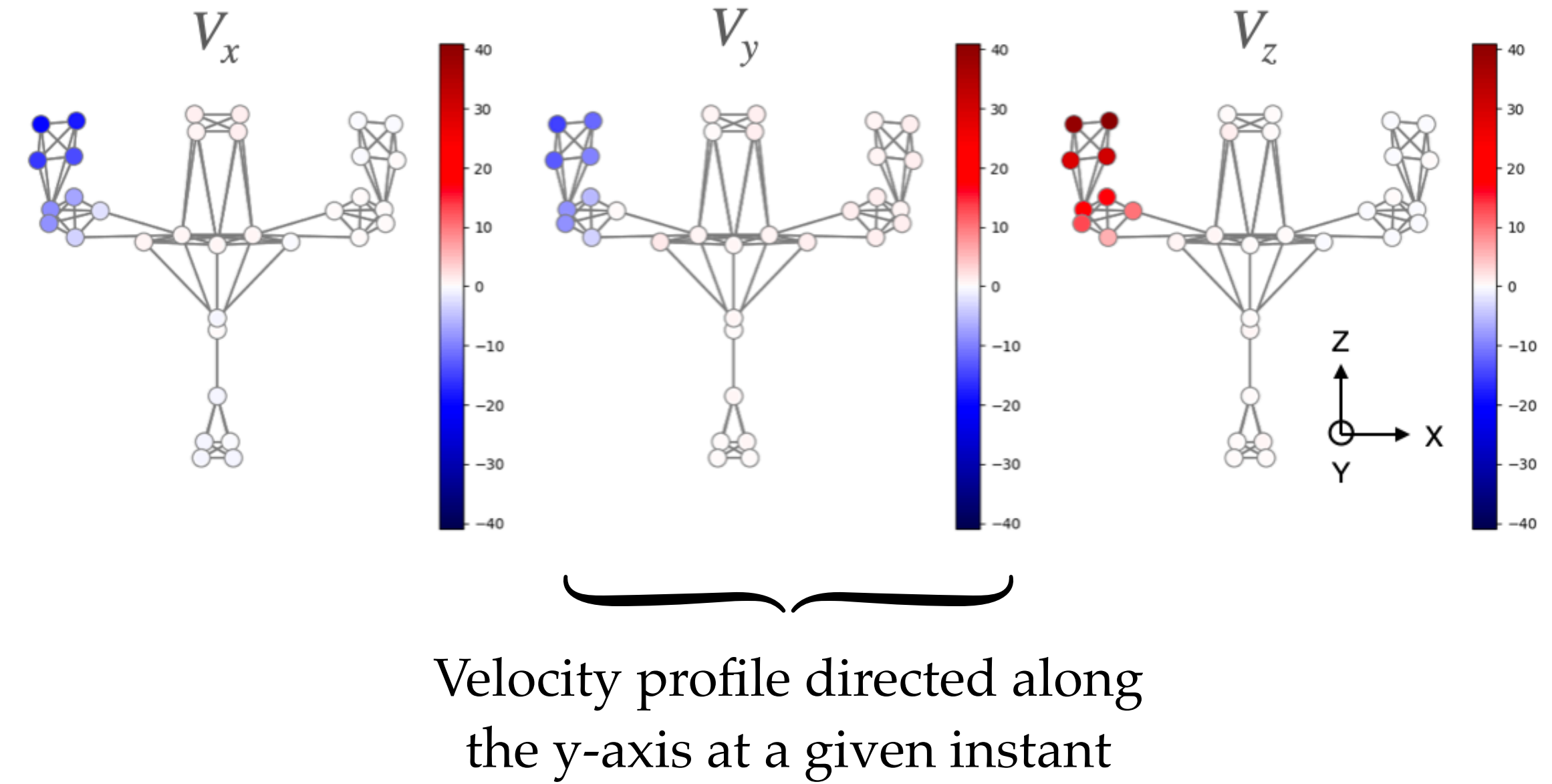
Close nodes
↓
Close sensors
along the body



Graph construction



Velocity profiles



Dictionary learning

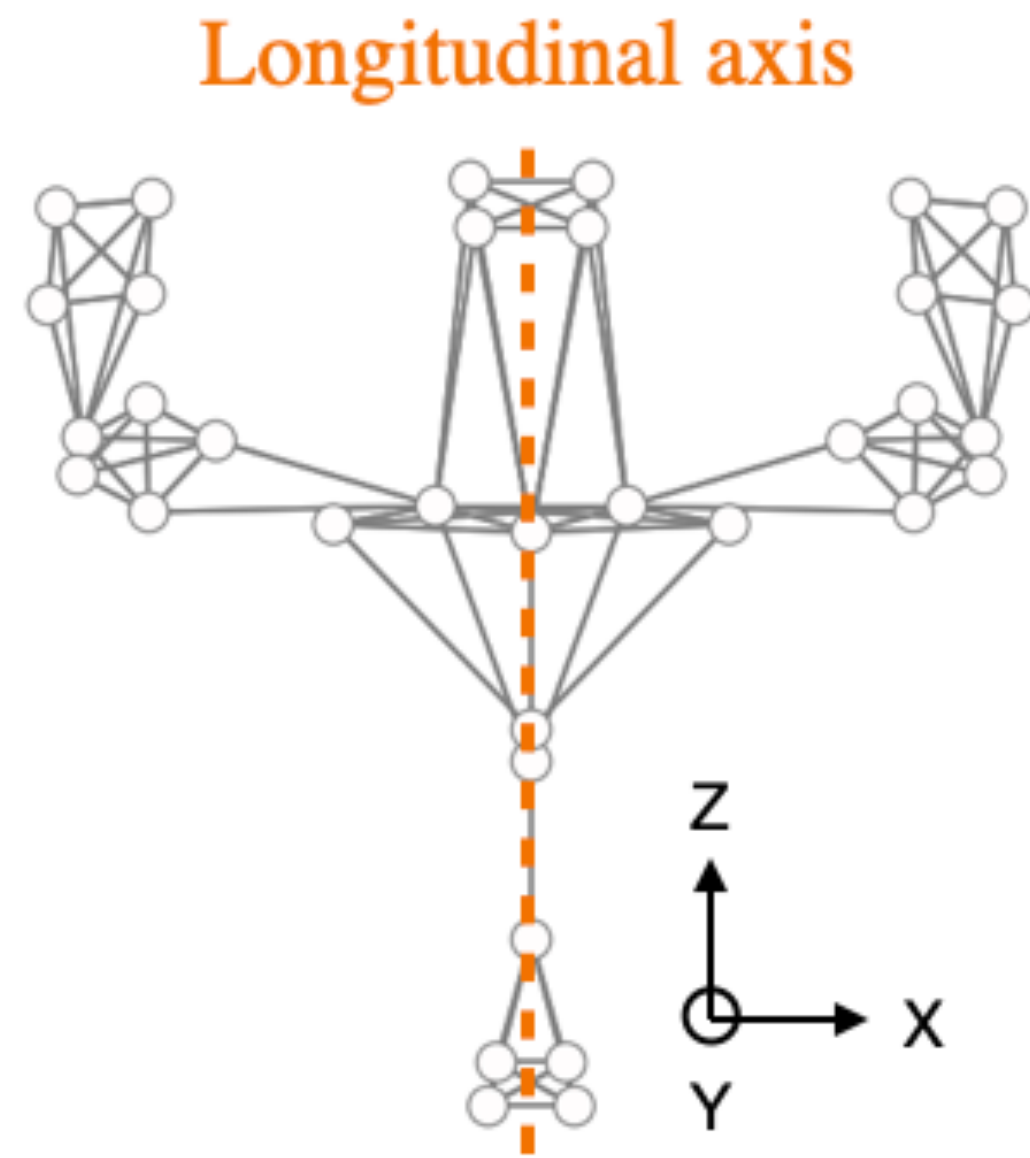
$$\mathbf{y} \approx \sum_{l=1}^L x_l \mathbf{d}^l$$

Signal Activations Atoms

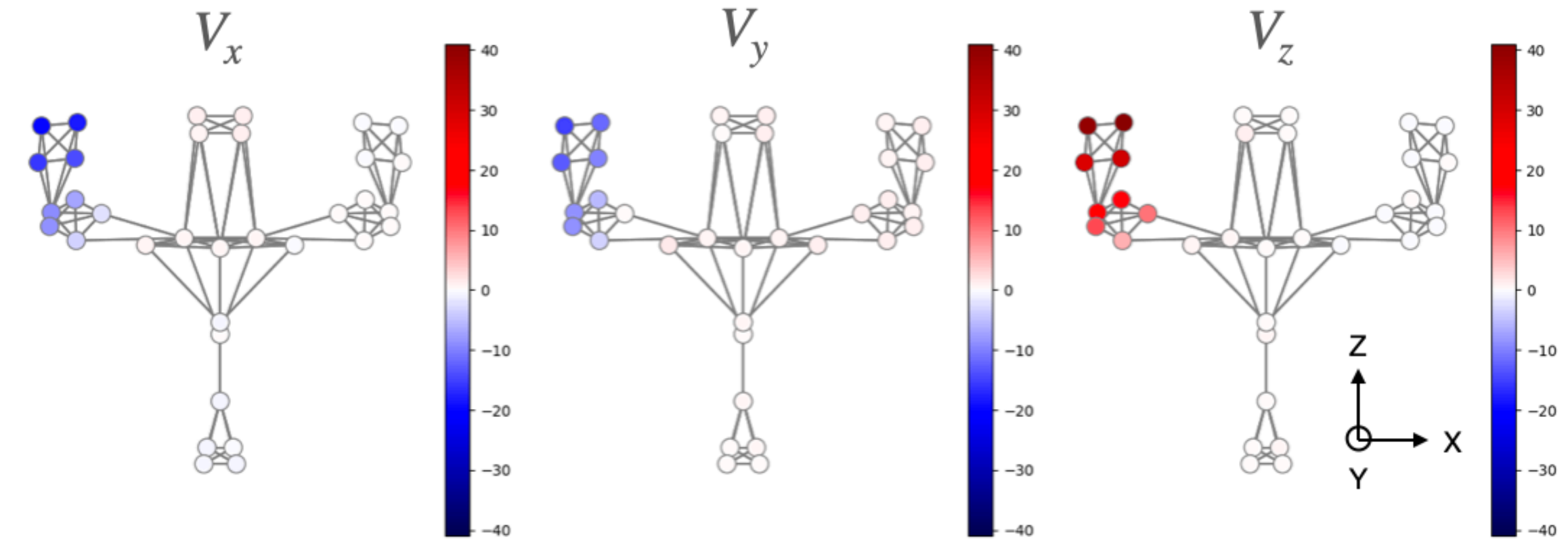
argmin X, D $\|Y - DX\|_F^2$
 s.t. $\|x_i\|_0 \leq T \quad \forall i$

Graph construction

Close nodes
↓
Close sensors
along the body



Velocity profiles



Double sparsity

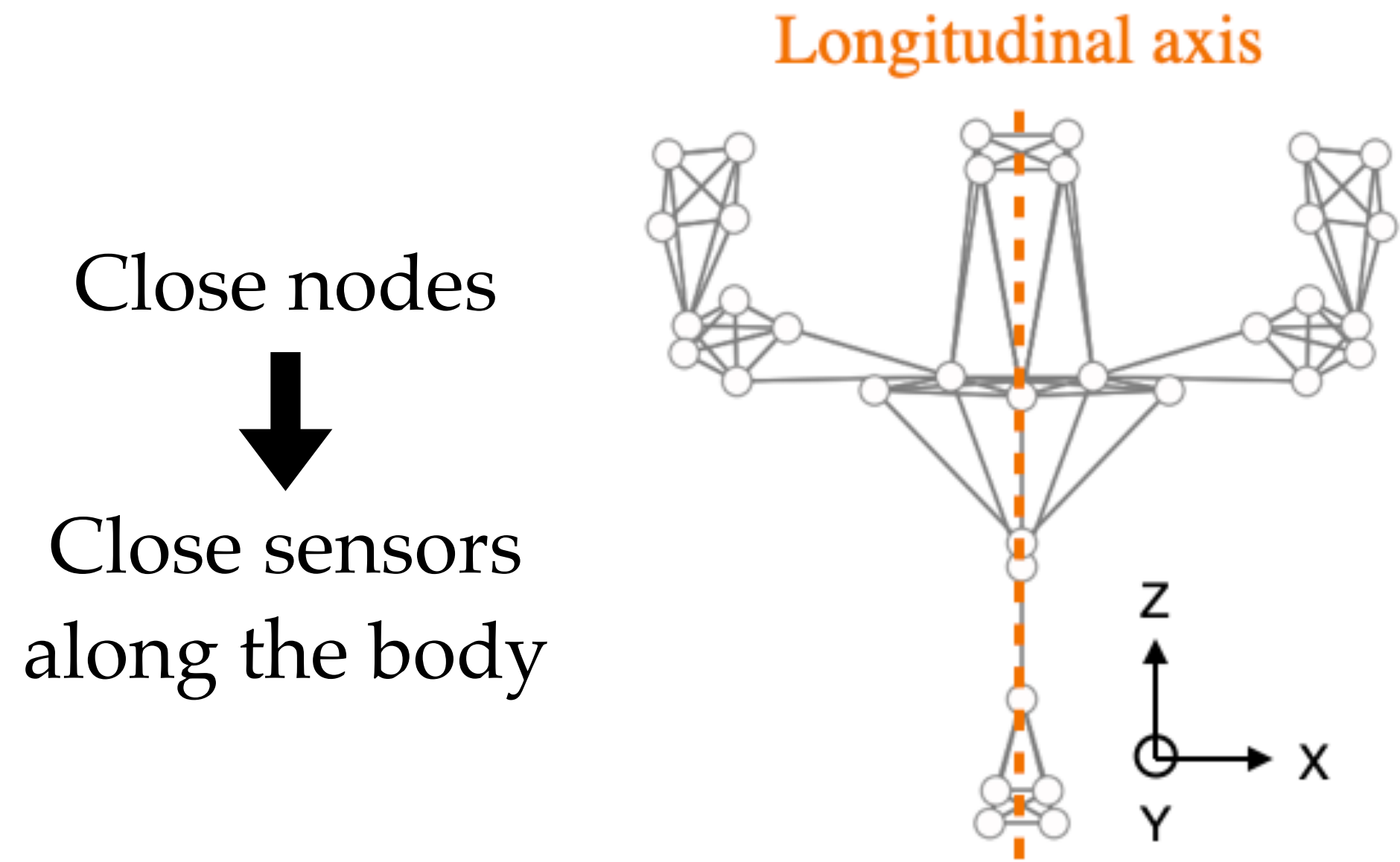
$$\mathbf{y} \approx \sum_{l=1}^L x_l \mathbf{d}^l$$

Signal Activations ~~Atoms~~
Super-atoms

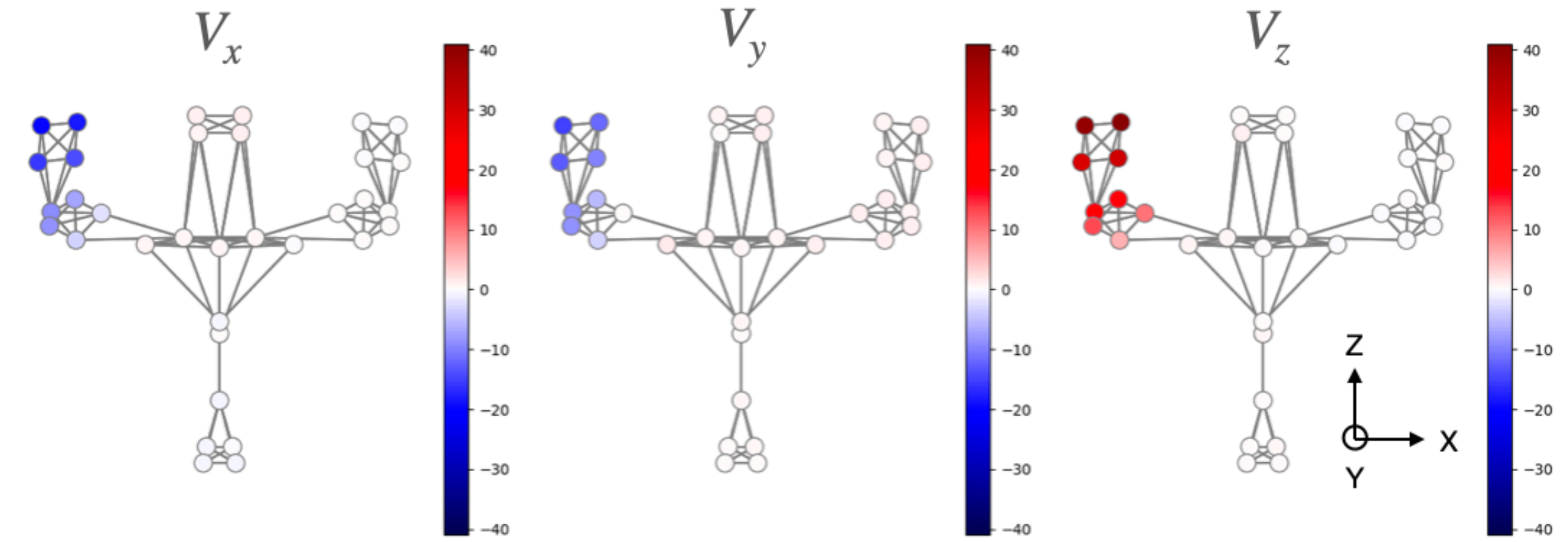
$$\mathbf{d}^l \approx \sum_{k=1}^K a_k \phi^k$$

Super-atom Atom

Graph construction



Velocity profiles



Velocity profile directed along the y-axis at a given instant

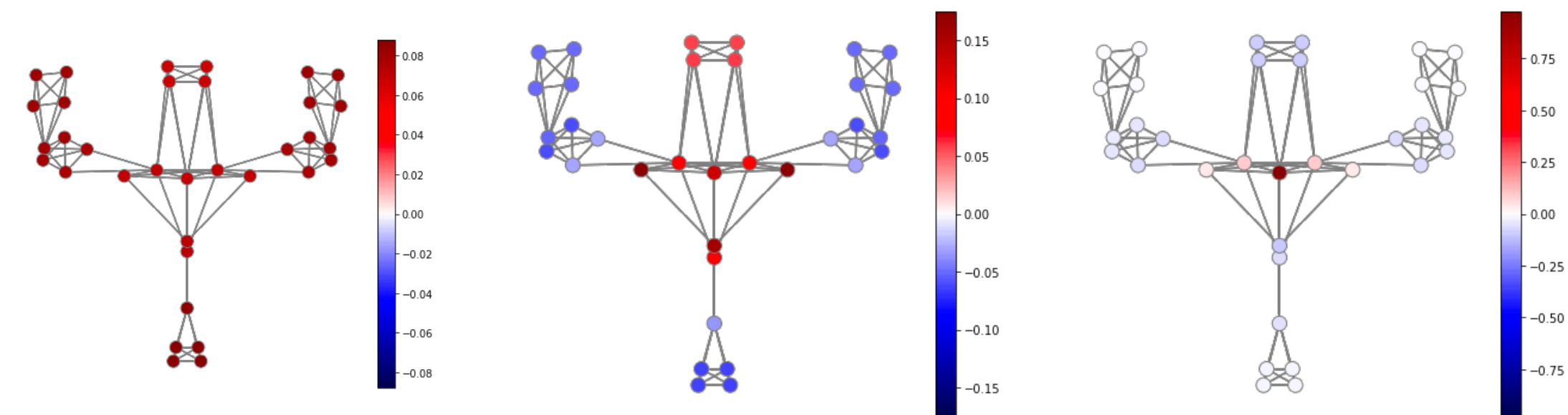
Double sparsity

$$y \approx \sum_{l=1}^L x_l \mathbf{d}^l$$

Signal Activations ~~Atoms~~
 Super-atoms

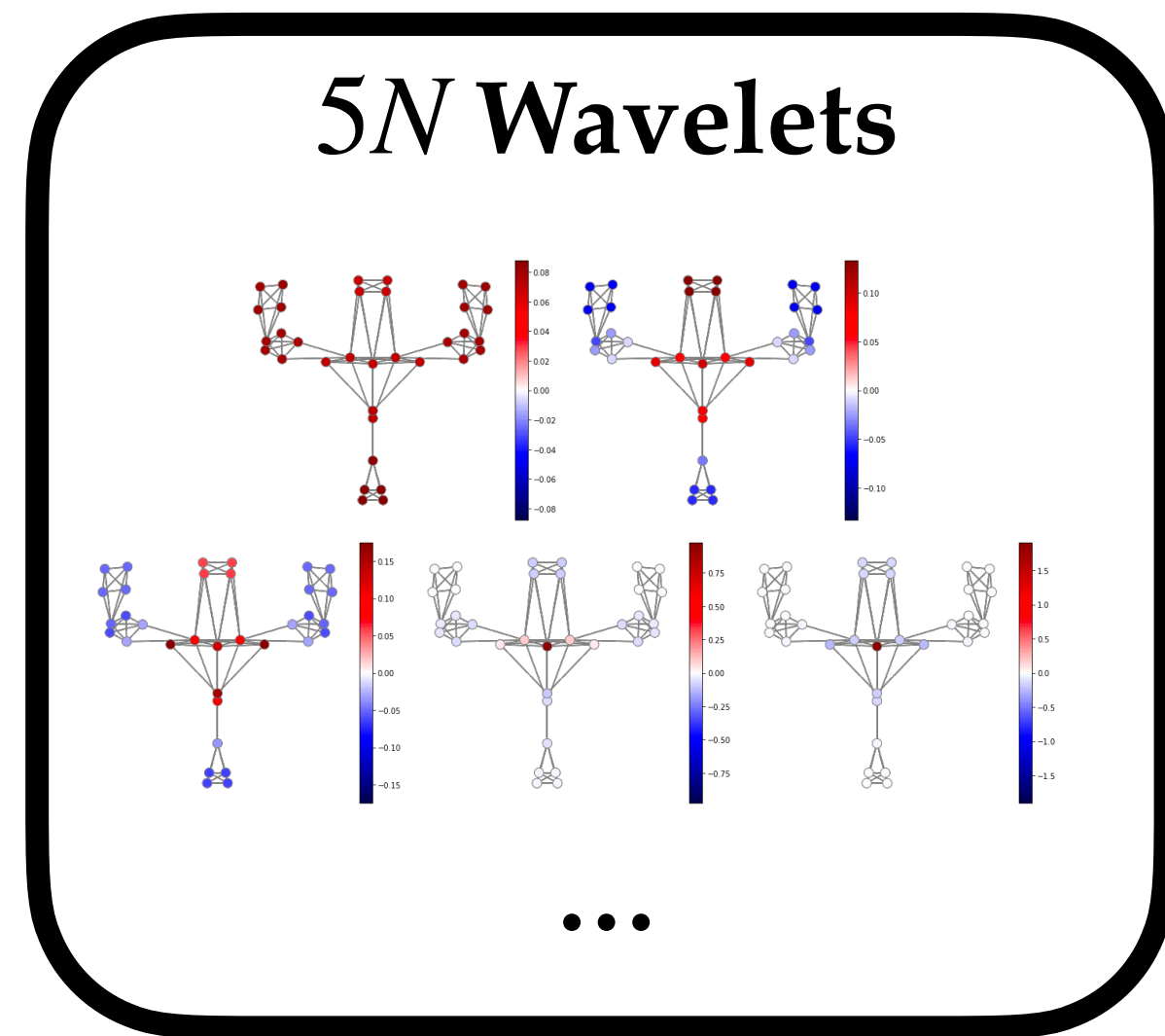
$$\mathbf{d}^l \approx \sum_{k=1}^K a_k \phi^k$$

Super-atom Atom



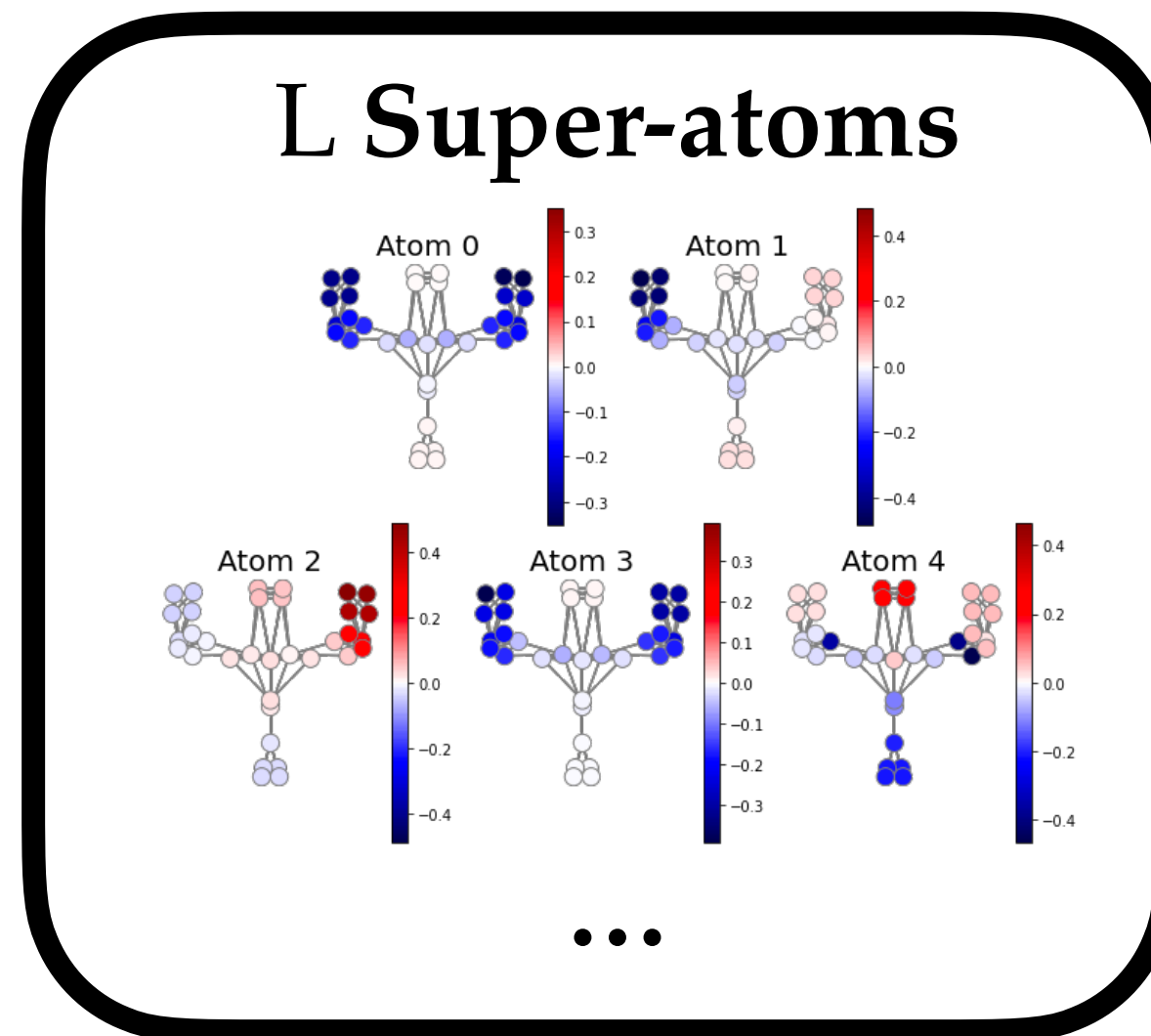
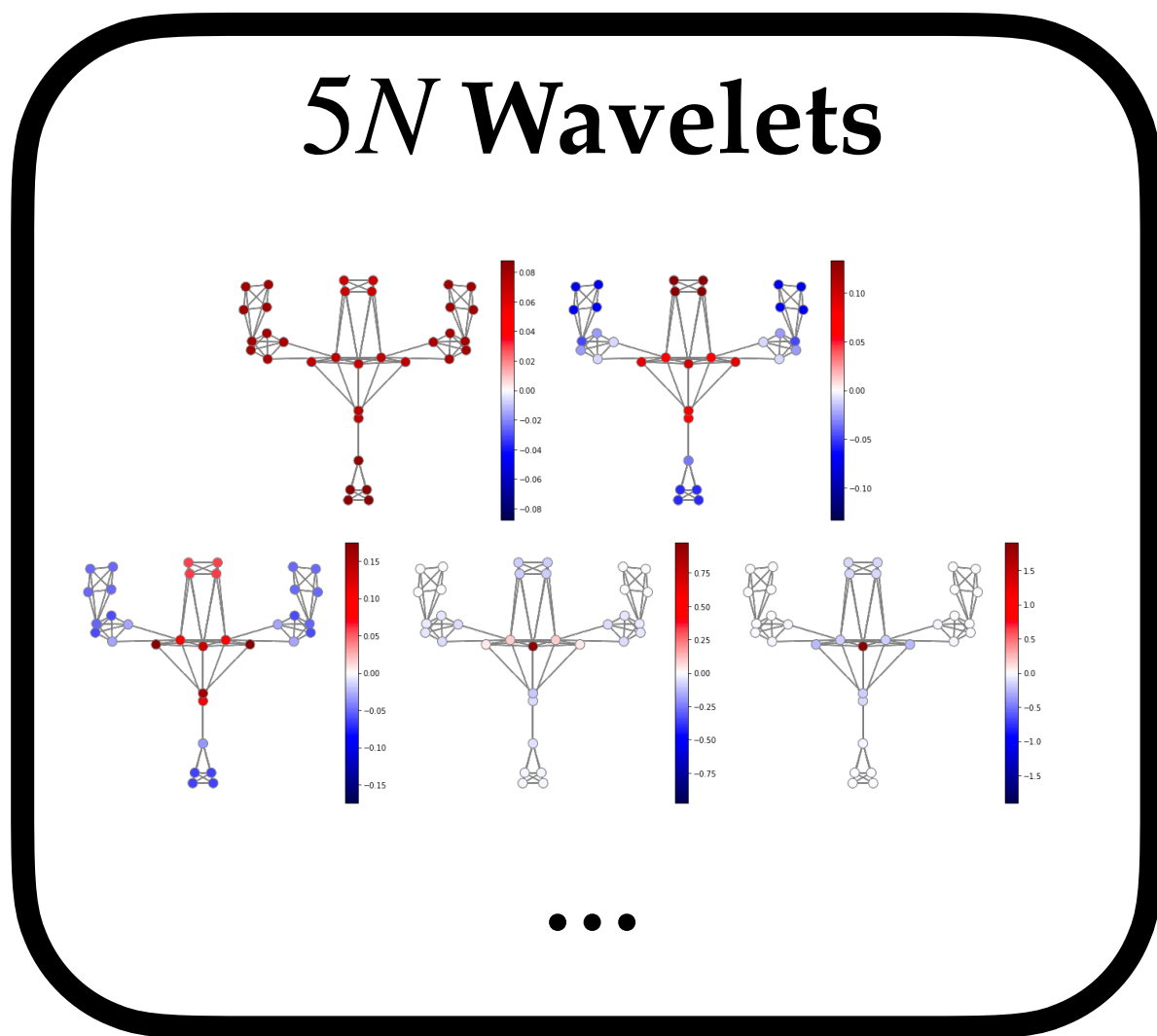
Each wavelet is characterized by a scale and a node on which it is centered

DSMH Method



DSMH Method

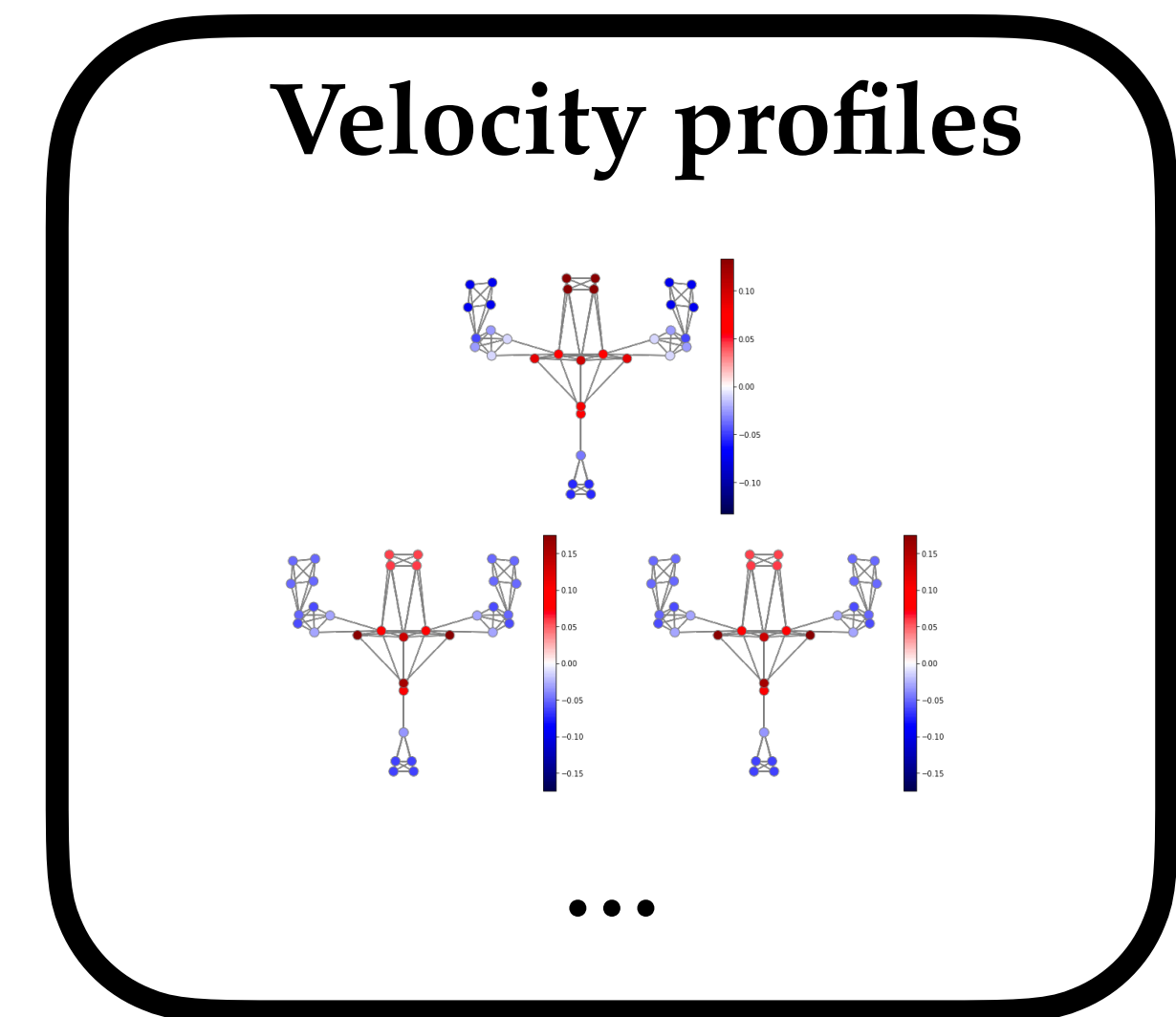
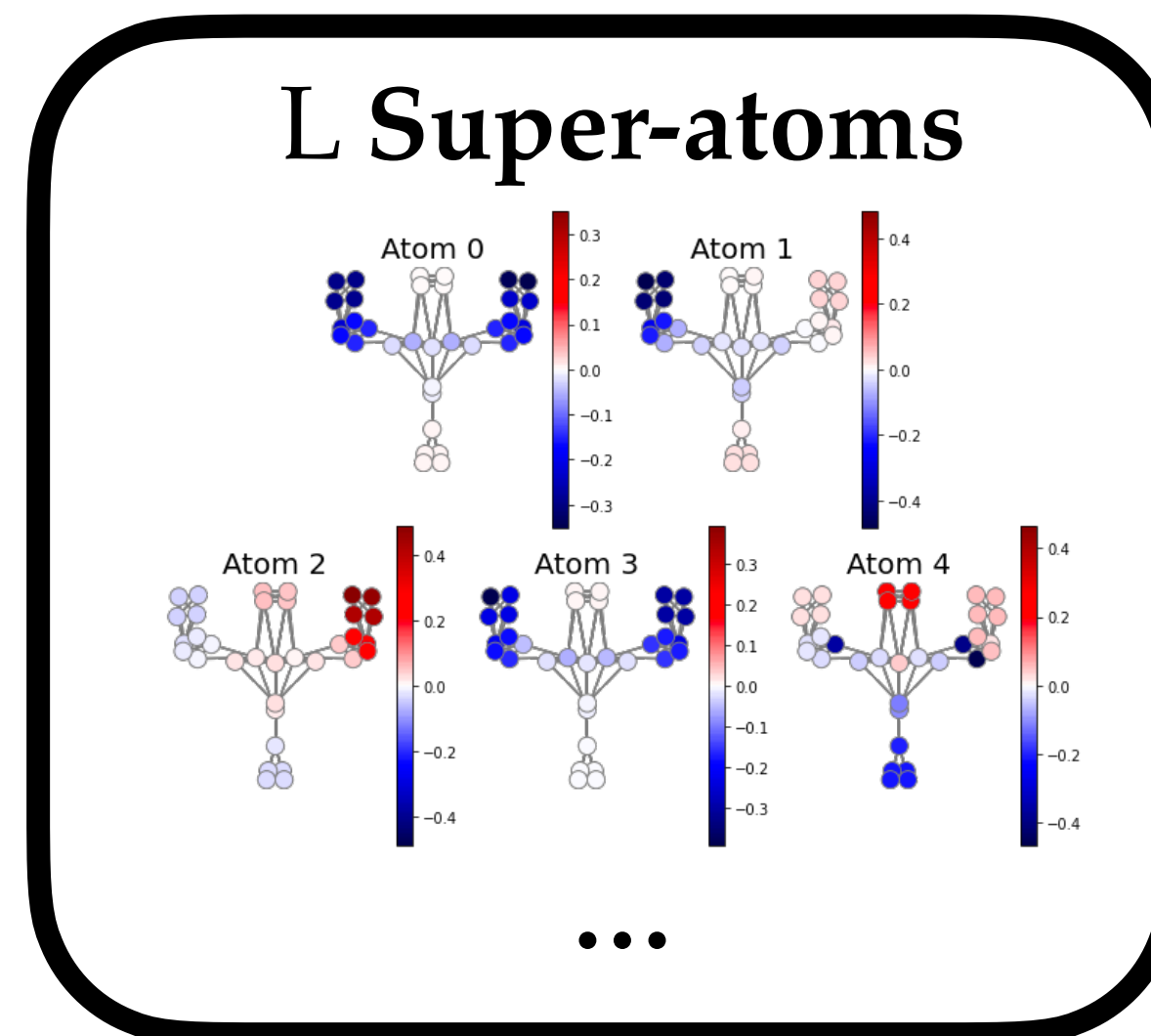
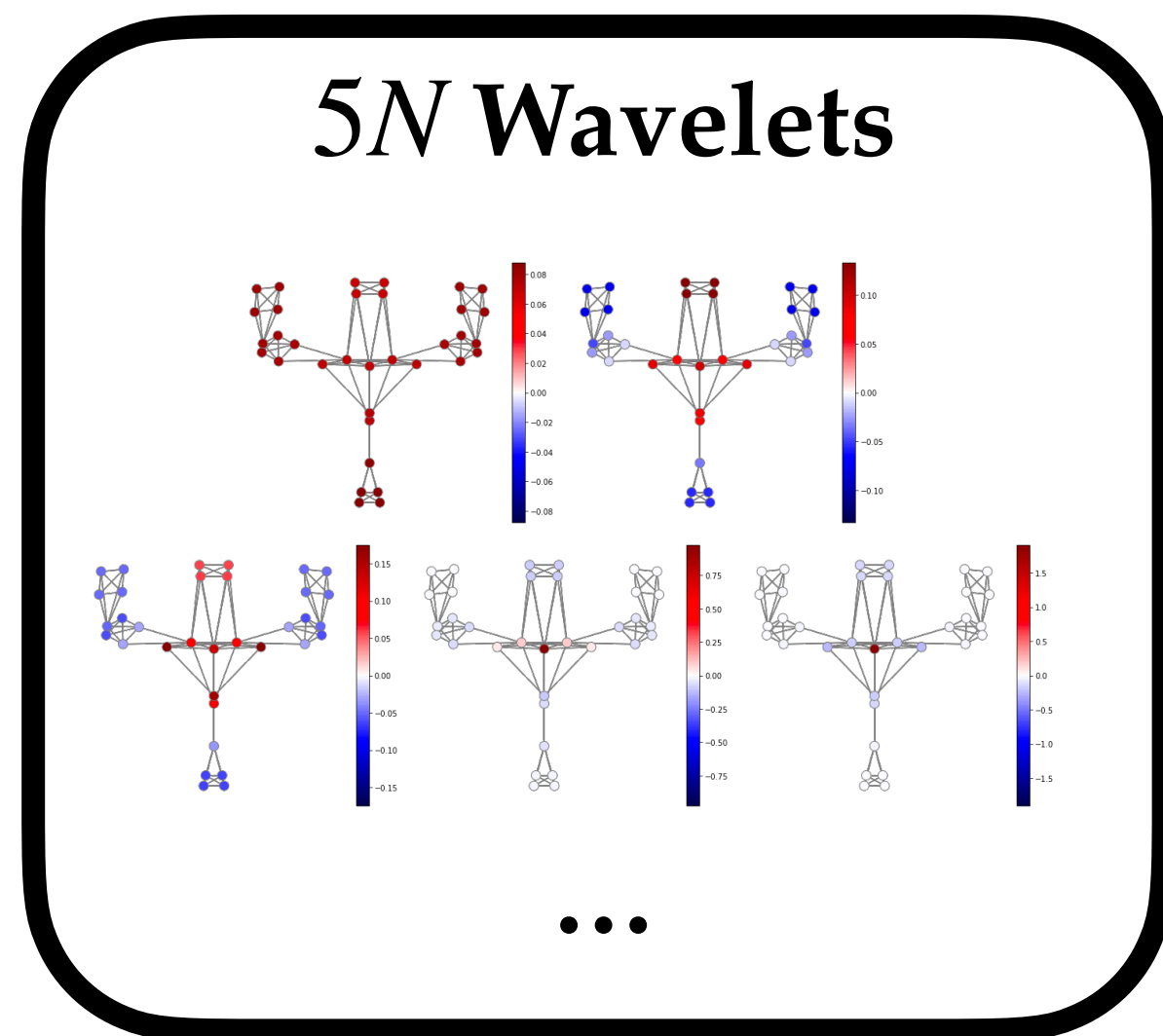
Construction of $L = 10$
super-atoms by combining
at most $P = 5$ wavelets



DSMH Method

Construction of $L = 10$
super-atoms by combining
at most $P = 5$ wavelets

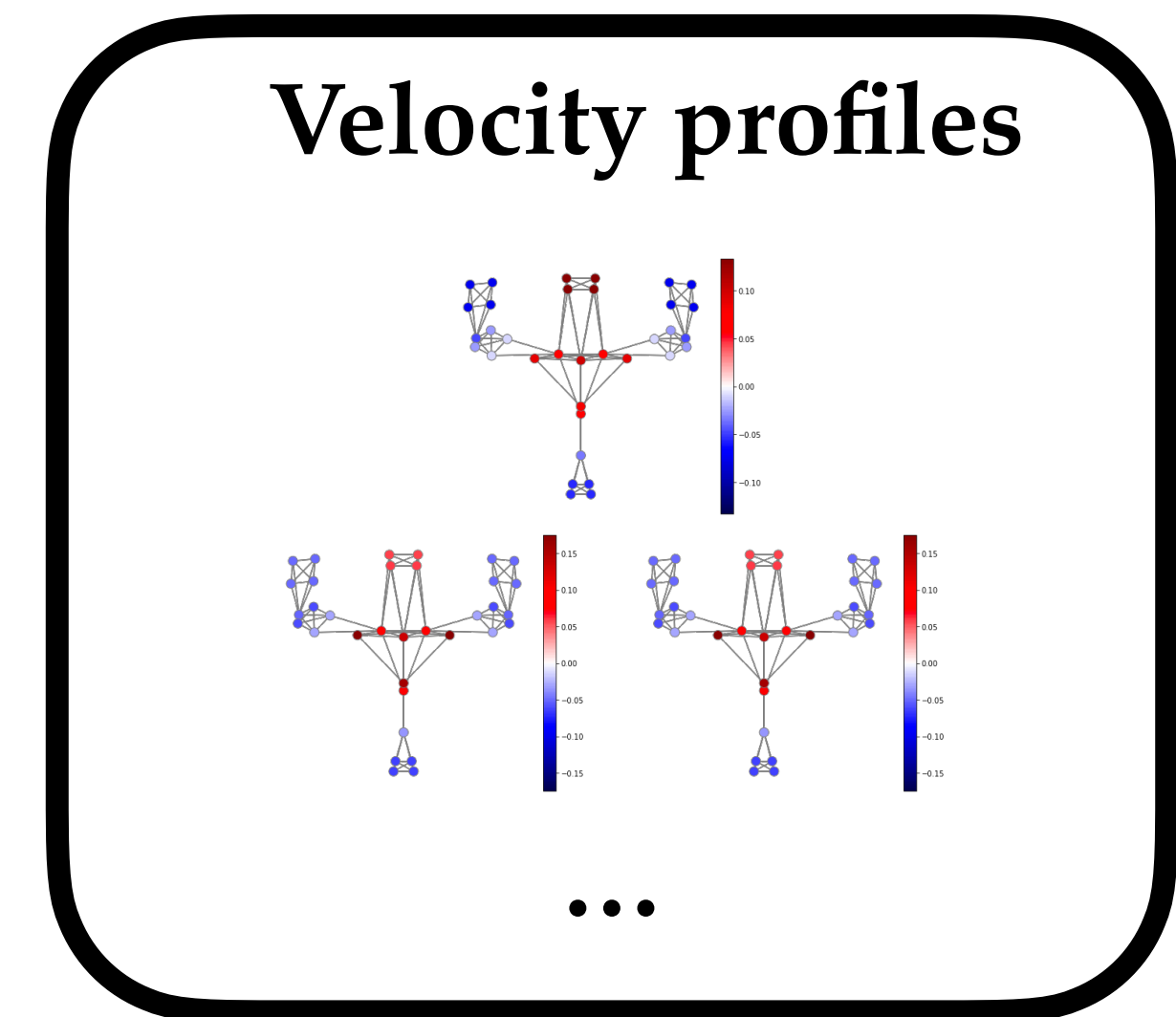
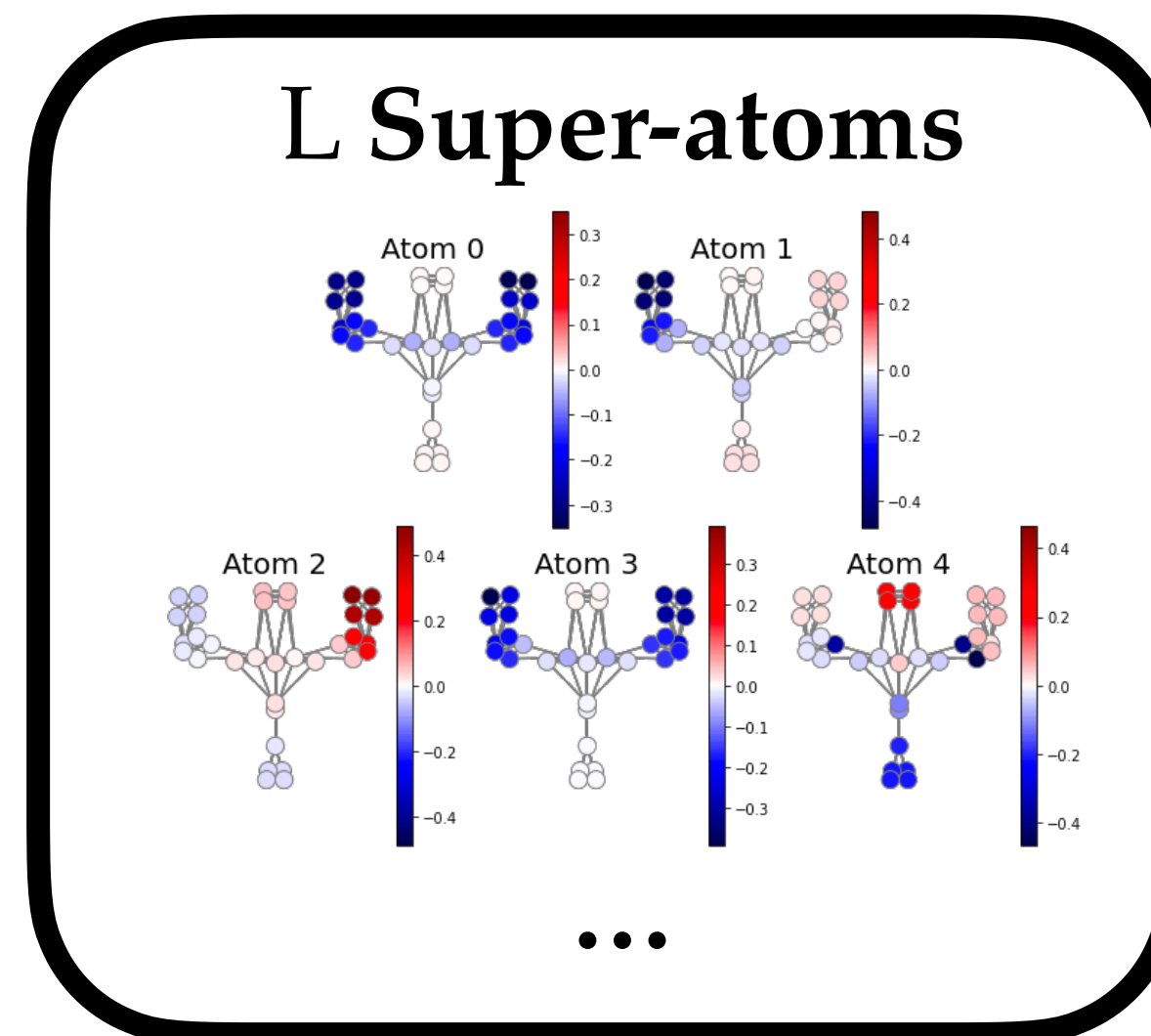
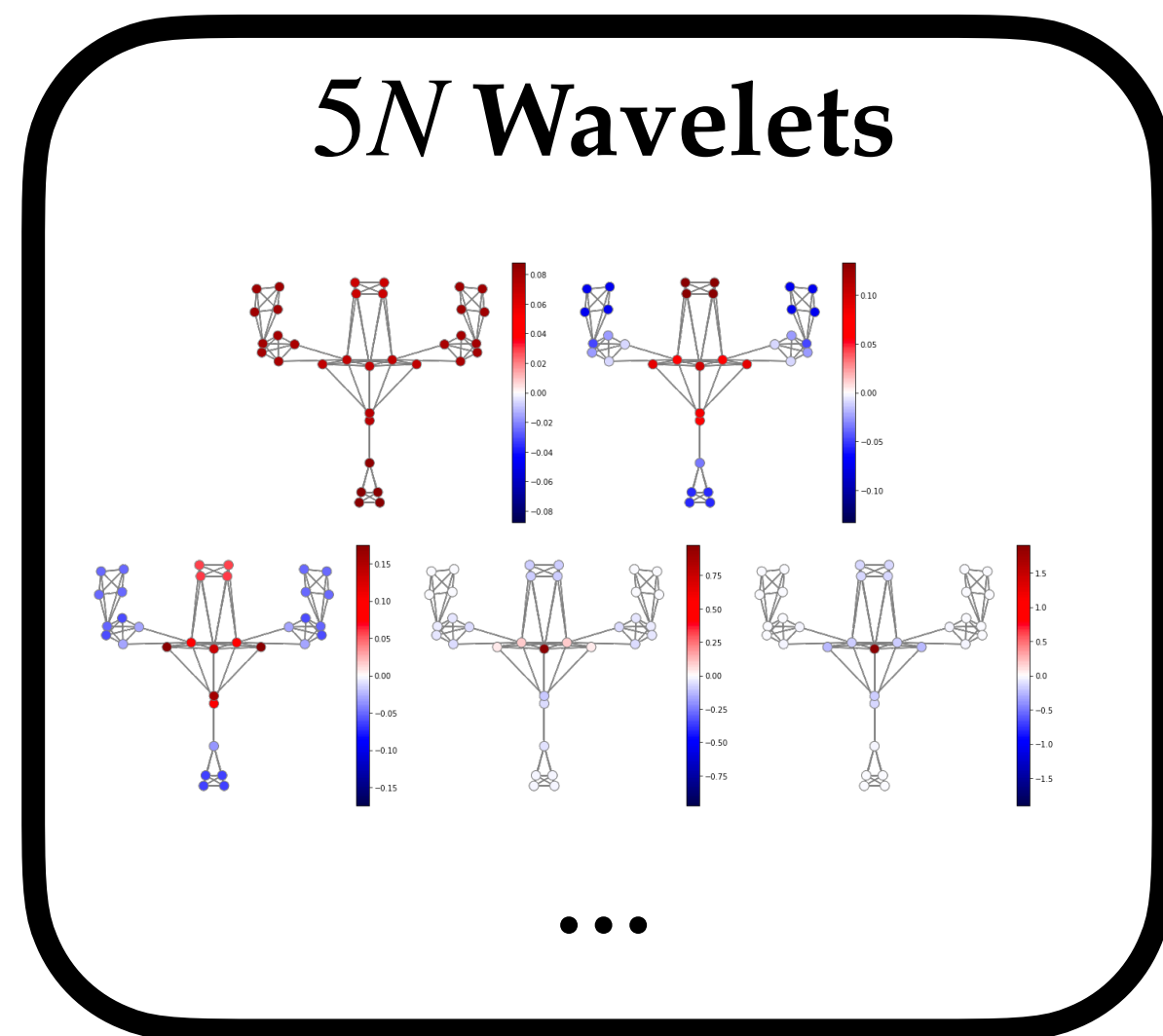
Use of at most $T = 3$ super-atoms
to approximate each graph signal



DSMH Method

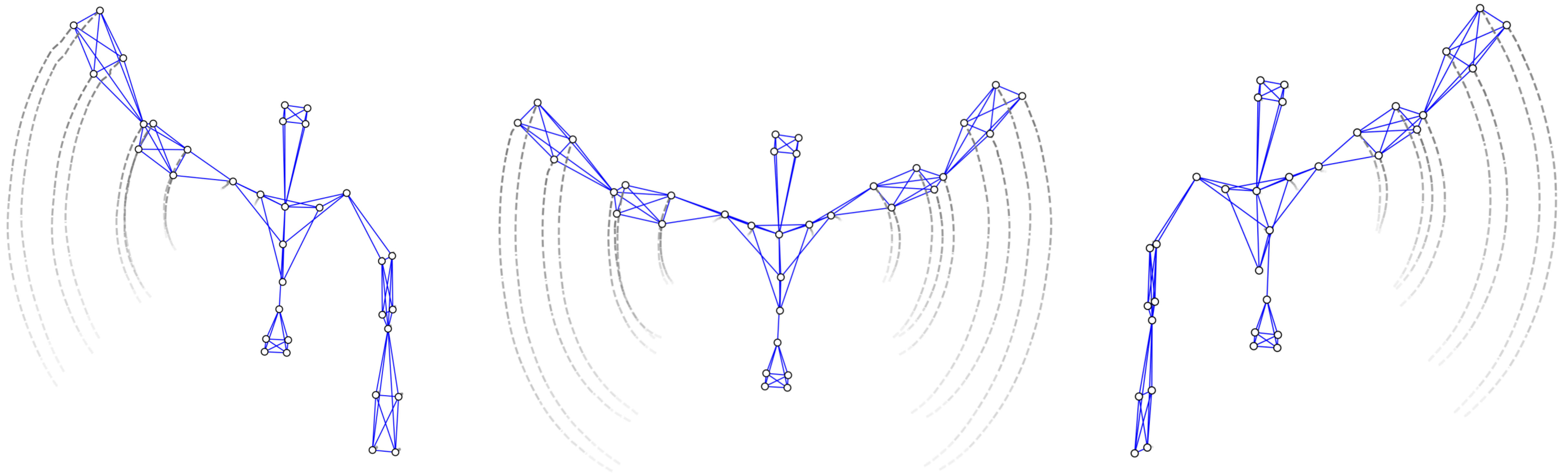
Construction of $L = 10$
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Use of at most $T = 3$ super-atoms
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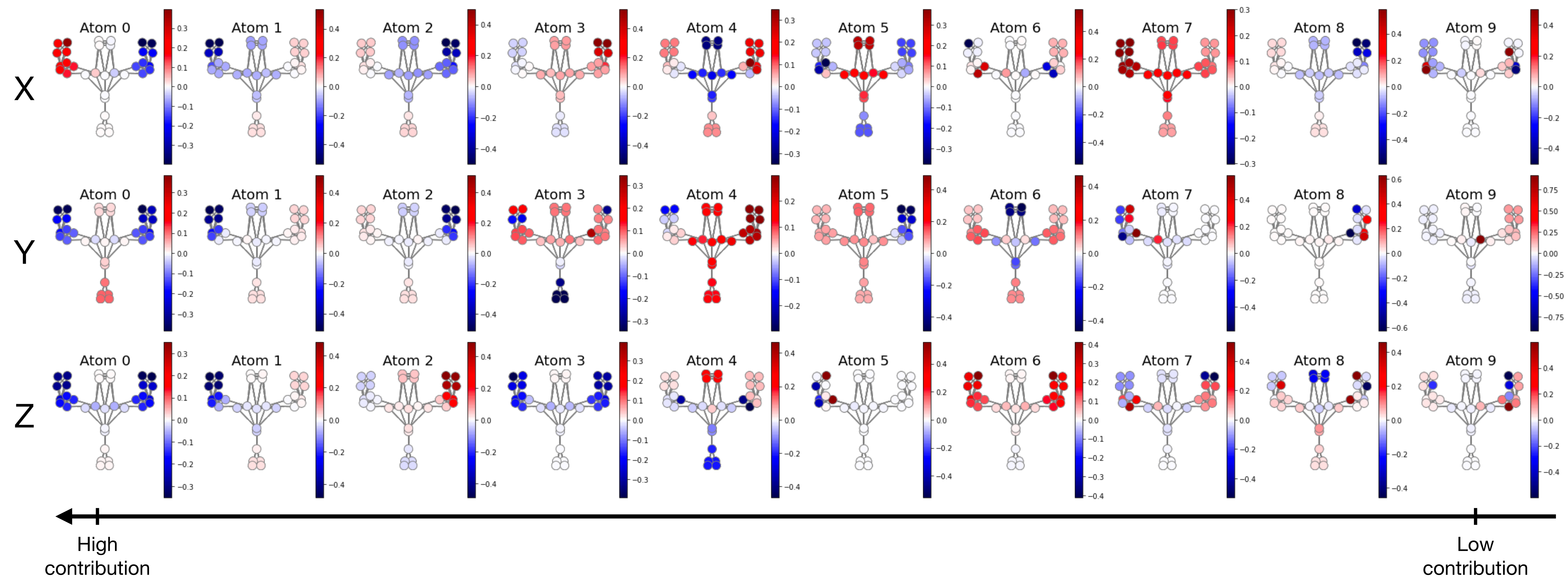


$L = 10$ $P = 5$ $T = 3$ \longrightarrow 80 % signal reconstruction

Elevation movements in the scapular plane: right arm, left arm and bilateral elevation

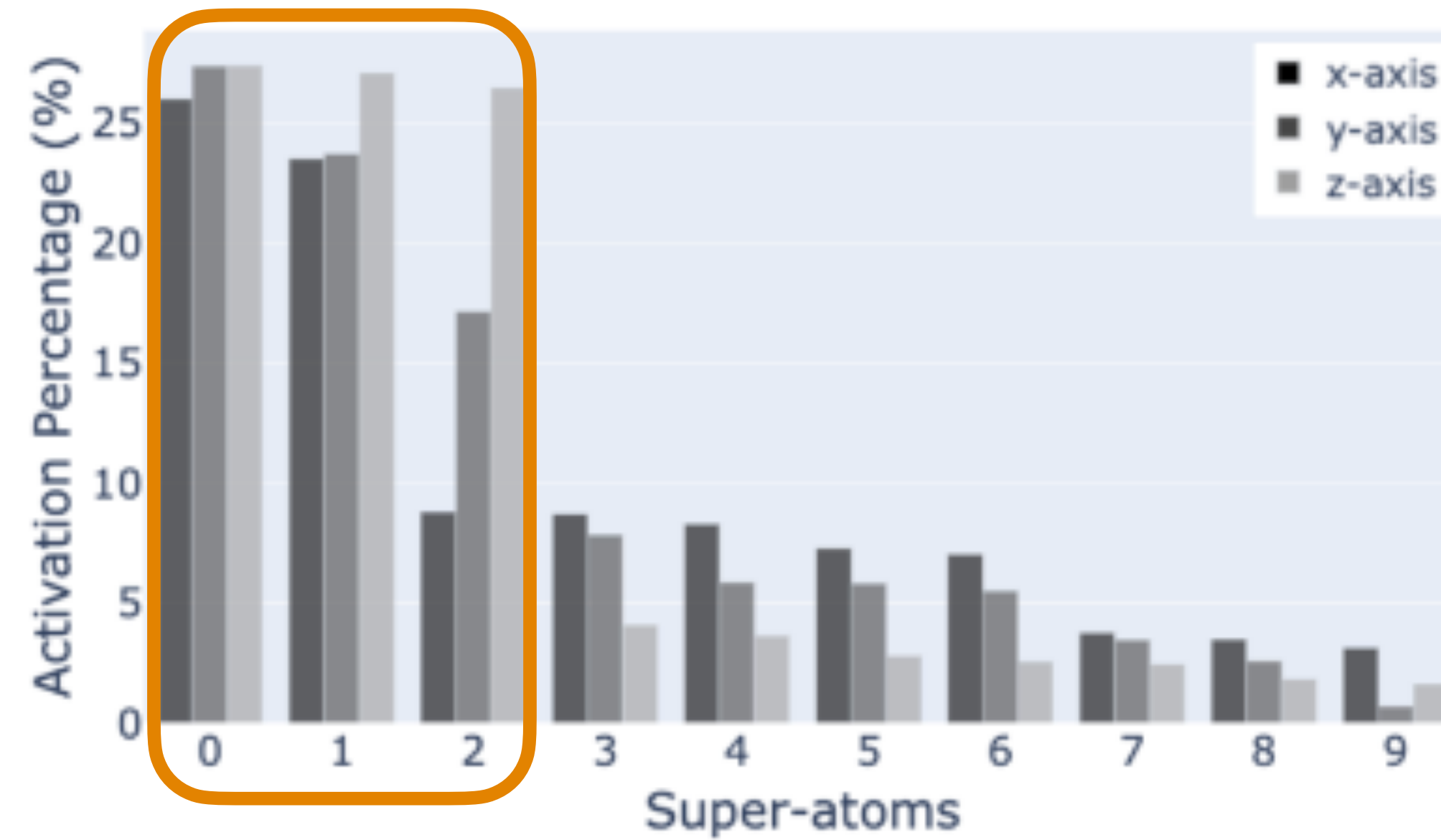
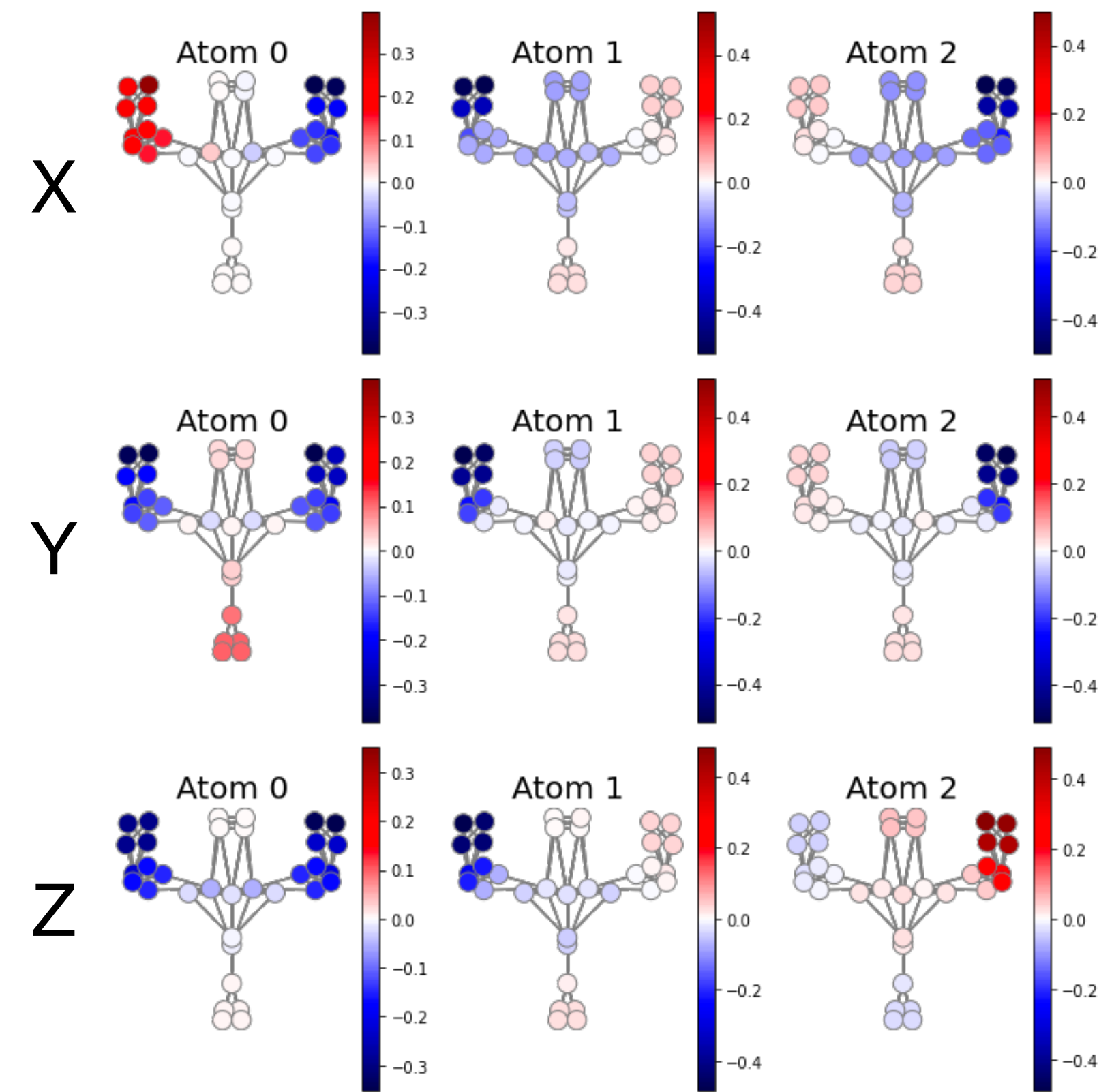


DSMH dictionary



DSMH dictionary

Elevation movements in the scapular plane : right arm, left arm and bilateral elevation



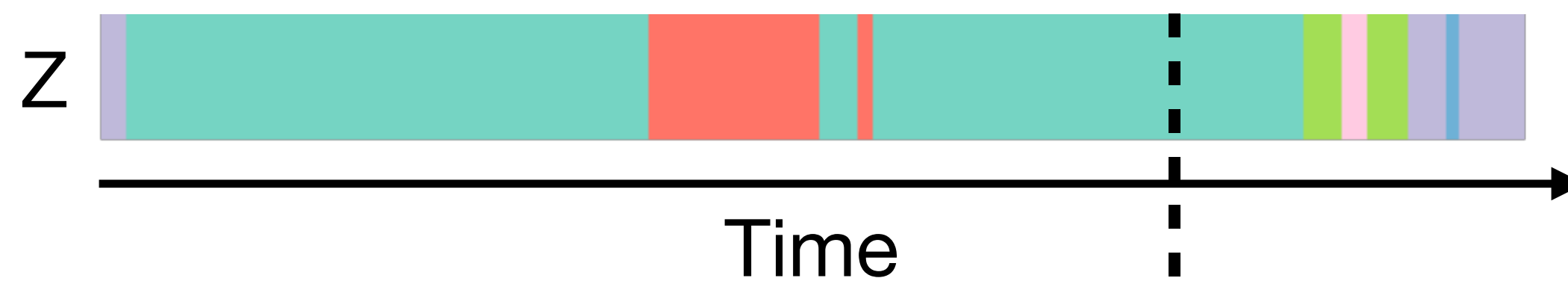
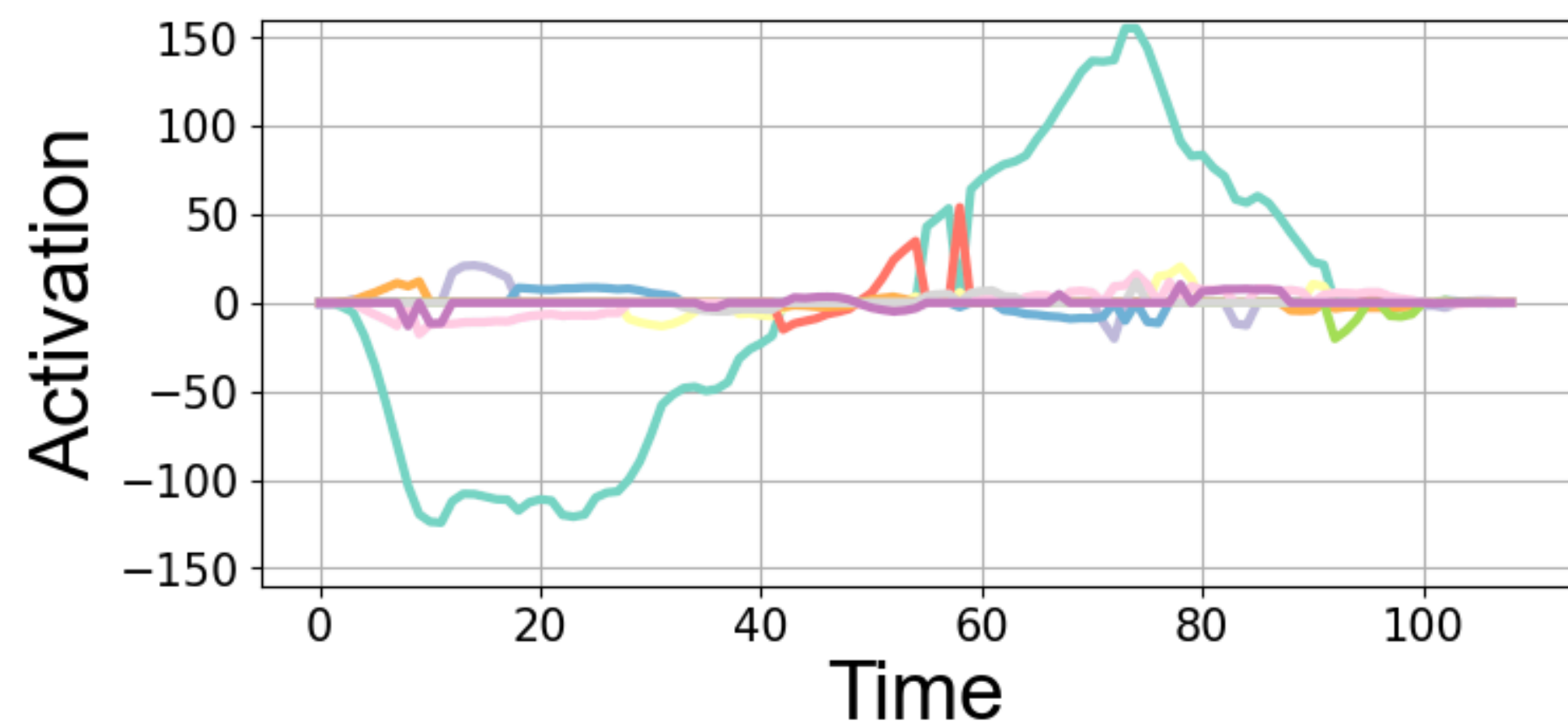
High contribution

Low contribution

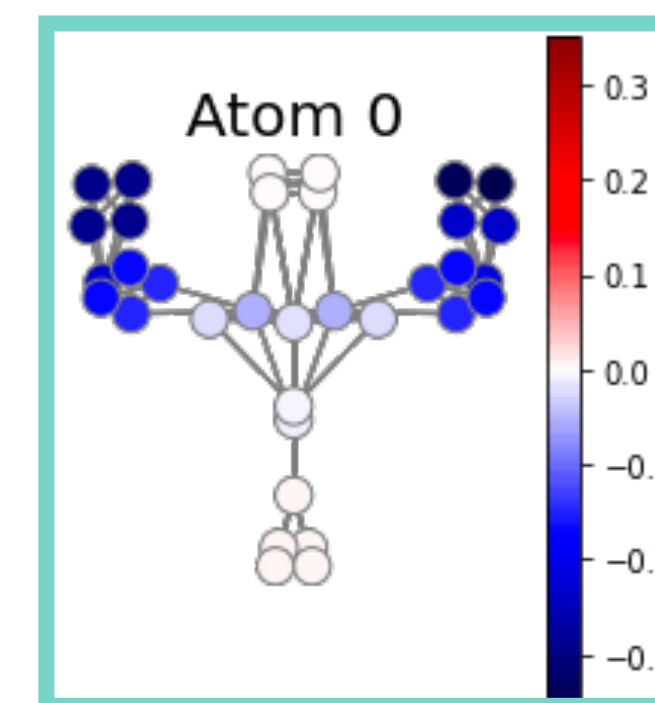
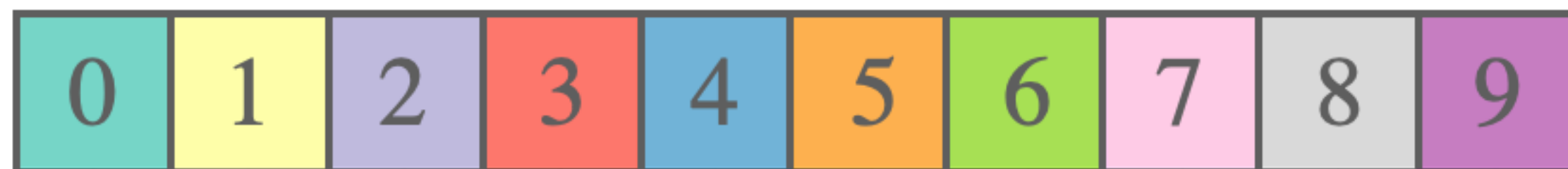
Timelines

Most activated super-atom over time

Bilateral elevation, Z-axis

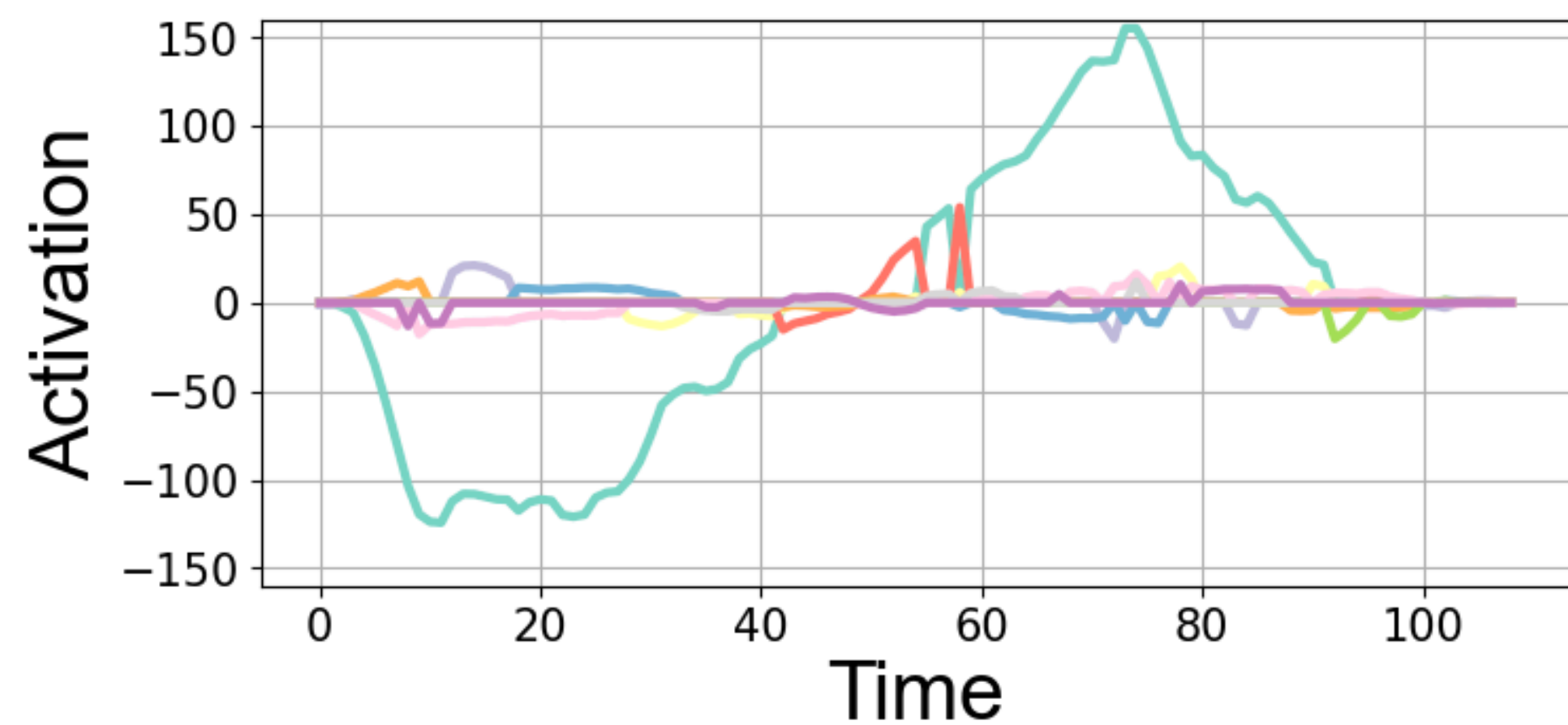


Super-atoms

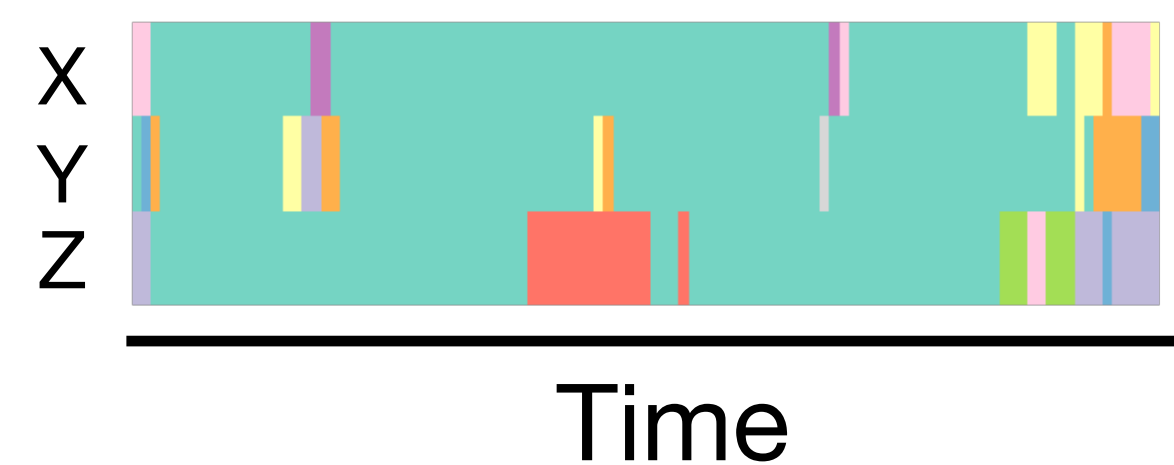
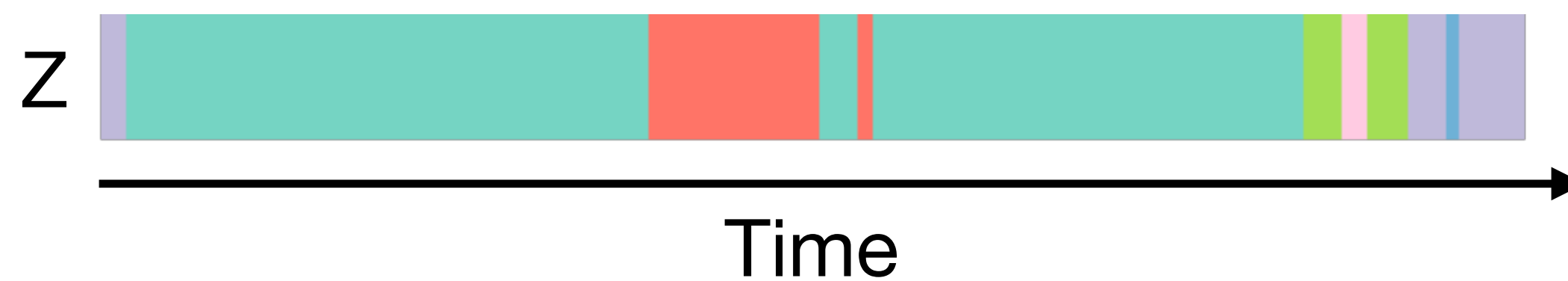


Timelines

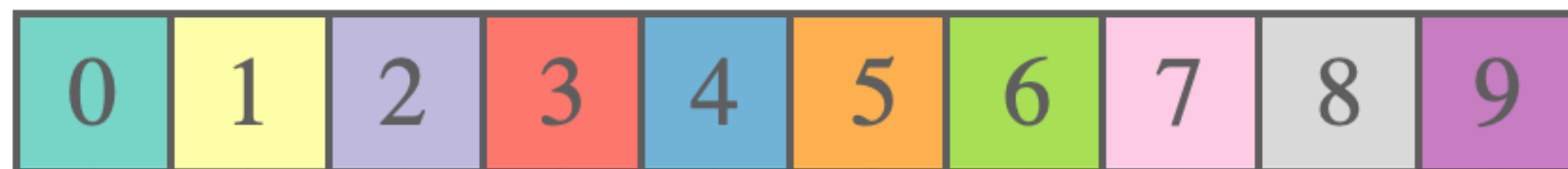
Bilateral elevation, Z-axis



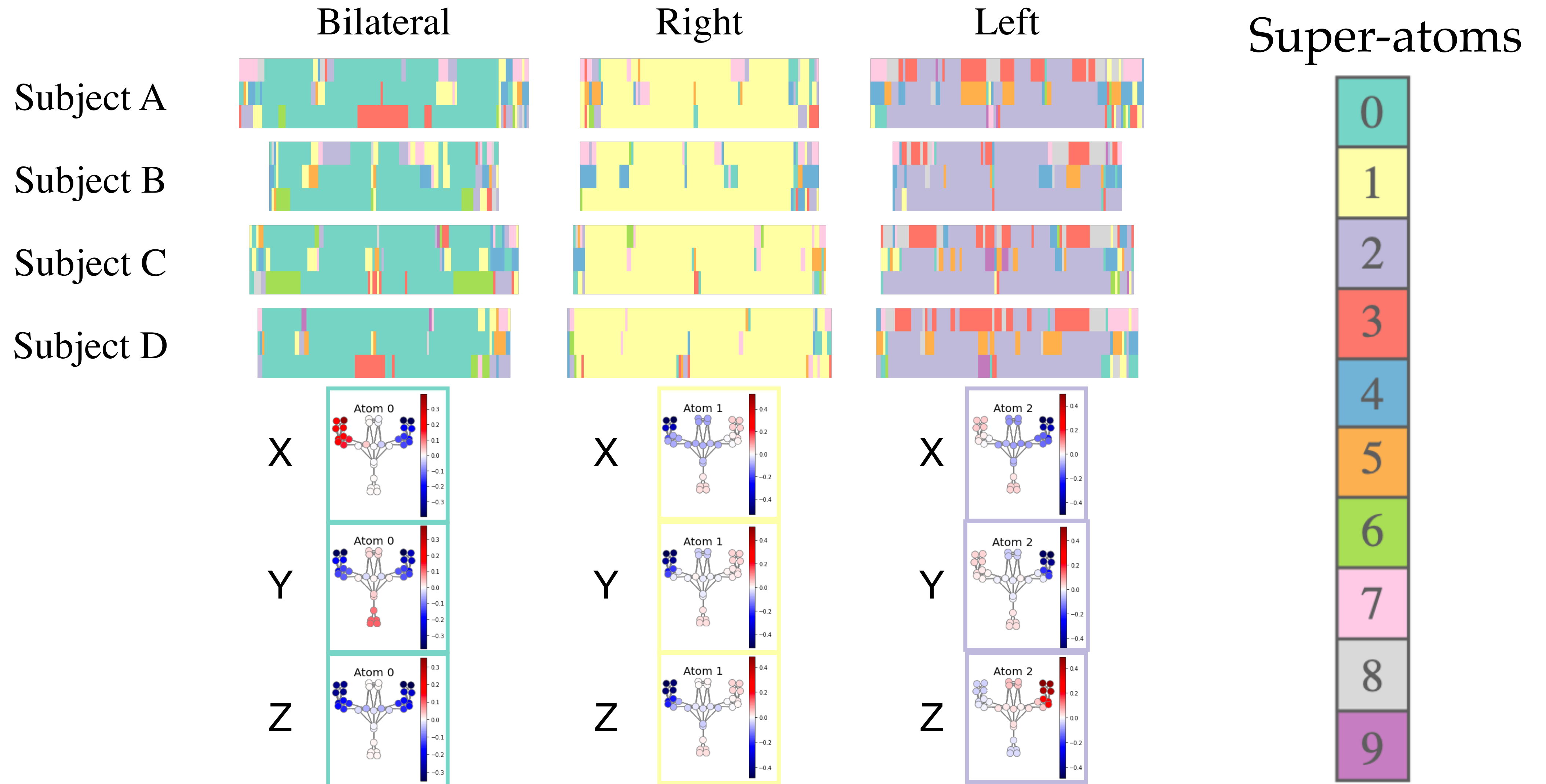
Most activated super-atom over time



Super-atoms

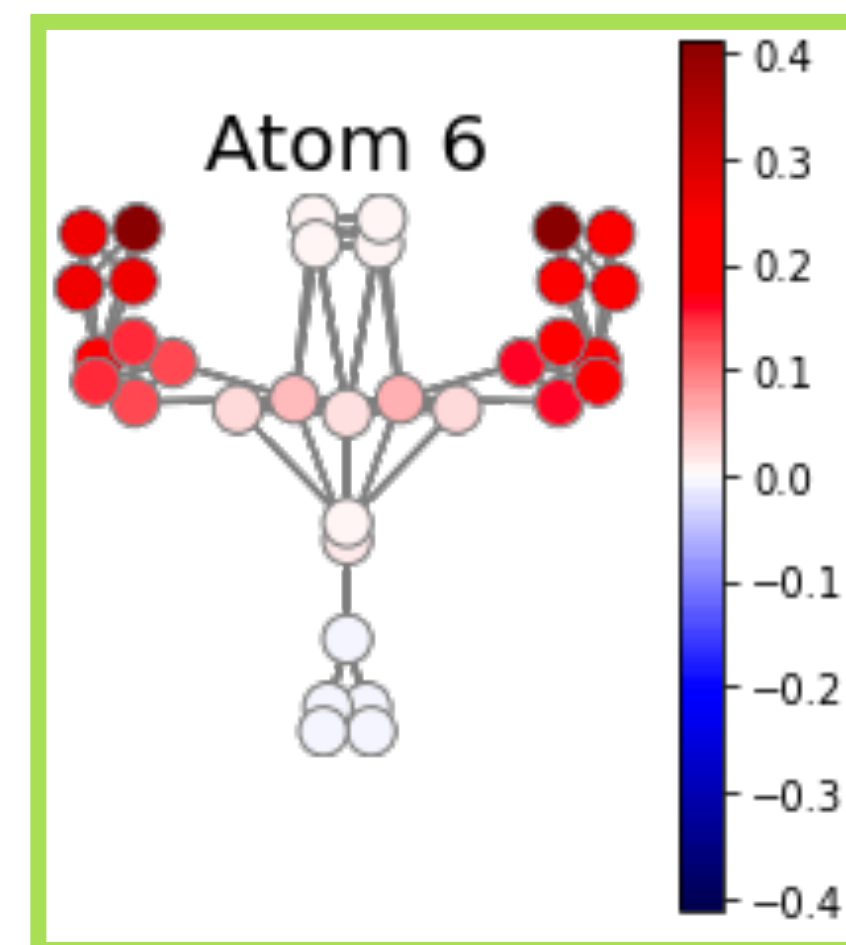
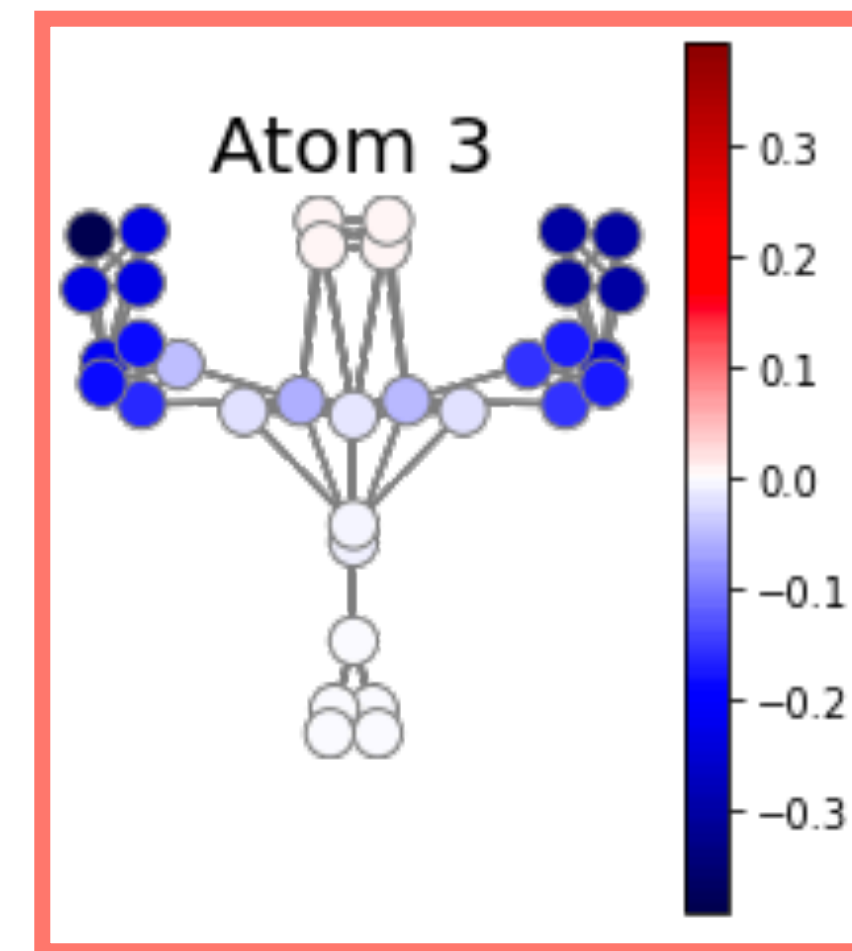
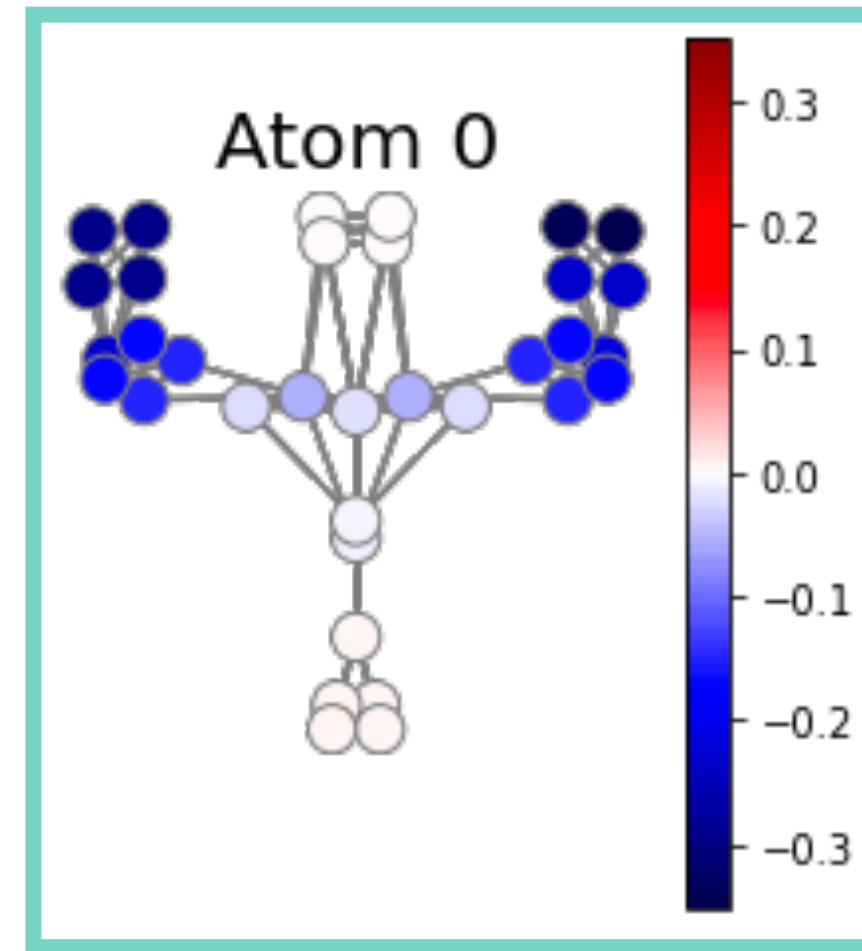
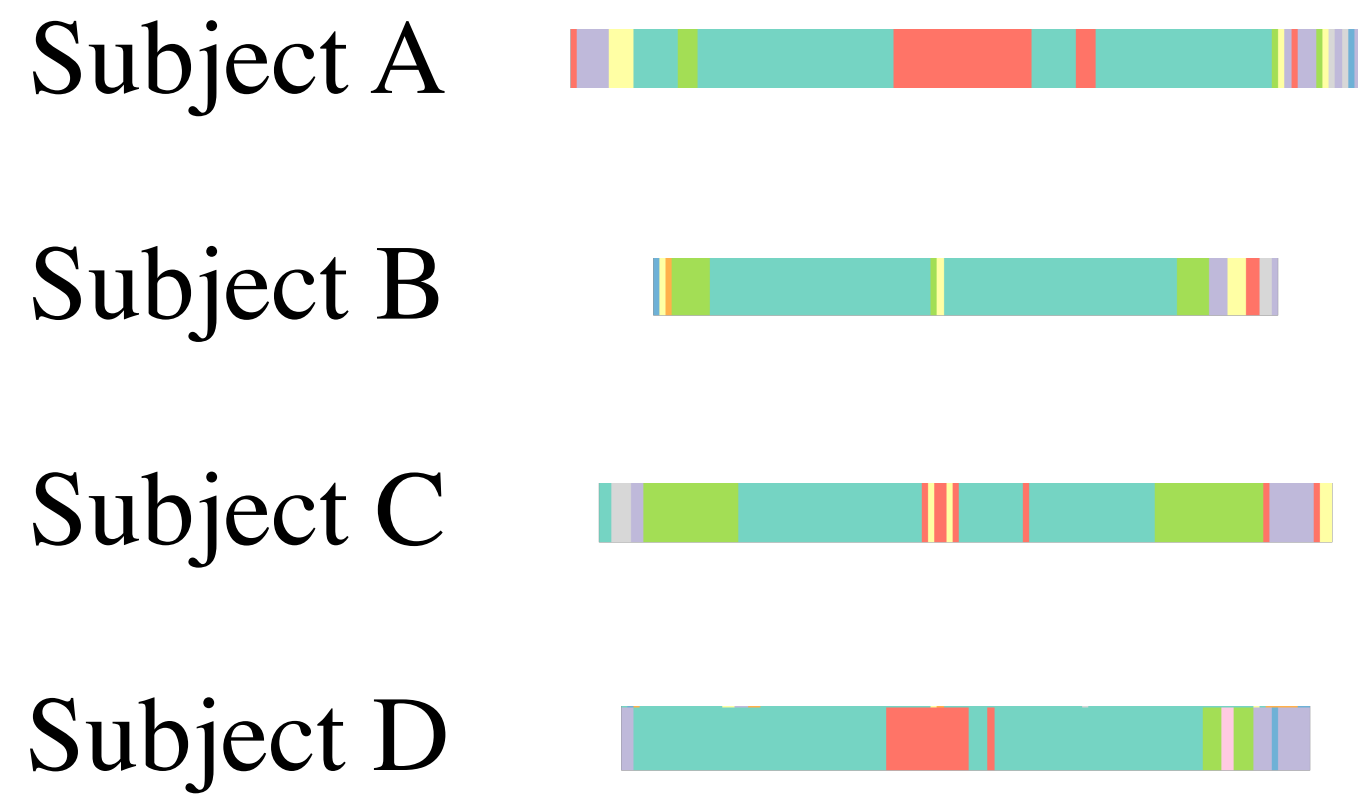


Timelines 1st activation



Zoom on 1st activation Timelines

Bilateral, z-axis



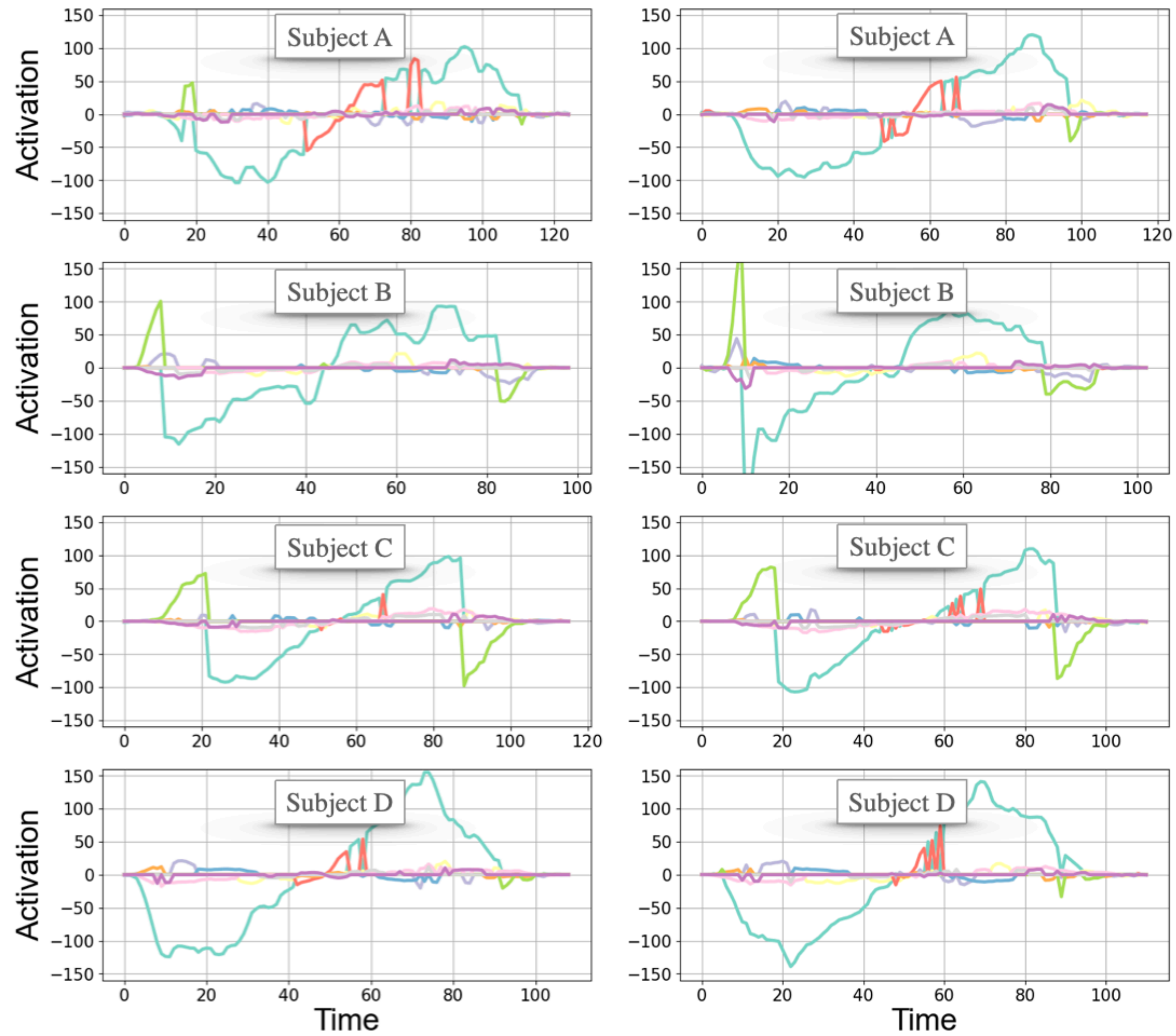
Super-atoms



➔ Different movement strategies

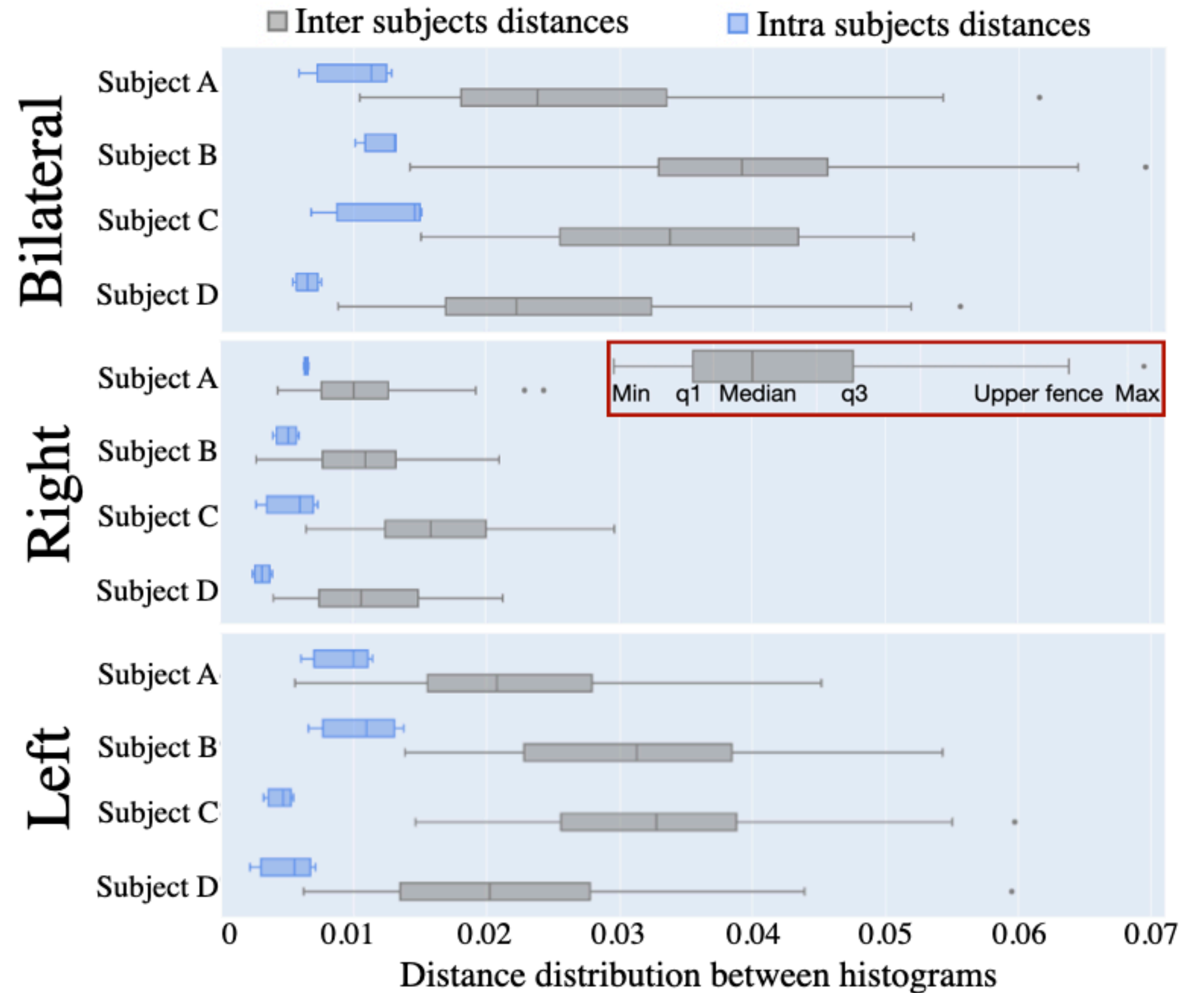
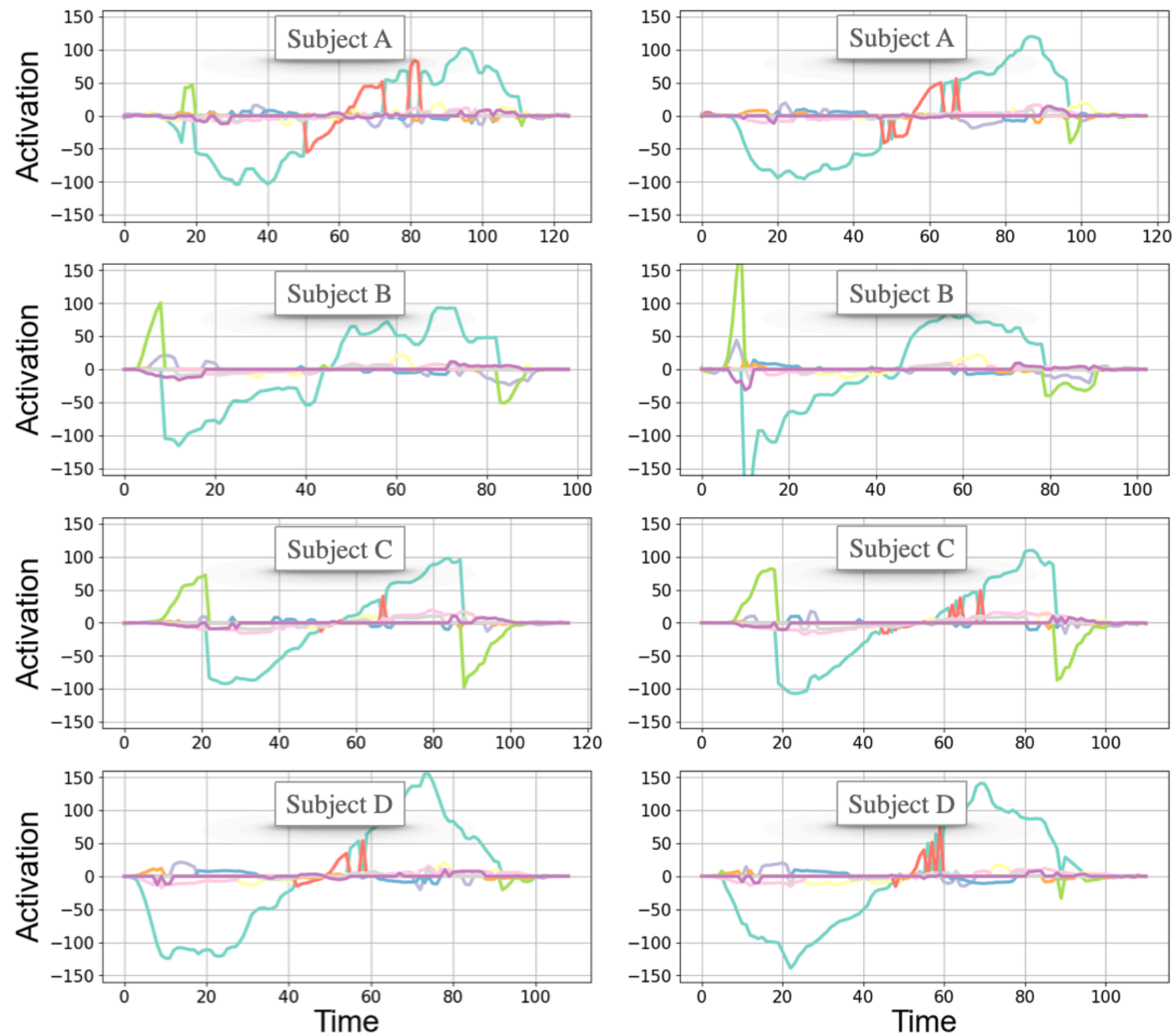
Inter / Intra subject comparison

Bilateral elevation, Z-axis



Inter / Intra subject comparison

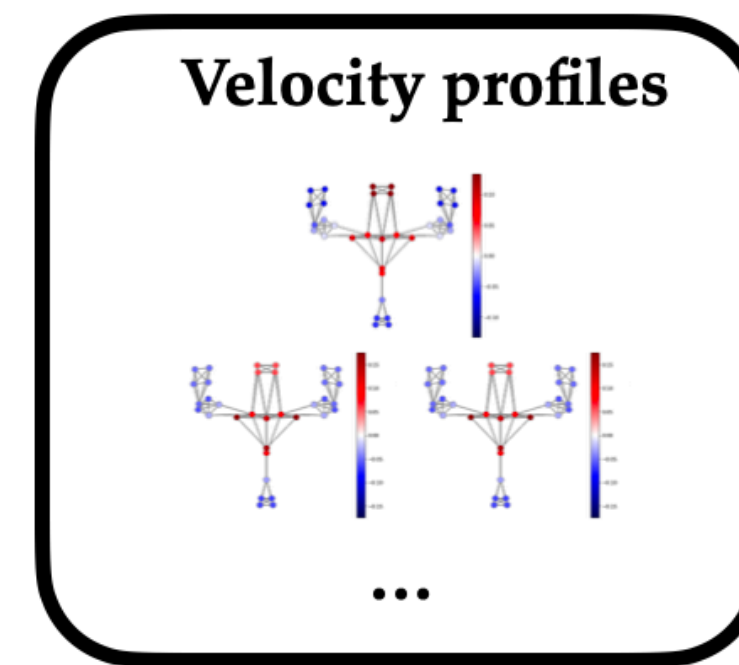
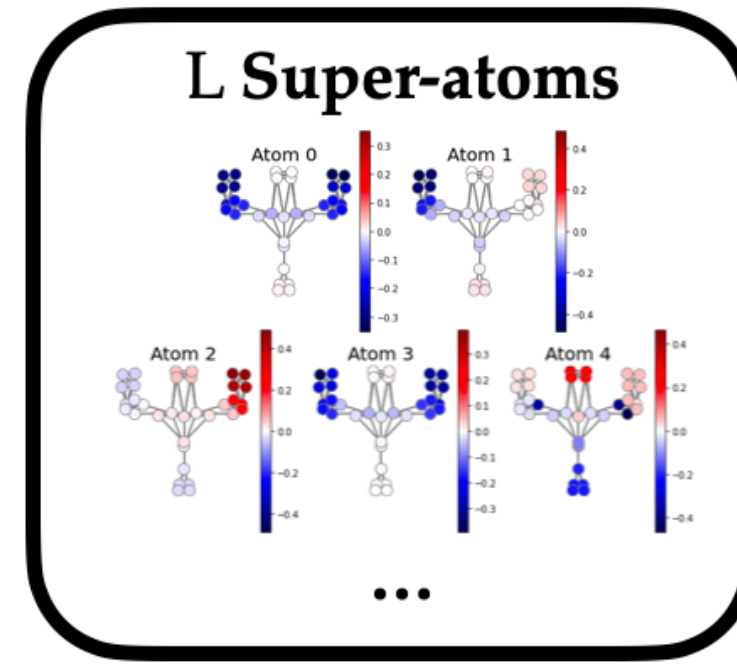
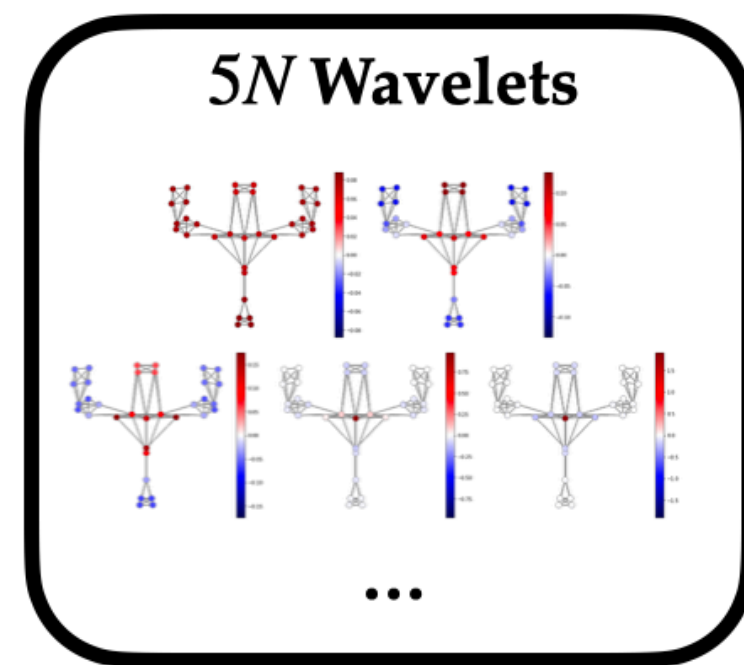
Bilateral elevation, Z-axis



DSMH Method

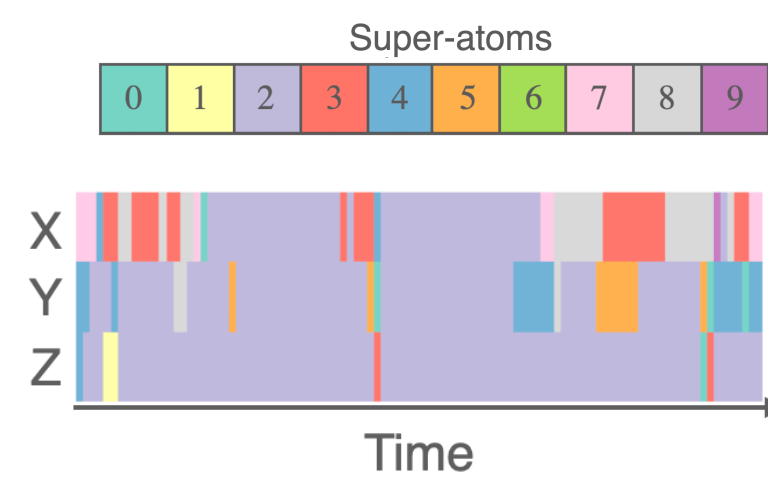
Construction of $L = 10$
super-atoms by combining
at most $P = 5$ wavelets

Use of at most $T = 3$ super-atoms
to approximate each graph signal



Qualitative
analysis of motion
sequences

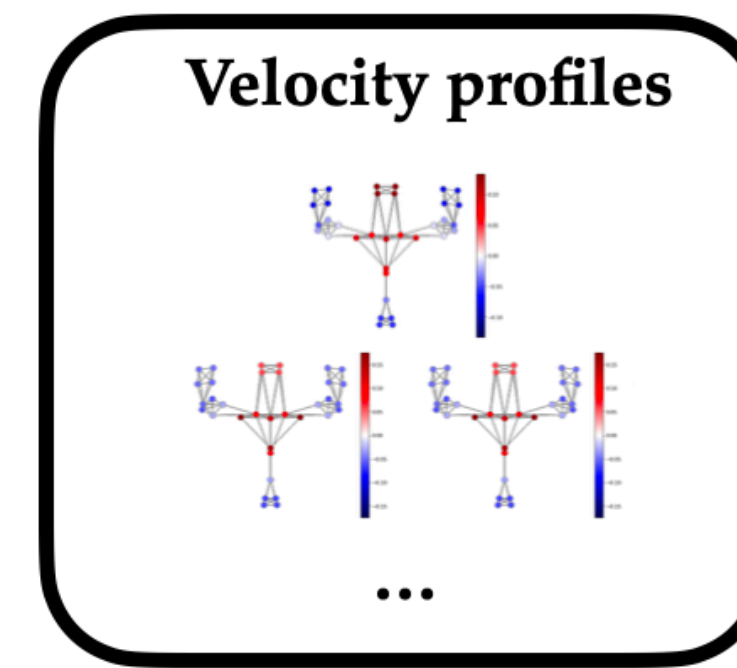
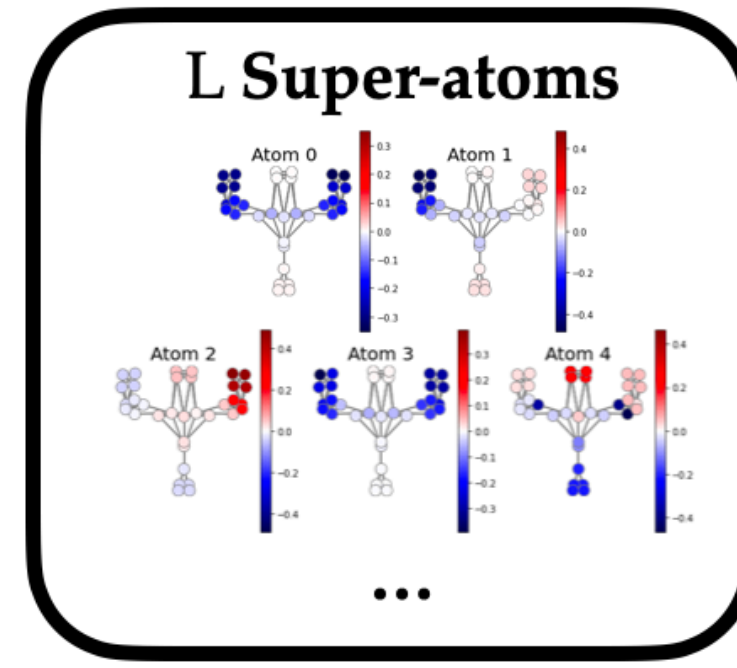
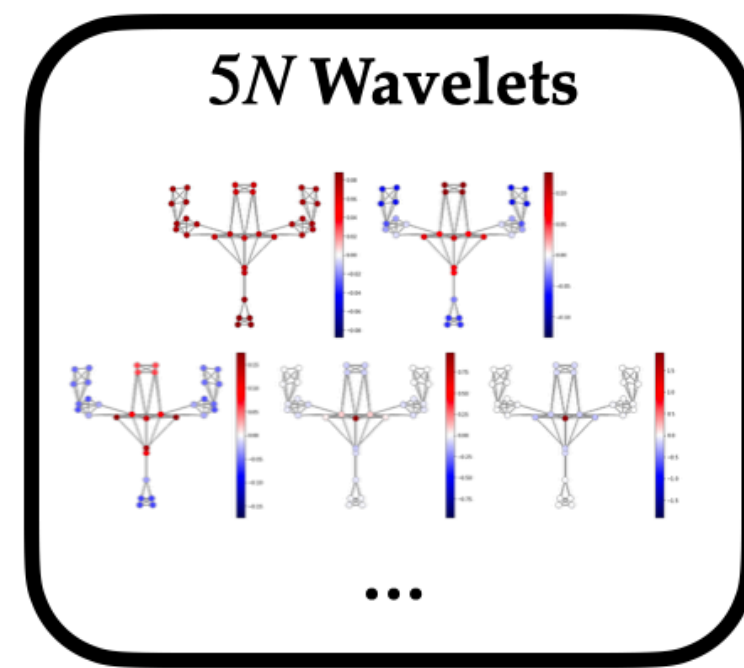
Timelines



DSMH Method

Construction of $L = 10$ super-atoms by combining at most $P = 5$ wavelets

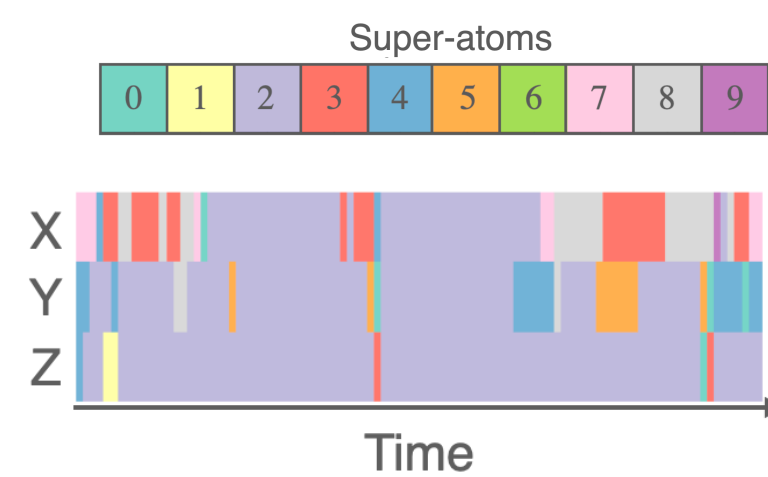
Use of at most $T = 3$ super-atoms to approximate each graph signal



Qualitative analysis of motion sequences

Quantitative comparison of motion sequences

Timelines



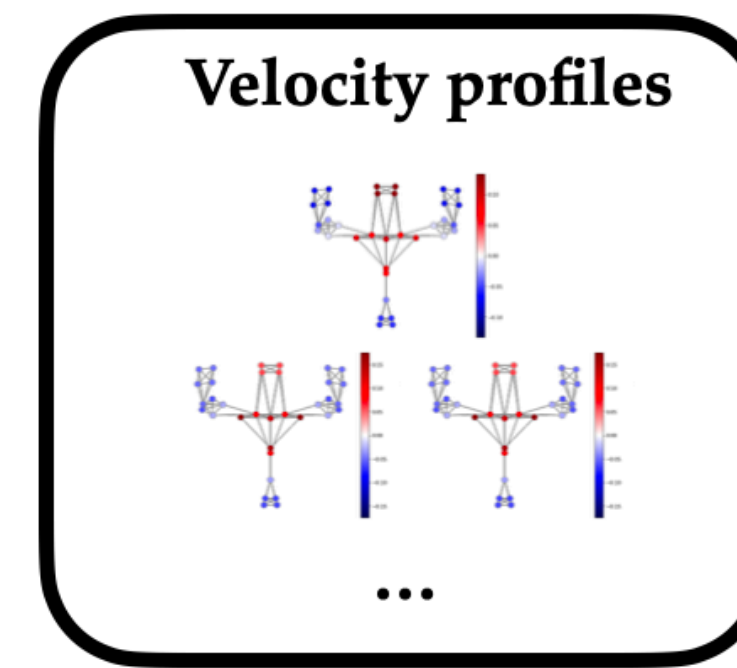
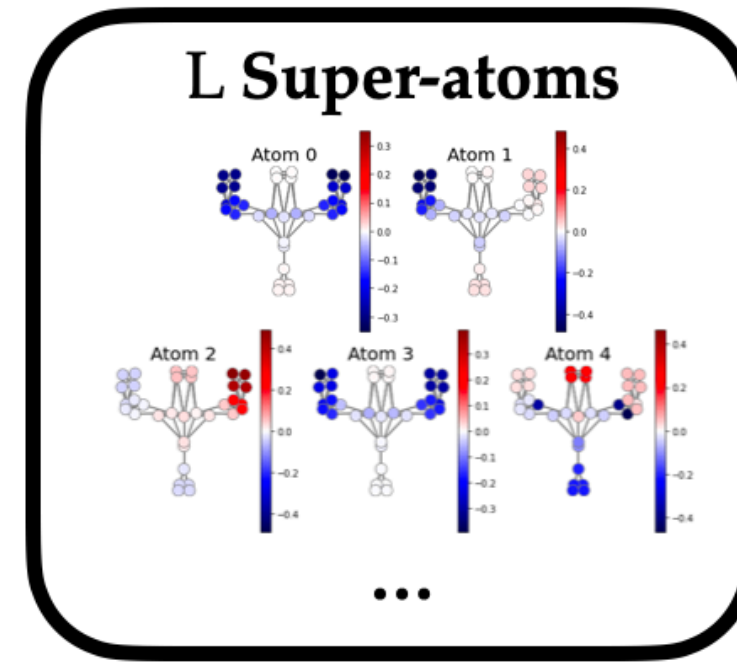
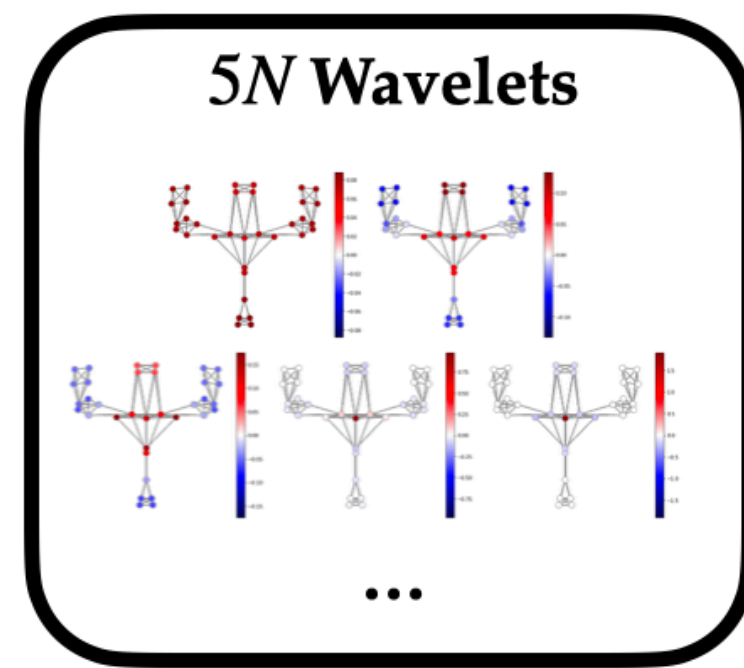
Histograms



DSMH Method

Construction of $L = 10$ super-atoms by combining at most $P = 5$ wavelets

Use of at most $T = 3$ super-atoms to approximate each graph signal

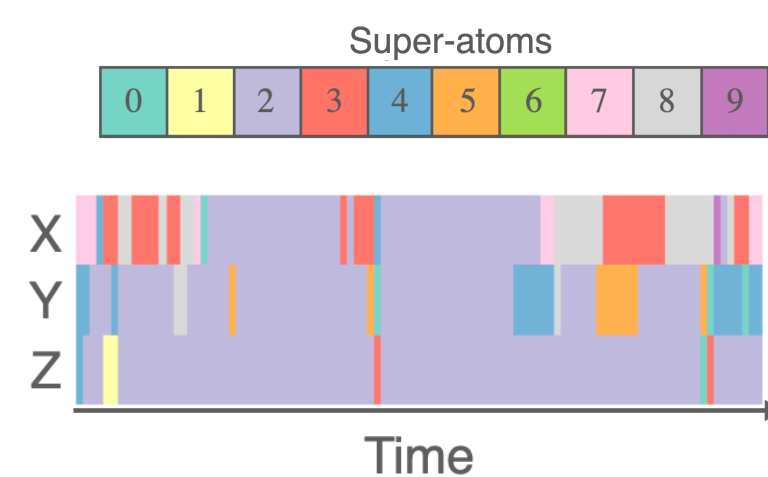


Qualitative analysis of motion sequences

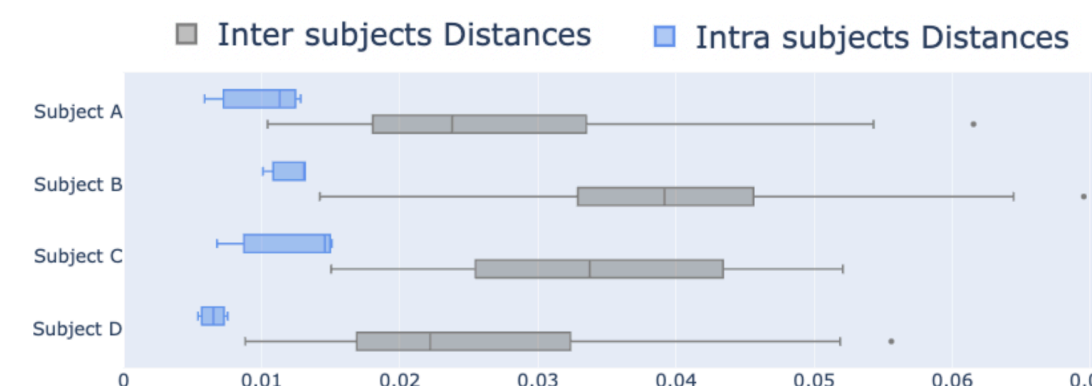
Quantitative comparison of motion sequences

Other applications

Timelines



Histograms



Denoising + Human action recognition

Thanks for your attention

Marion Chauveau, Antoine Mazarguil and Laurent Oudre

Contact: marion.chauveau@univ-grenoble-alpes.fr

Université Paris-Saclay, Université Paris Cité, ENS Paris-Saclay, CNRS,
SSA, INSERM, Centre Borelli, F-91190, Gif-sur-Yvette, France



Annexes

DSMH dictionary

X

Y

Z

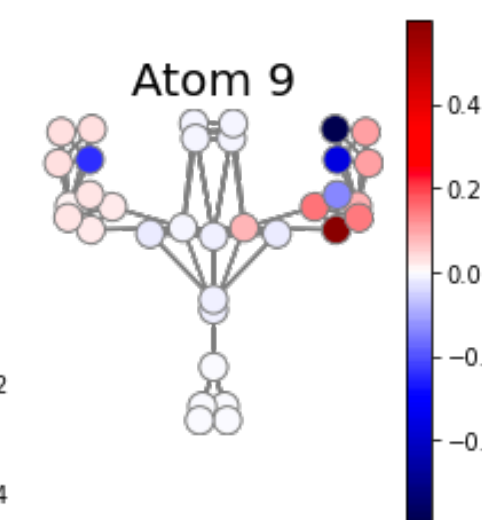
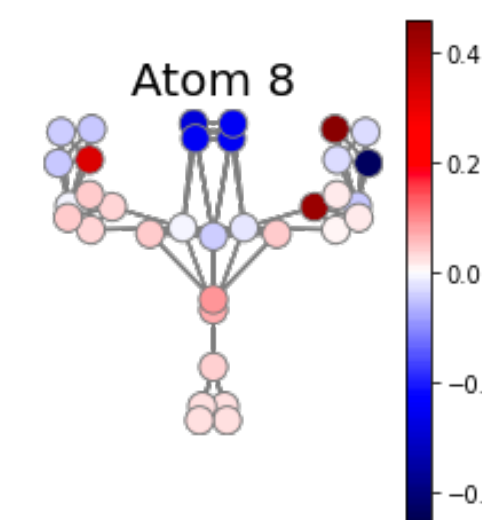
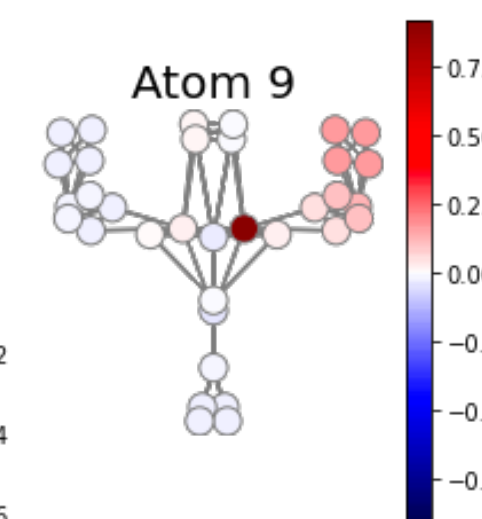
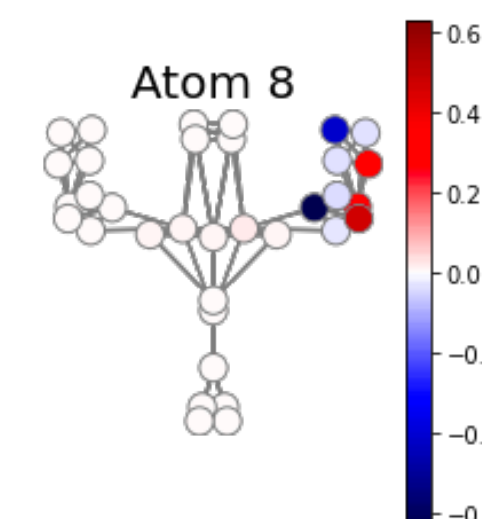
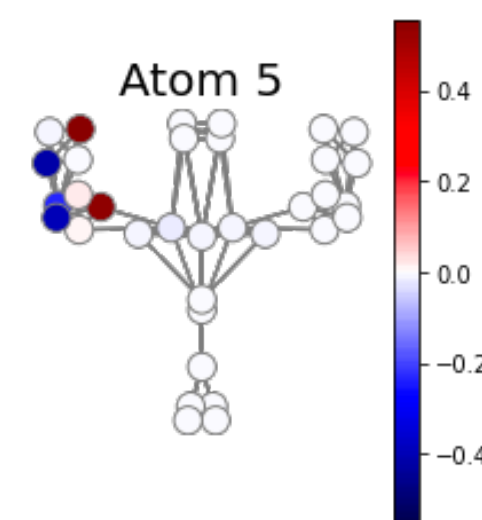
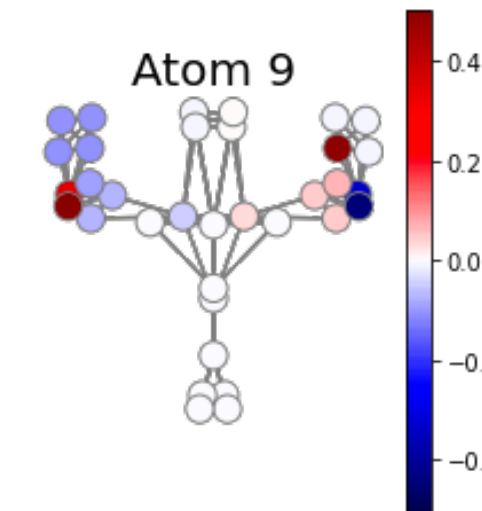
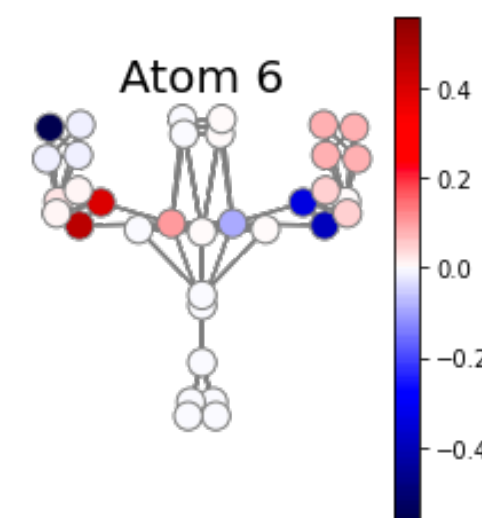
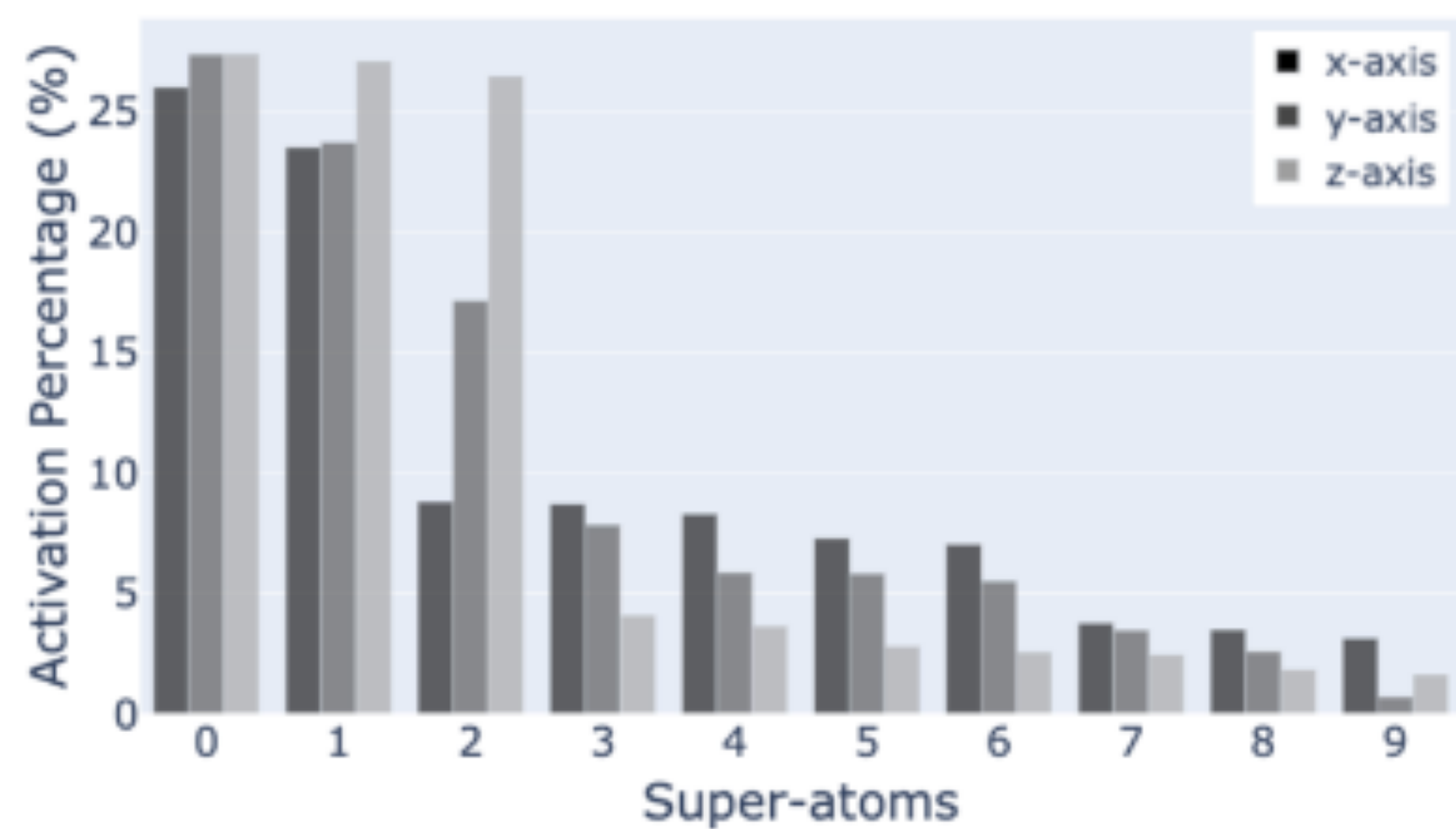


DSMH dictionary

X

Y

Z



Human action recognition

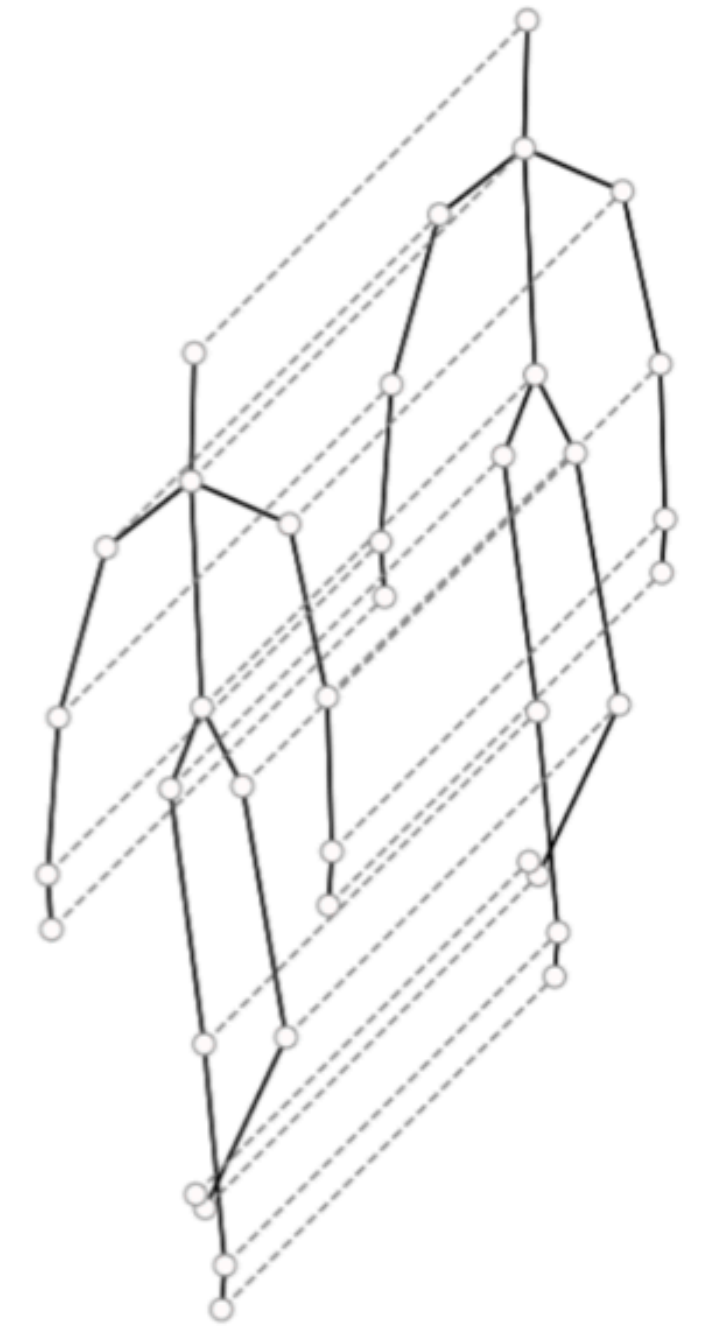
Recognition Method	UTK	MSR	F3D
Spatio-temporal Graph + GFT	95 %	71,45 %	82,63 %
Spatio-temporal Graph + DSMH	95,5 %	70,14 %	78,12 %
Weighted Graph + GFT	94,97 %	70,78 %	79,76 %
Weighted Graph + DSMH	96 %	71,94 %	82,38 %

Recognition Method	UTK [14]	MSR [15]	F3D [16]	ntu_cs_mini [5] [17]
Kao et al. [8]	95.00	71.45	82.63	-
ST-GCN [1], [5], [18]	-	27.64 (CS)	-	71.53 (CS)
GR-GCN [3]	98.5*	-	98.4*	-
Deep STGC _K [2]	-	-	99.1*	-
shift-GCN [4], [5]	-	-	-	60.00 (CS)
Our method	96.00	71.94	82.38	66.25

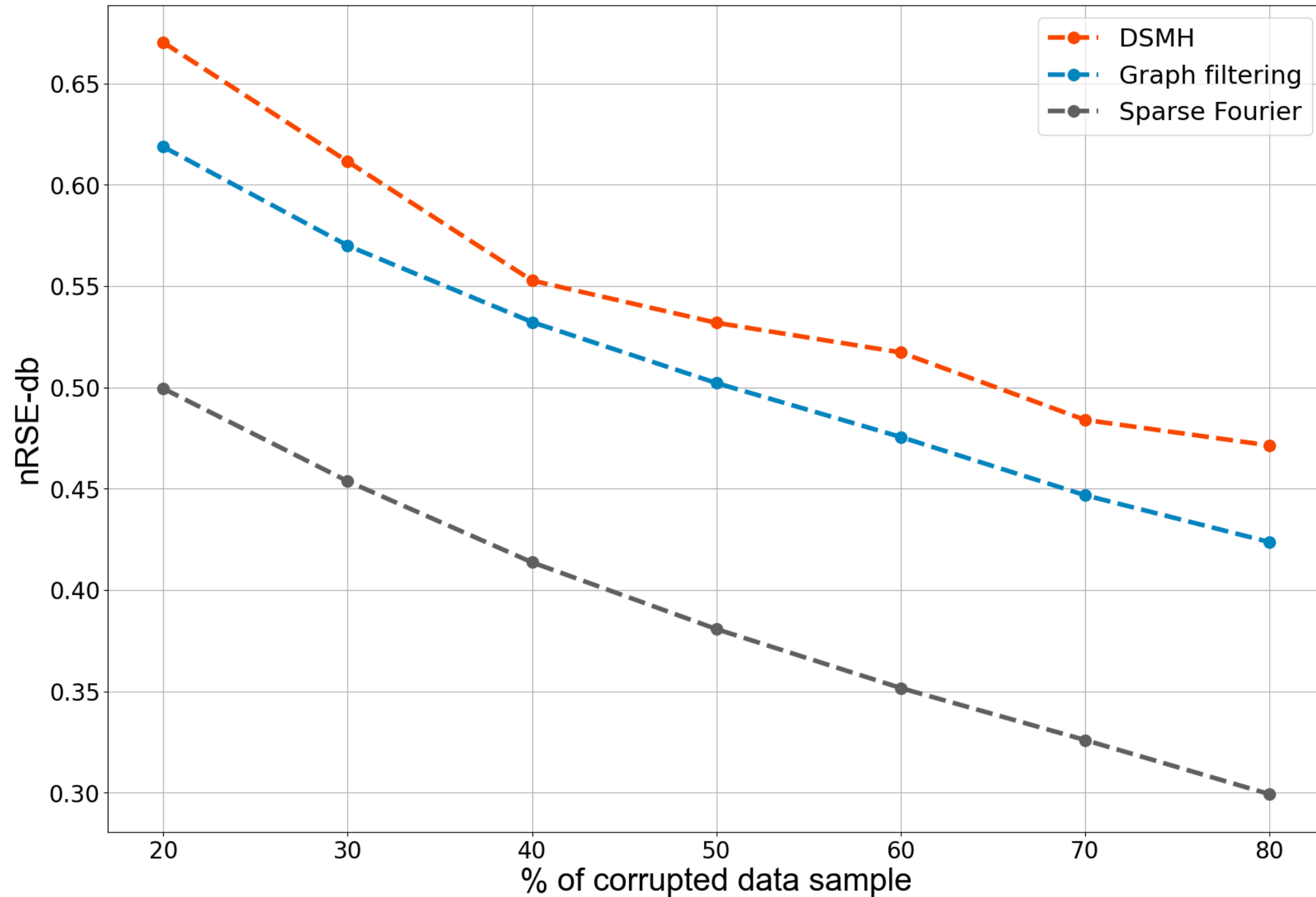
Weighted graph



Spatio-temporal graph



Denoising



$$\text{nRSE-db} = -\log_{10}\left(\frac{\|Y - Y_{denoised}\|_F}{\|Y\|_F}\right)$$

DSMH method:

$$Y_{denoised} = \Phi AX$$

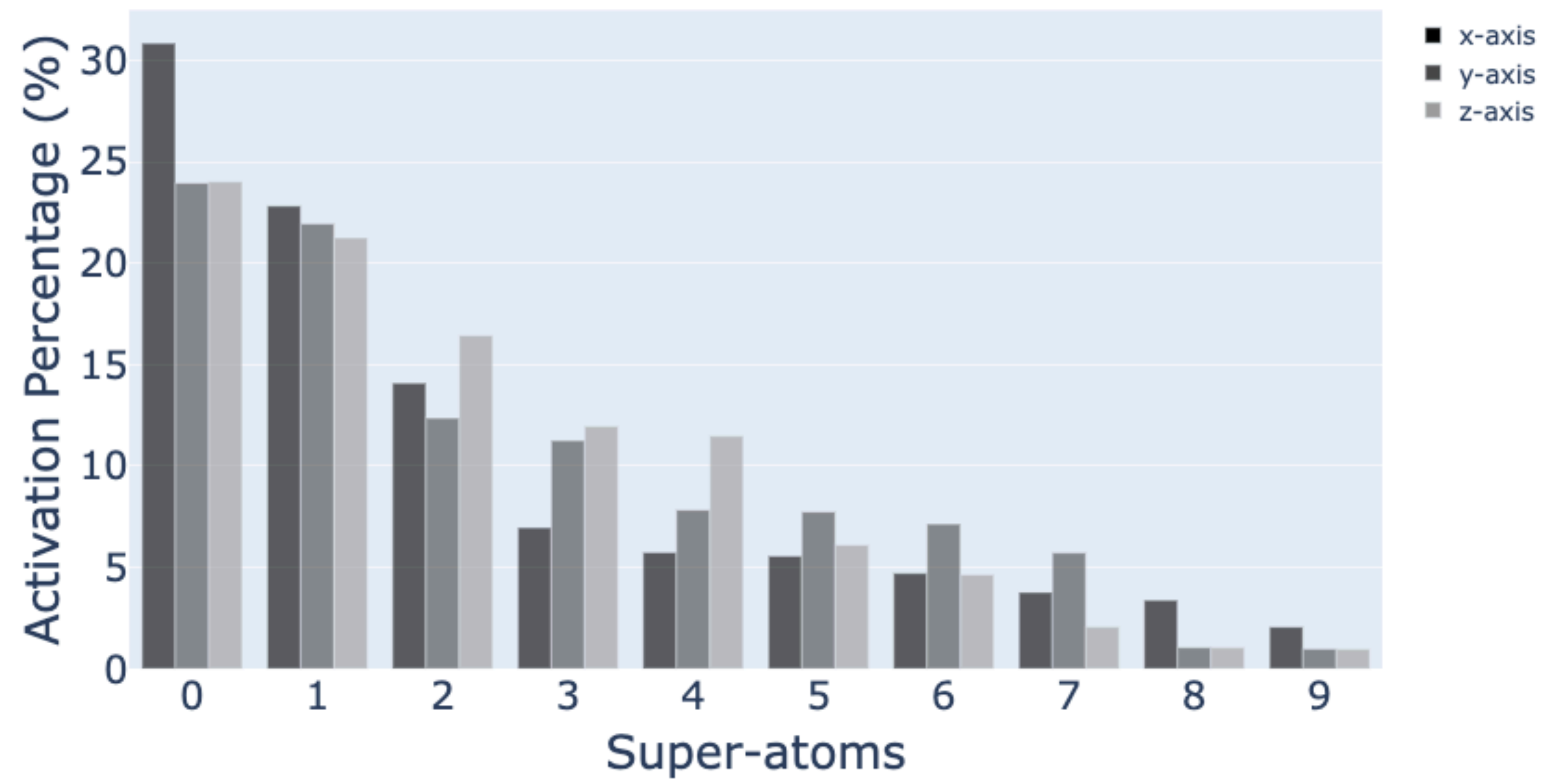
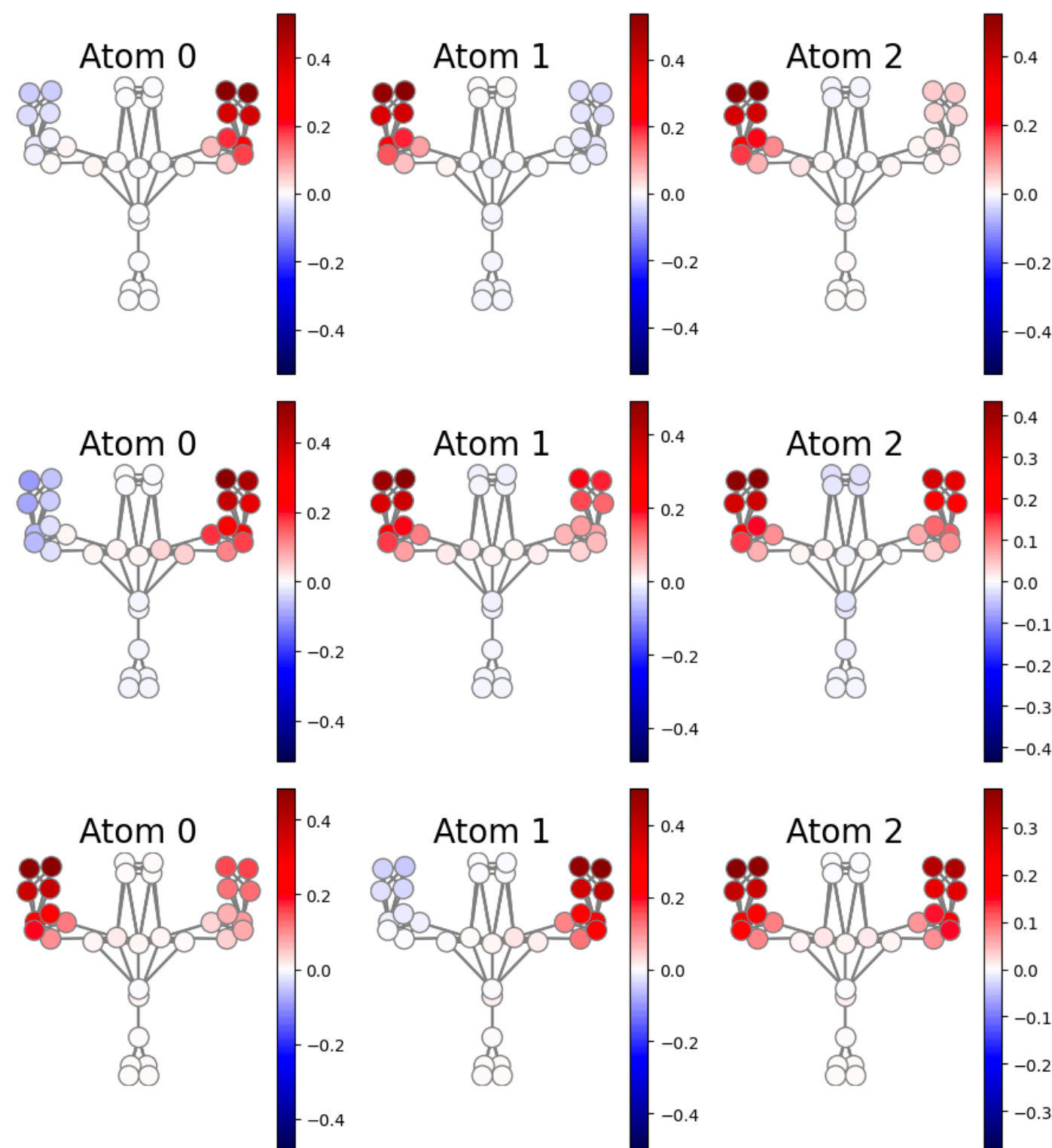
Graph filtering method:

$$Y_{denoised} = (I + \alpha(I - A)^*(I - A))^{-1}Y$$

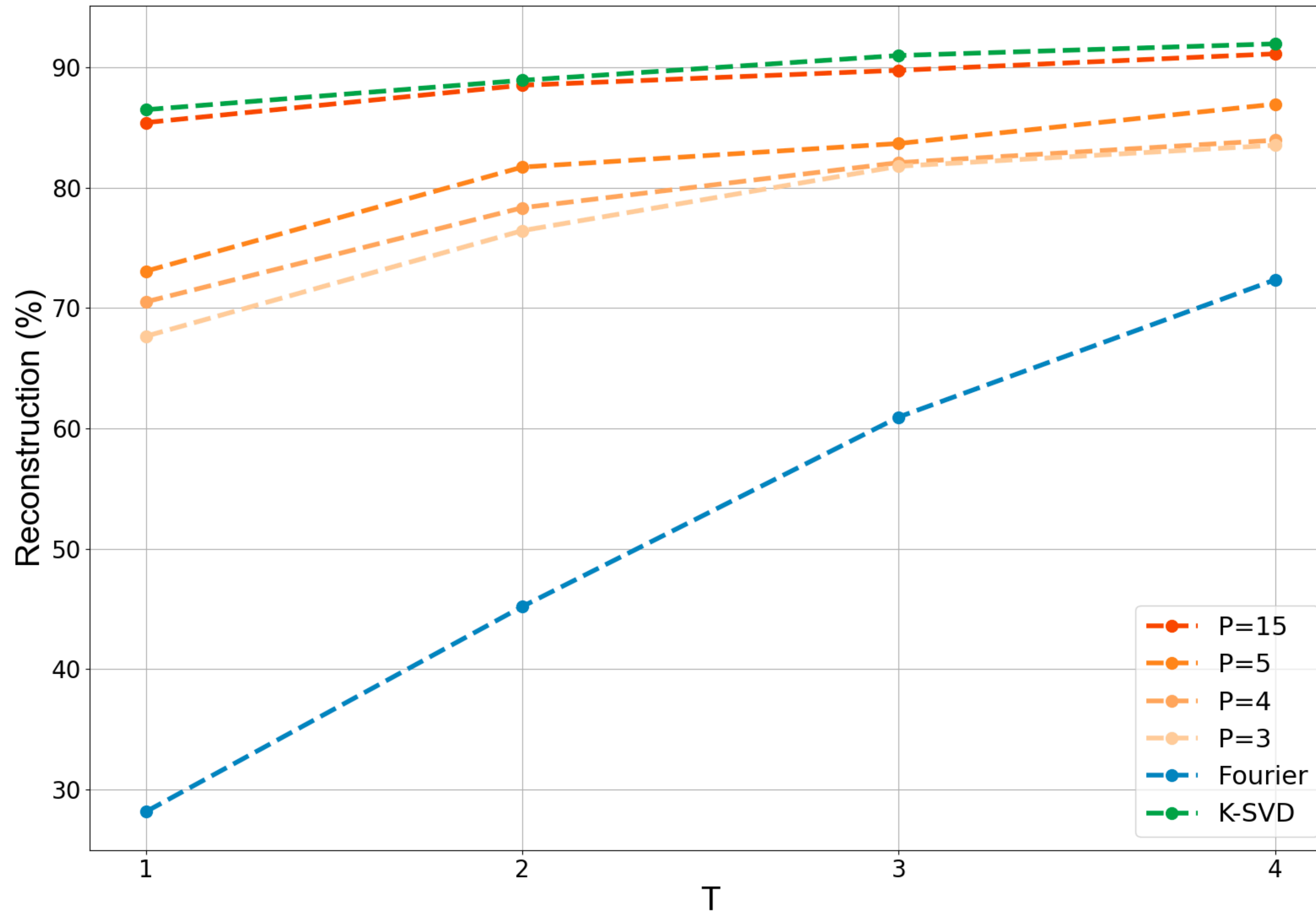
Method	20% of corr. data	50% of corr. data
Noisy data	0.49	0.29
Graph filtering [45]	0.62	0.50
Sparse Fourier [44]	0.50	0.38
DSMH	0.72	0.55

TABLE I. nRSE-db obtained for 20% and 50% of corrupted samples with the following 3 methods: the double sparsity method ($s_1 = 5$, $s_2 = 7$, $L = 10$), the graph filtering method ($\alpha = 0.39$), and the sparse Fourier method ($s_1 = 5$).

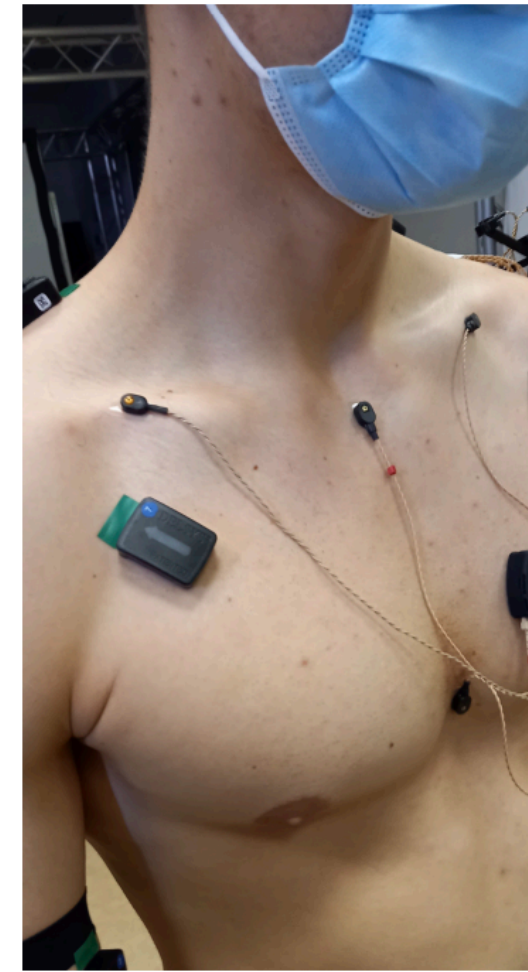
Unconstrained dictionary



Signal reconstruction



Arm-CODA

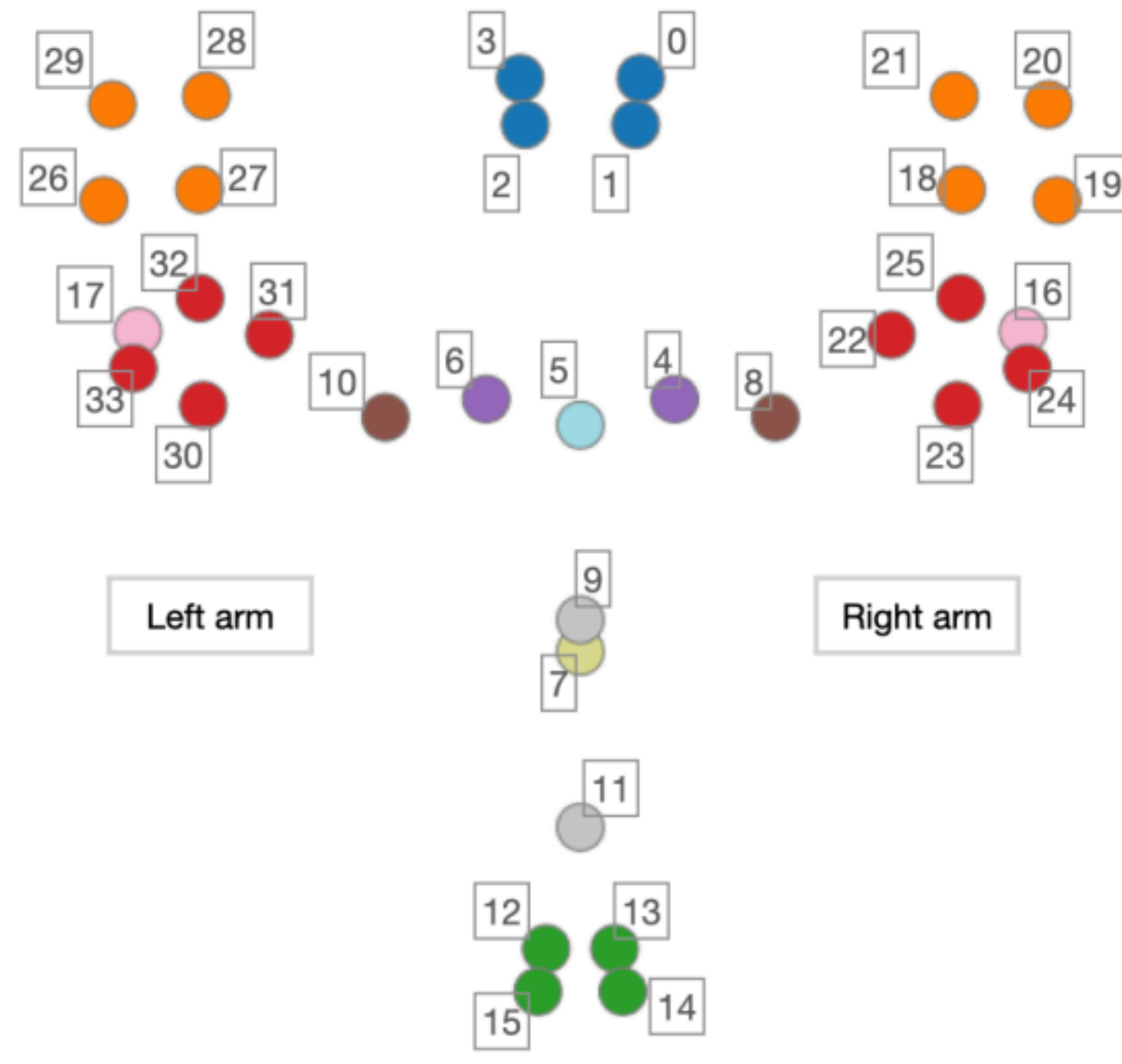
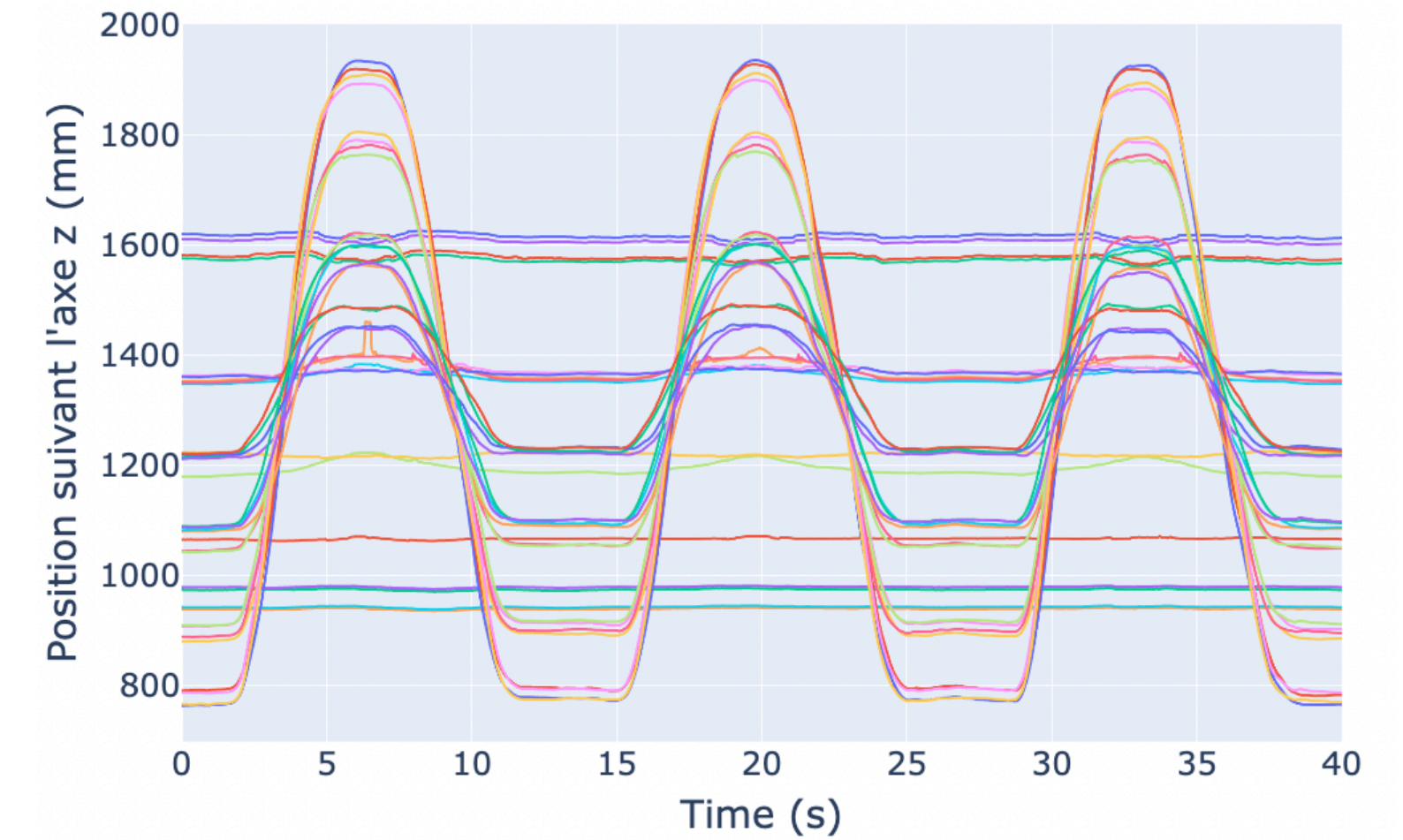


(a) CODA simple marker placed on the front side of the subject



(b) CODA cluster placed on the subject's forearm

Bilateral elevation in the Scapular plane, Sujet 04



Marker index	Marker type	Position
0-3	Cluster	Top of the forehead
4	Simple marker	Middle of the right clavicle
5	Simple marker	Sternal manubrium, just below the jugular incisure
6	Simple marker	Middle of the left clavicle
7	Simple marker	2 cm above the xiphoid process
8	Simple marker	Middle of the right scapular spine
9	Simple marker	Apophysis of T7
10	Simple marker	Middle of the left scapular spine
11	Simple marker	Apophysis of L3
12-15	Cluster	Below posterior superior iliac spine
16	Simple marker	Right elbow, lateral epicondyle of the humerus
17	Simple marker	Left elbow, lateral epicondyle of the humerus
18-21	Cluster	Right forearm
22-25	Cluster	Lateral face of the right arm, close to the elbow
26-29	Cluster	Left forearm
30-33	Cluster	Lateral face of the left arm, close to the elbow

Arm-CODA

	Age	Height (cm)	Weight (kg)	BMI (kg/m ²)
mean (\pm std)	44.2 (\pm 14.1)	173.7 (\pm 8.4)	73.7 (\pm 11.8)	24.4 (\pm 3.1)
min	23.0	156.0	51.0	19.1
max	65.0	188.0	95.0	29.0

Table 1: Summary of the participants' characteristics.

34 Cartesian Optoelectronic Dynamic Anthropometer (CODA) motion system 3D position markers

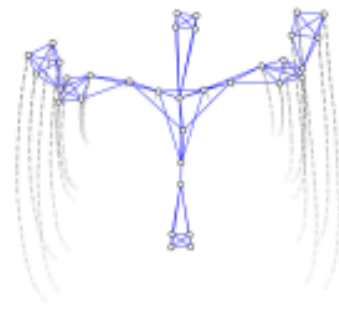
Active sensors emit an optical signal received by six depth cameras

Sensor fusion algorithm merges the measurements of the different cameras and obtain estimate of the position of each sensor

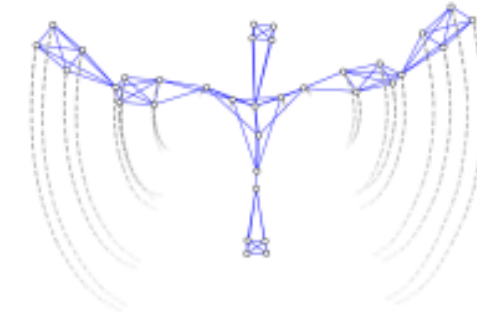
Data position of the 34 sensors is measured at 100 Hz

- Simple markers (see Figure 5(a)), attached to the subject's skin by an adhesive strip, powered by a battery placed on the subject's body (each battery powers up to 4 markers).
- Markers associated with a rectangular cluster (see Figure 5(b)), including a battery, attached to the subject with a strap. Each cluster was shaped like a rectangle with 4 markers positioned in its corners, allowing it to locate the fixed structure in space and orientation.

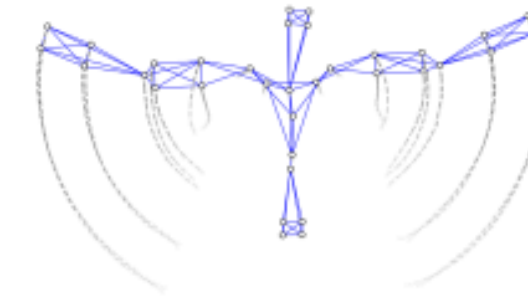
Arm-CODA



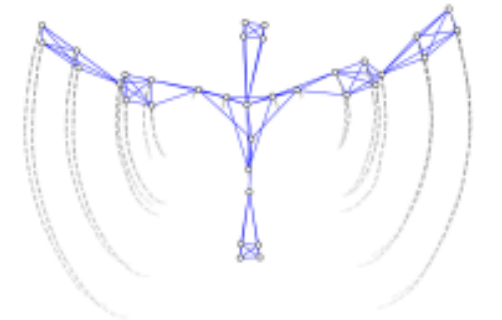
Mvt 0: Sagittal plane elevation (Seated)



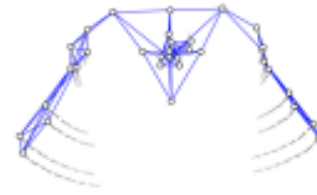
Mvt 1: Scapular plane elevation (Seated)



Mvt 2: Frontal plane elevation (Seated)



Mvt 3: Scapular plane elevation with lateral wrist orientation (Seated)



Mvt 4: Lateral elbow rotation (Seated and seen from above)



Mvt 5: Hair combing, right arm (Seated)



Mvt 6: Hair combing, left arm (Seated)



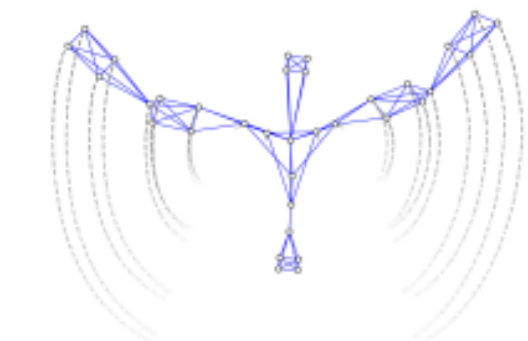
Mvt 7: Low back washing, right arm (Seated)



Mvt 8: Low back washing, left arm (Seated)



Mvt 9: Sagittal plane elevation (Standing)



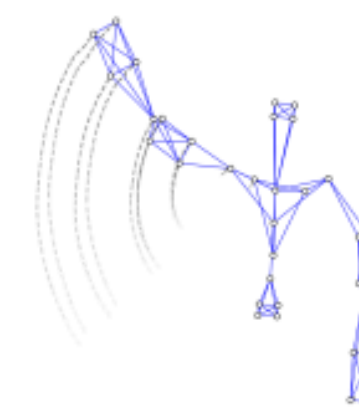
Mvt 10: Scapular plane elevation (Standing)



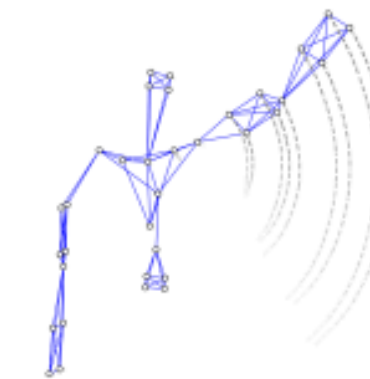
Mvt 11: Sagittal right arm elevation (Standing)



Mvt 12: Sagittal left arm elevation (Standing)

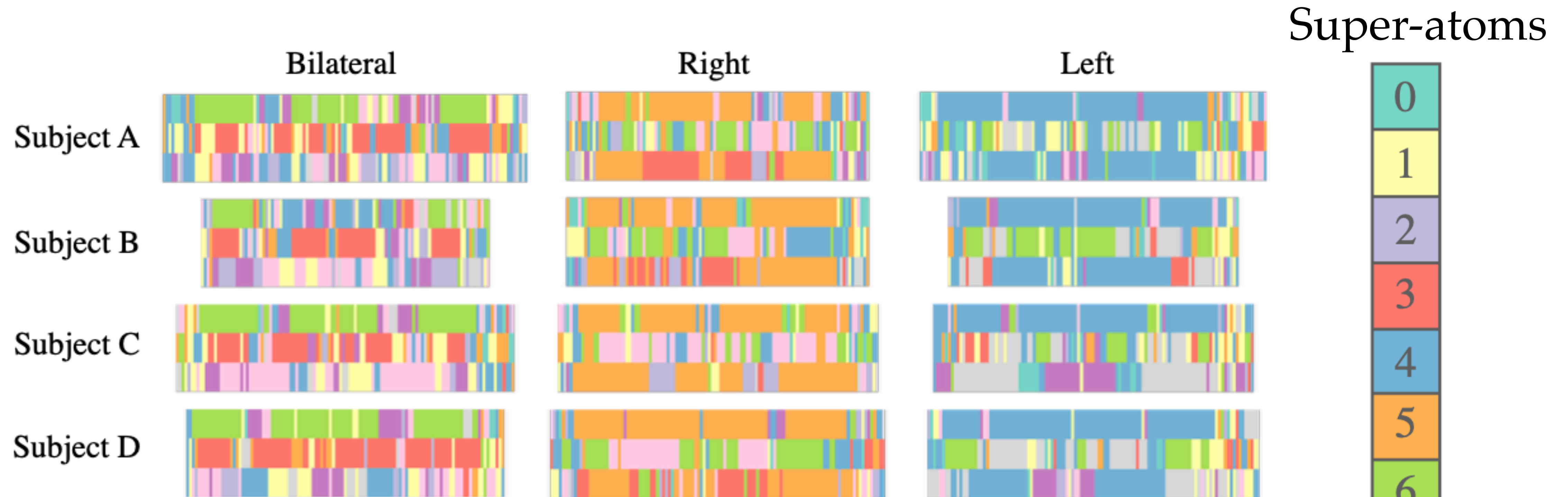


Mvt 13: Scapular right arm elevation (Standing)



Mvt 14: Scapular left arm elevation (Standing)

Timelines 2nd activation

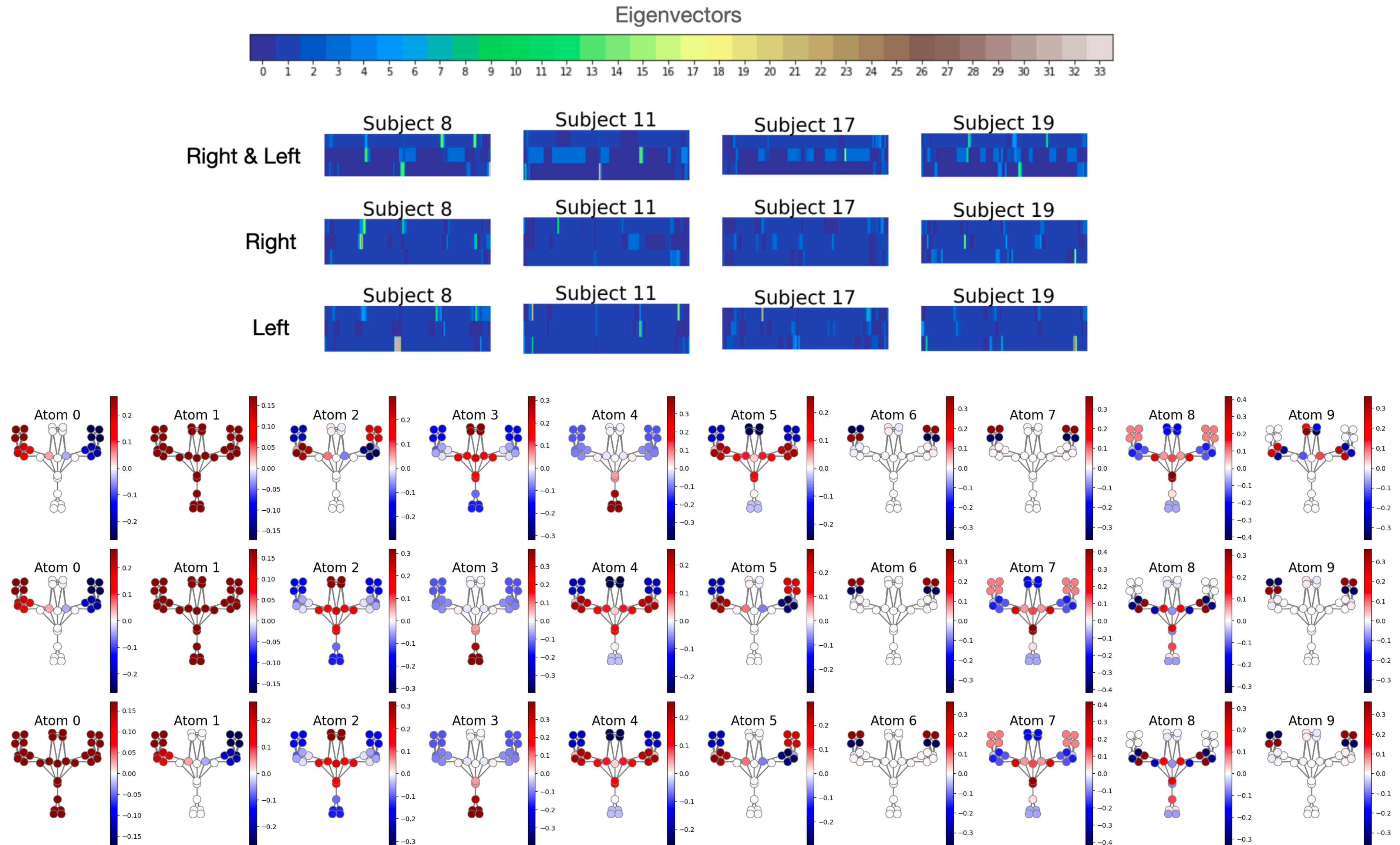


More variations over time & more differences between subjects

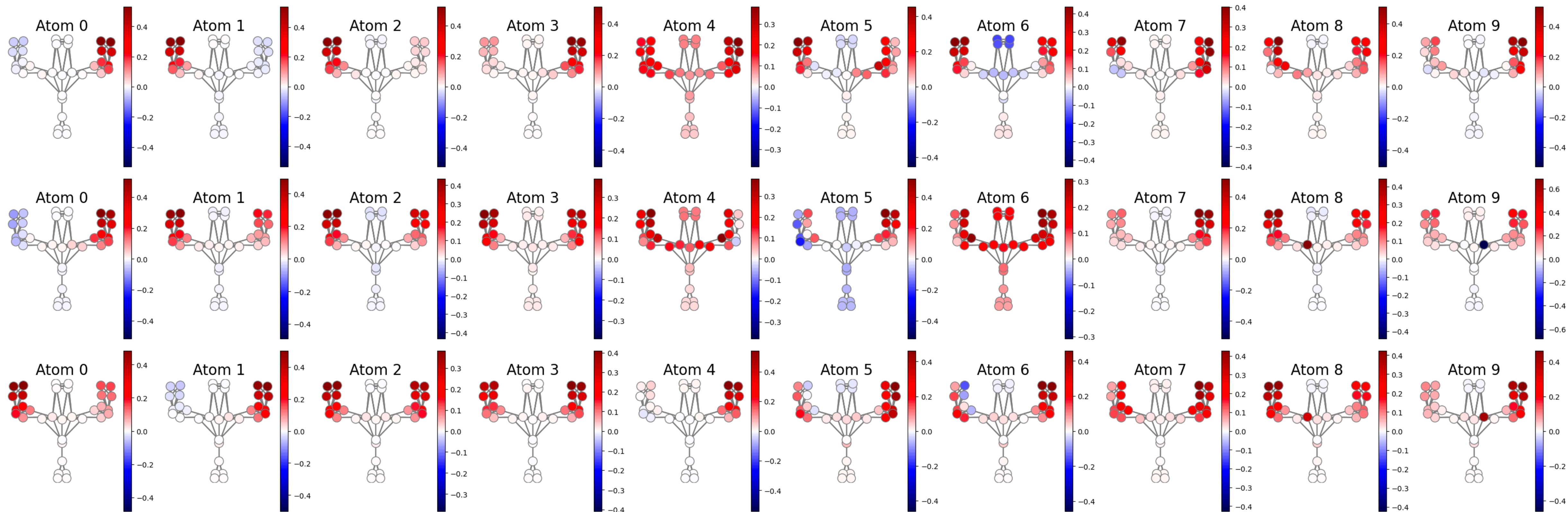
BUT two different movements can easily be distinguished

This second level of activation still allows to capture phenomena specific to signals

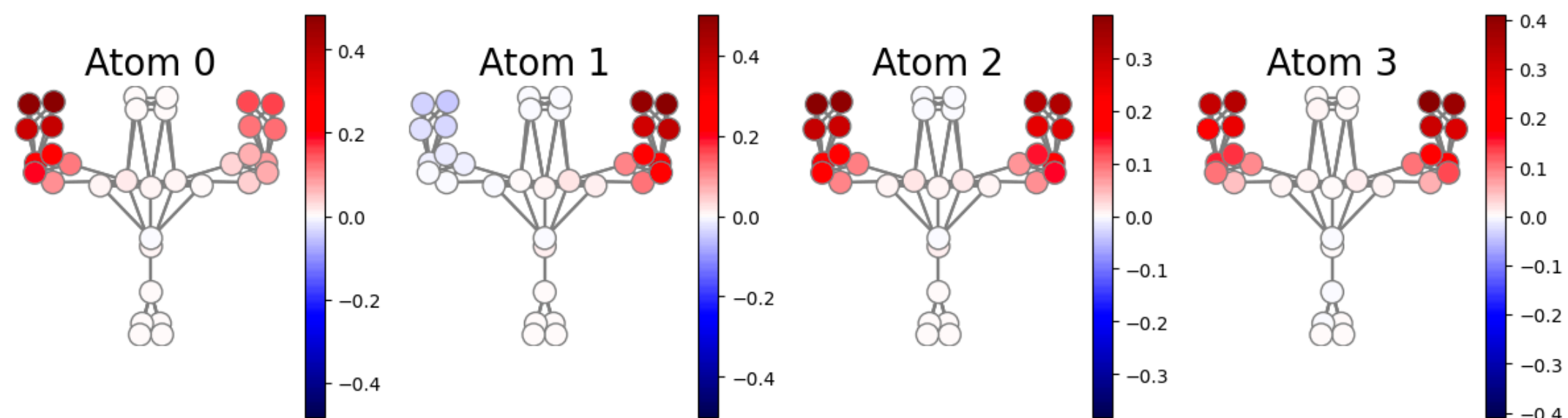
Representations with Fourier basis



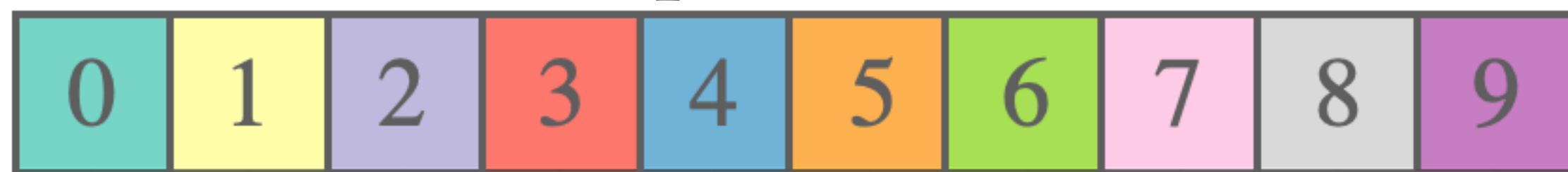
Unconstrained Dictionary



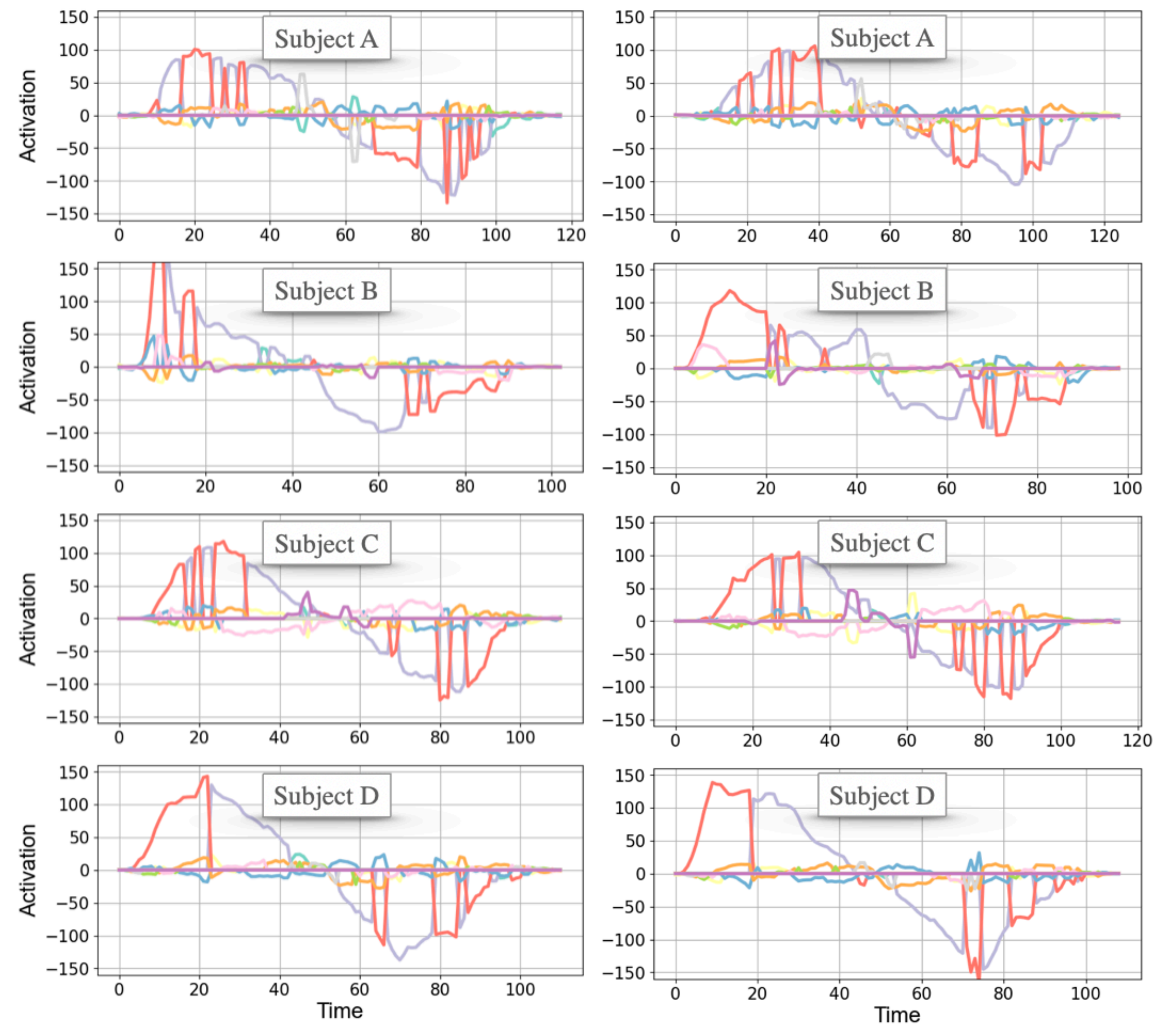
Unconstrained Dictionary



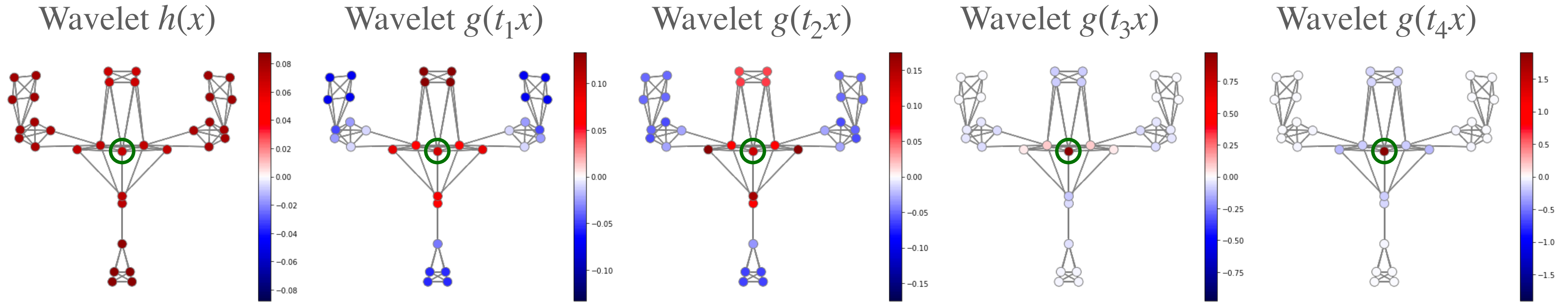
Super-atoms



Bilateral elevation, Z-axis



Mexican Hat Wavelets



$$h(x) = \gamma e^{-\left(\frac{20}{0.4\lambda_{max}}x\right)^4}$$

$$g(tx) = tx \times e^{-tx}$$

$$T_g \hat{\delta}_n(l) = g(\lambda_l) \hat{\delta}_n(l)$$